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### ► To cite this version:

Régis Poulain, Stéphanie Delannoy, Ivan Guillot, Fabienne Amann, Raphaëlle Guillou, et al.. First experimental evidence of oxygen ordering in dilute titanium-oxygen alloys. *Materials Research Letters*, 2022, 10, pp.481-487. 10.1080/21663831.2022.2057202 . cea-03652064

**HAL Id: cea-03652064**

**<https://cea.hal.science/cea-03652064>**

Submitted on 26 Apr 2022

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To cite this article: Régis Poulain, Stéphanie Delannoy, Ivan Guillot, Fabienne Amann, Raphaëlle Guillou, Sylvie Lartigue-Korinek, Dominique Thiaudière, Jean-Luc Béchade, Emmanuel Clouet & Frédéric Prima (2022) First experimental evidence of oxygen ordering in dilute titanium–oxygen alloys, *Materials Research Letters*, 10:7, 481-487, DOI: [10.1080/21663831.2022.2057202](https://doi.org/10.1080/21663831.2022.2057202)

To link to this article: <https://doi.org/10.1080/21663831.2022.2057202>



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## First experimental evidence of oxygen ordering in dilute titanium–oxygen alloys

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### ABSTRACT

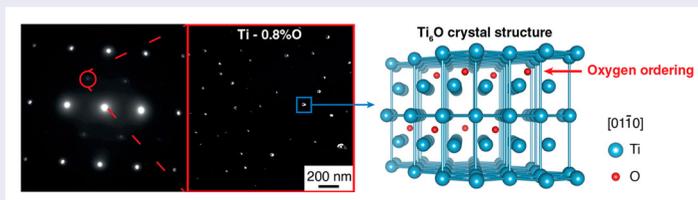
Small addition of oxygen is currently used to improve the mechanical properties of titanium. It has been thought, until now, that oxygen fully dissolves in the titanium matrix, thus leading to a solid solution. However, we show here, with transmission electronic microscopy and X-ray diffraction, that oxygen can also form ordered precipitates with a  $Ti_6O$ -type structure, even for a concentration as low as 0.15 wt% O. The ordered precipitates found in a series of pure binary Ti–O alloys are also visible in commercially pure titanium, including grades 2 and 4, two compositions widely used for technological applications.

### ARTICLE HISTORY

Received 7 February 2022

### KEYWORDS

Titanium alloys; oxygen addition; ordering; nanoparticles; precipitation



### IMPACT STATEMENT

Oxygen-ordered precipitates are experimentally evidenced in a series of Ti–O alloys and in CP titanium. These findings question the paradigm defining oxygen only as a solute atom in titanium alloys.

## Introduction

The hexagonal close-packed (hcp) structure of titanium ( $\alpha$  phase) can incorporate up to 15 wt% oxygen [1], with oxygen addition generally resulting in a large strength increase but also a drastic drop in ductility at room temperature [1–4]. In the early 1970s, a few scattered studies on order–disorder transitions reported that oxygen had a natural tendency to order itself into interstitial superlattices when added in high concentration in titanium  $\alpha$  phase [5–9]. More recently, thermodynamic models relying on *ab initio* calculations have foretold the existence of  $Ti_6O$  ordered compounds [10,11], with oxygen ordering on the octahedral interstitial sites of the hcp lattice, for compositions

as low as 0.3 wt% oxygen at room temperature. However, these predictions have not been supported, so far, by experimental observations of such compounds for oxygen contents below the  $Ti_6O$  stoichiometry. Despite the possibility for oxygen to form ordered compounds, it is generally assumed that oxygen is only found in solid solution in titanium alloys, in particular when describing the impact of oxygen addition on mechanical properties [1,3,12–14]. Here, we set out to challenge these views and investigate the capacity of oxygen to form ordered compounds in the  $\alpha$  phase, for titanium alloys with varying oxygen contents ranging from 0.4 to 0.8 wt% and for commercially pure grade 2 and grade 4 titanium.

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Supplemental data for this article can be accessed here. <https://doi.org/10.1080/21663831.2022.2057202>

## Material and methods

The full investigation is performed on both grade 2 and grade 4 Commercially Pure Titanium (CP-Ti) and on arc-melted 200 g buttons of Ti–O alloys obtained from pure titanium sponges alloyed with TiO<sub>2</sub> powder during the melting stage. As-melted ingots are hot-rolled into square-shaped bars, subsequently annealed at 923 K for 1.8ks for complete recrystallization and water quenched. Samples of all materials are then cold-rolled down to 0.6 mm thick sheets with a reduction level of 40%. The metal plates are finally recrystallized in molten salt baths at 1023 K for 600 s and subsequently water quenched. The chemical composition of the materials is checked by gas analysis (Table 1).

Polished specimens are prepared from as-quenched materials for X-ray diffraction. The latter is performed using a Panalytical XPert Pro diffractometer with Cu K $\alpha$  radiation operating at 45 kV and 40 mA with a precession of the sample. The Rietveld refinement is carried out using the MAUD (Material Analysis Using Diffraction) software [15]. All refinement parameters are initially locked and then manually unlocked according to the following sequence: the baseline is first adjusted, followed by the sample height  $z$  and the lattice parameters of the different crystalline structures. Then, the peak broadening induced by the crystallite size and the micro-strains is corrected by application of the theory of Popa [16], and finally the material texture is adjusted using the Popa function. Conventional Transmission Electron Microscopy (CTEM) and High-Resolution TEM (HRTEM) investigations are performed on samples mechanically polished down to a thickness of roughly 100  $\mu\text{m}$ . Final thinning is carried out with a Tenupol twin-jet electropolishing apparatus using a solution comprising 66% methanol, 27% butanol and 7% HClO<sub>4</sub> at 19 V and at a temperature between  $-10$  and  $-20^\circ\text{C}$ . Samples are then observed with a JEOL 2100+ electron microscope operating at 200 kV. The determination of the precipitate size is carried out from TEM images using the ImageJ software [17] according to the following protocol: a threshold is first performed

so that all precipitates are highlighted and a ‘particle analysis’ is then launched. During this process, highlighted surfaces below 0.5 nm<sup>2</sup> are not taken in account to reduce the contrast noise. Dynamical diffraction patterns have been computed using the software CRYSTAL developed in our laboratory by D. Gratias and M. Quiquandon based on the quantum mechanical formulation of dynamical elastic diffraction of fast electrons [18,19].

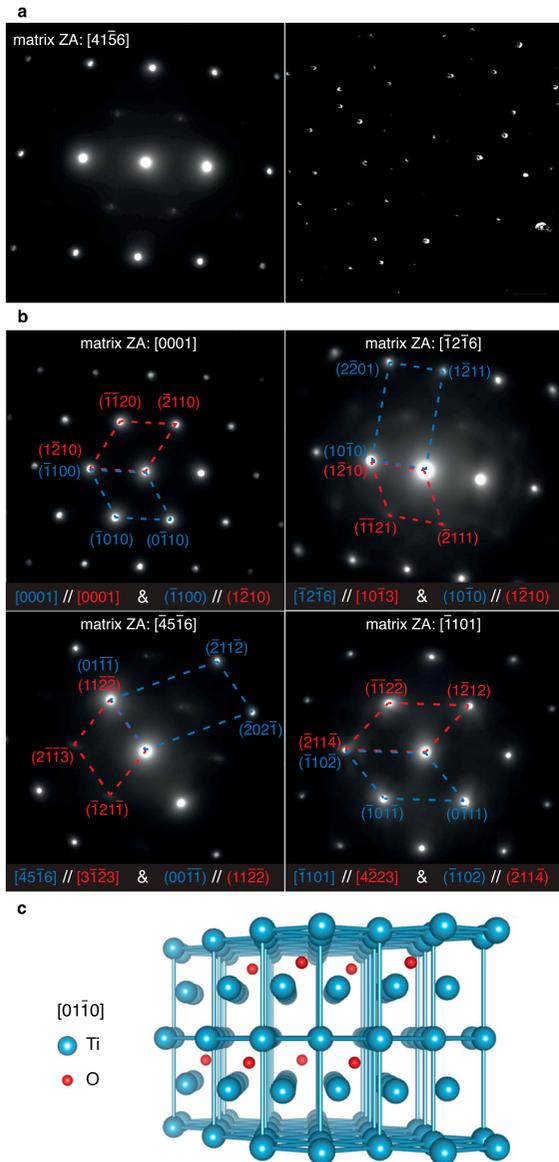
## Results and discussion

SEM/EBSD analysis (not shown here) systematically conducted on all samples confirms that, at the mesoscopic scale, the samples are single-phased with a hexagonal alpha phase. The average grain size varies between 30 and 90  $\mu\text{m}$ , depending on the samples. TEM observations are first performed on the Ti–0.8O (wt%) alloy to investigate the impact of oxygen content on the fine-scaled microstructure. Figure 1(a) reveals that, in some selected zone axes, like in  $[41\bar{5}6]_\alpha$ , superlattice reflections associated with ordering are observed. Dark-field images obtained using these reflections unambiguously reveal nanometric precipitates finely dispersed in the  $\alpha$  matrix. To further investigate the nature of those precipitates, a complete set of Selected Area Diffraction Patterns (SADP) where the precipitates are in diffraction conditions are acquired (Figure 1(b)). In some orientations, superlattice reflections are visible, as in  $[\bar{1}2\bar{1}6]_\alpha$ , and in others, like in  $[\bar{1}101]_\alpha$ , the precipitates diffraction spots are observed to actually be superimposed with the matrix ones. The indexation of a complete set of diffraction patterns shows that the diffraction signature of the precipitates perfectly matches the Ti<sub>6</sub>O crystal structure [7–9] (Figure 1(c)). This trigonal structure (space group P31c) is very close to the one of the  $\alpha$ -matrix, with titanium atoms lying on the same hcp lattice and oxygen atoms ordering every second layer along the  $[0001]_\alpha$  axis with one-third of octahedral sites occupied in each basal layer. The orientation relationship between the two phases inferred from the different TEM diffraction patterns can be defined as follows:  $[0002]_\alpha // [0002]_{\text{Ti}_6\text{O}}$  and  $(1\bar{1}00)_\alpha // (1\bar{2}10)_{\text{Ti}_6\text{O}}$ , which corresponds to the theoretical description available in the literature [6,7] and involves a fully coherent interface between the two phases.

Figure 2 depicts the simulated diffraction patterns of the precipitates structure in the zone axes where superlattices spots are visible. The proposed simulated diffraction patterns assume a sub-stoichiometric Ti<sub>6</sub>O-type structure. To account for all observed superlattice reflexions, it is necessary to consider that the two (0001) layers enriched in oxygen are actually not fully occupied, with

**Table 1.** Composition of the Ti–O alloys measured by gas analysis.

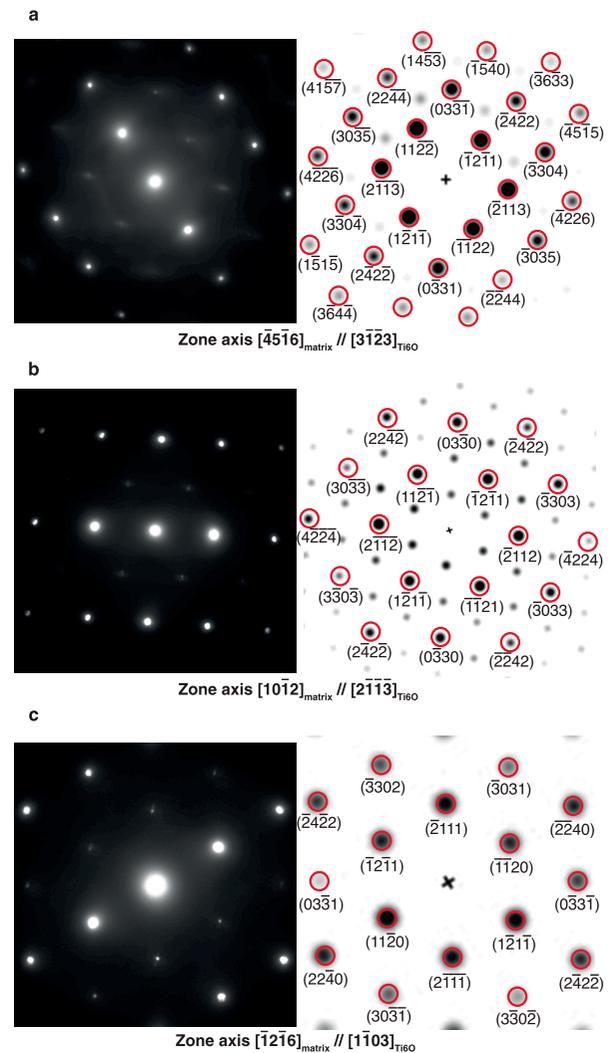
Alloy	Measured composition (wt%)				
	O	N	C	H	Fe
Pure Ti (sponge)	0.059	0.002	\	\	\
Ti–0.4%O	0.415	0.007	< 0.005	< 0.006	< 0.004
Ti–0.6%O	0.603	0.006	\	\	\
Ti–0.8%O	0.768	0.002	\	\	\
Ti-grade 2	0.157	0.003	0.004	0.001	0.034
Ti-grade 4	0.320	0.006	0.007	0.001	0.175



**Figure 1.** Dark-field TEM images of Ti–0.80 alloy and corresponding  $[41\bar{5}6]_{\alpha}$  SADP (a). Red circle indicates the superlattice reflection used to record the dark-field image. Set of SADPs taken in the Ti–0.80 alloy (b). For each zone axis (ZA), the orientation relationship between the matrix (in blue) and the  $\text{Ti}_6\text{O}$ -type precipitates (in red) is specified. Atomic representation of the  $\text{Ti}_6\text{O}$  crystal structure along  $[01\bar{1}0]_{\alpha}$  orientation (c), obtained using VESTA three-dimensional visualization program [20].

a different composition for each layer, thus breaking the mirror symmetry between these two planes existing in the perfect and stoichiometric  $\text{Ti}_6\text{O}$  structure. As a result, a perfect fit of the superlattice spots position is observed between the experimental and simulated patterns. Some spots of the  $[45\bar{1}6]$  and the  $[10\bar{1}2]$  diffraction patterns are not observable on the experimental pattern, which can be explained by their relative much lower intensity.

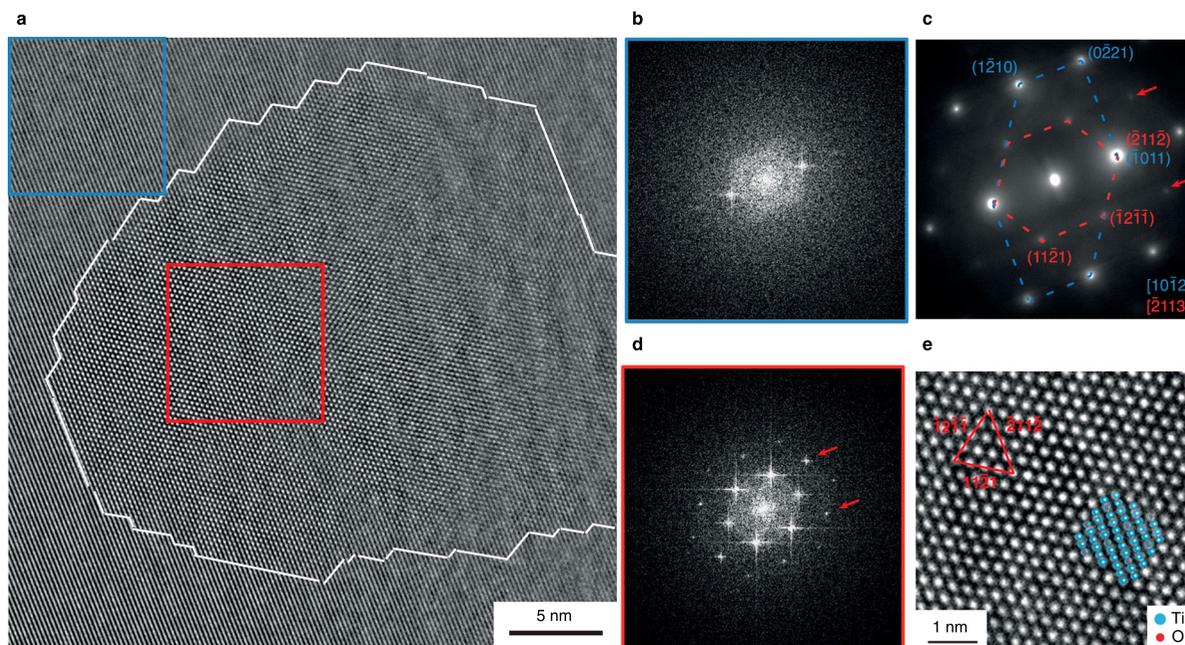
To confirm that the observed superlattice spots correspond to the diffraction signature of precipitates,



**Figure 2.** Comparison of the experimental diffraction patterns and the simulated diffraction patterns of the  $\text{Ti}_6\text{O}$  structure. The chosen zone axes are those in which superlattice spots have been evidenced:  $[45\bar{1}6]$  (a),  $[10\bar{1}2]$  (b),  $[2\bar{1}16]$  (c). The red circles highlight the spots that are visible in the respective experimental image.

High-Resolution TEM (HRTEM) observations are carried out on Ti–0.80 alloy (Figure 3). HRTEM images are taken in such a way that only  $(\bar{1}011)_{\alpha}$  matrix planes are visible (Figure 3(a,b)) so that both phases can be differentiated. Fast Fourier transforms taken both from the matrix area (Figure 3(b)) and inside the precipitate (Figure 3(d)) display the different diffracting planes contributions of both structures. The superimposition of the  $\text{Ti}_6\text{O}$  atomic structure in this direction perfectly fits the observed contrast (Figure 3(e)), showing unambiguously that the ordered precipitates possess a  $\text{Ti}_6\text{O}$ -type crystal structure.

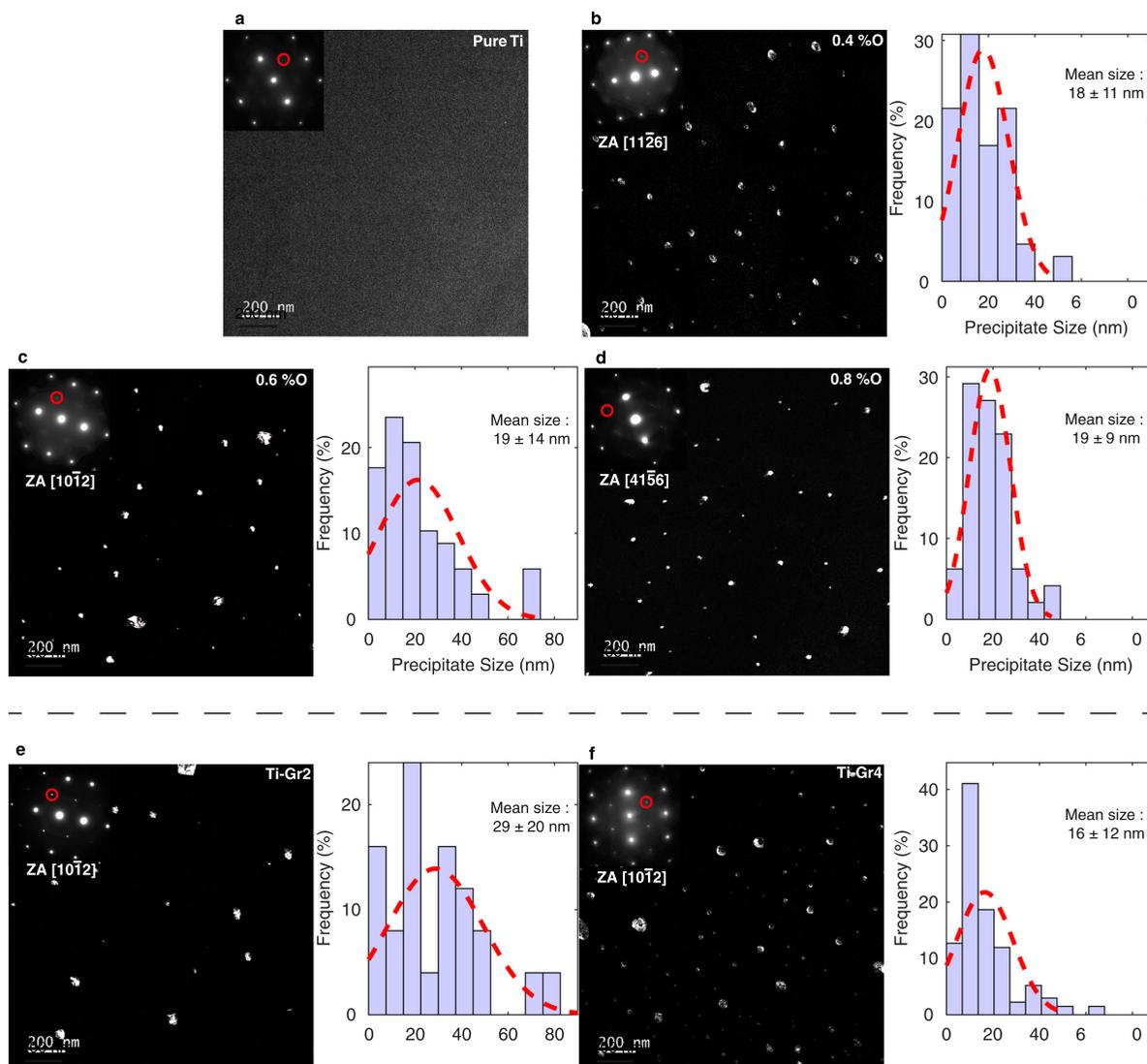
Additional TEM observations reveal that the same ordered precipitates are actually observed in all studied alloys, even at oxygen content as low as 0.157 wt%, in



**Figure 3.** High-resolution TEM image of an ordered precipitate in the Ti-0.80O alloy (a) and associated fast Fourier transforms in the matrix (in blue) (b) and in the precipitate (in red) (d). Corresponding indexed SADP (c). Organization of the atomic columns in the  $\text{Ti}_6\text{O}$  crystal structure and main planes (e). Red arrows highlight the superlattice spots rows.

the Ti grade 2 (Figure 4). The same observations in pure titanium (0.05 wt% of O) did not lead to any precipitate observation, thus confirming that ordered precipitates are not formed during TEM sample electropolishing and that their formation requires an oxygen content higher than 0.05 wt%. It is worth noting that the same ordered precipitates are also observed in the commercially pure grade 2 and grade 4 titanium (Figure 4(e,f)). These two CP Ti alloys contain less oxygen than the pure binary Ti-O alloys synthesized for this study, showing that ordered precipitates can form for an oxygen composition as low as 0.157 wt%. The highest impurity content of these CP alloys, in particular Fe, do not inhibit this oxygen ordering. On the other hand, one should point that such ordered compounds have never been reported before in these CP alloys. Possible explanation is that the superlattices spots corresponding to the  $\text{Ti}_6\text{O}$ -type precipitates are only visible in particular matrix zone axes, like  $[41\bar{5}6]_\alpha$ ,  $[11\bar{2}6]_\alpha$  and  $[10\bar{1}2]_\alpha$ , whereas the most studied zone axes are the one with the lowest indices, such as  $[0001]_\alpha$ ,  $[11\bar{2}0]_\alpha$  or  $[10\bar{1}1]_\alpha$  [21]. One cannot also exclude the potential impact of the thermomechanical heat-treatment on precipitation. Looking now to the variation of the precipitation microstructure among the different alloys, image analyses indicate that the size of the precipitates does not evolve significantly with oxygen content and remains stable around  $\sim 18\text{--}20$  nm.

In order to give a complementary insight on the presence of these ordered nanoprecipitates, X-ray diffraction (XRD) analyses are performed on the different Ti-O alloys (Figure 5). All diffraction patterns display a series of peaks compatible with the sole presence of the  $\alpha$  phase. No additional diffraction peaks are thus observed, which can be reasonably accepted on the basis of the theoretical diffraction intensities of the  $\text{Ti}_6\text{O}$  phase as shown in *Supplementary Information Content Fig. 1*. Indeed, most of the  $\text{Ti}_6\text{O}$  peaks display a relative intensity below 1%, making them hardly detectable by XRD analyses and only peaks corresponding also to diffraction peaks of the  $\alpha$  matrix have a high enough intensity to be evidenced. However, as it will be shown below, these diffraction peaks existing both for the matrix and the ordered precipitates bring important information on the lattice mismatch between both phases. Looking more closely to XRD data, a systematic shoulder can be observed on most of the  $\alpha$  peaks, which intensity increases with oxygen content. This asymmetric broadening is due to the overlap of intense peaks from the  $\alpha$ -Ti matrix with small and broad peaks, at slightly lower angles, arising from the ordered nanoprecipitates. The increasing visibility of these shoulders when the oxygen content increases can be explained by the lattice mismatch evolution between the  $\alpha$ -matrix and the ordered nanoprecipitates. As shown in Figure 5(c), all lattice parameters increase with oxygen content, as determined by Rietveld refinement assuming



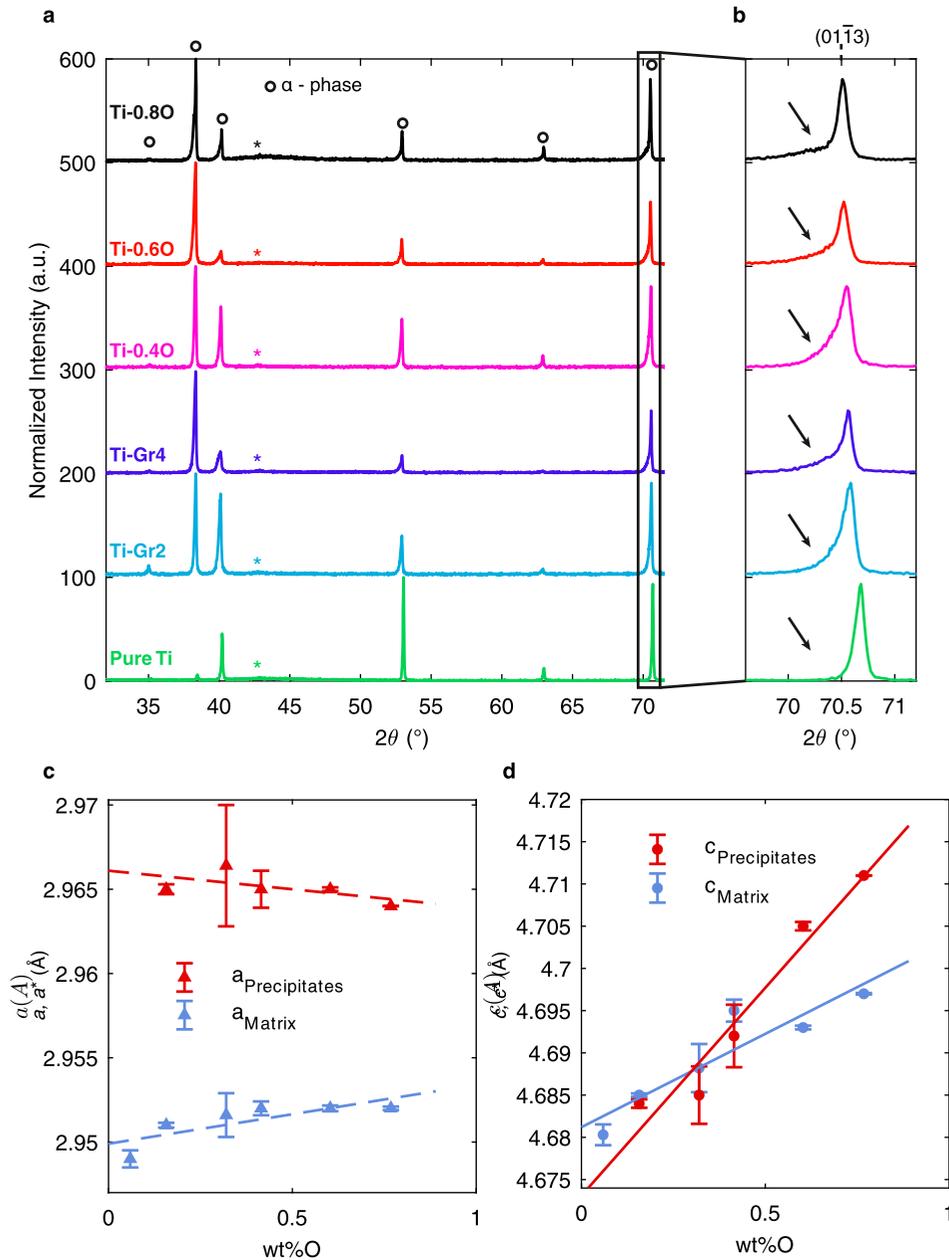
**Figure 4.** TEM observations in dark-field conditions of the pure titanium (a), the Ti-xO alloys with  $x = 0.4$  (b),  $0.6$  (c),  $0.8$  (d), and the titanium grade 2 ( $x = 0.157$ ) (e) and grade 4 ( $x = 0.320$ ) (f). The insets indicate the corresponding zone axis and show the SADPs and the reflections used to record the dark-field images (red circles). The corresponding distribution function of the precipitates size is represented for each alloy.

a mixture of  $\alpha$  phase and of  $\text{Ti}_6\text{O}$ -type ordered phase. The increase in the  $c$  parameter of the precipitates is much stiffer than for the matrix, leading to an increasing mismatch between both structures. Regarding the matrix, it can be calculated that the  $c$  parameter along the  $[0001]$  axis increases more rapidly than  $a$  parameter, i.e. distances in the basal plane, consistently with the known evolution of  $\alpha$ -Ti with oxygen [22,23].

The ordered precipitates evidenced in our work are in agreement with the phase diagram deduced from *ab initio* calculations in [11], showing such an ordering of oxygen atoms at low temperature. Neglecting the potential impact of impurity elements, results obtained in grade 2 CP Ti show that the formation of  $\text{Ti}_6\text{O}$ -type ordered precipitates may occur when the global concentration of

oxygen is above 0.15 wt%. Water-quenched conditions used here does not allow reaching a fully stable equilibrium microstructure. As a consequence, lattice parameters of the two phases, the  $\alpha$  solid solution on the one hand and the ordered precipitates on the other hand, vary with the nominal oxygen concentration, a signature that the composition of these two phases evolves. It may however be noticed that such water-quenched conditions are severe compared to common practice in titanium metallurgy. The formation of  $\text{Ti}_6\text{O}$  precipitates is also expected from softer quenching conditions, with a precipitation microstructure probably closer from equilibrium.

Observation of  $\text{Ti}_6\text{O}$ -type precipitates also call for revisiting our current understanding of oxygen impact on



**Figure 5.** XRD analyses of the Ti-xO alloys (a) and evolution of the shoulder on the  $(01\bar{1}3)$  reflection with oxygen content (b). Evolution of the lattice parameters of the matrix (in blue) and of the precipitates (in red) deduced by Rietveld analysis from XRD data (c). Parameters of the precipitates are normalized by  $a^* = a(\text{Ti}_6\text{O})/\sqrt{3}$  and  $c^* = c(\text{Ti}_6\text{O})/2$  for comparison with the matrix. Error bars represent the estimated error on the values obtained by Rietveld refinement. The peaks marked by the symbol \* in XRD data correspond to an artifact due to sample holder.

the mechanical properties of titanium alloys, which have mostly been described in the light of a strong interaction of individual oxygen atoms with mobile dislocations leading to a drastic strength increase [3,4]. In addition to the usual solid solution contribution, it appears necessary to also consider these ordered precipitates. Finally, beyond the case of the binary Ti-O alloys described in our work, the question of the existence of such ordered  $\text{Ti}_6\text{O}$  precipitates in other titanium alloys naturally arises.

## Conclusion

The Ti-O alloys of this study demonstrate the oxygen capability to order even in diluted titanium alloys. The  $\text{Ti}_6\text{O}$ -type precipitates evidenced here present a crystalline structure very close to the  $\alpha$ -hcp lattice, making them challenging to observe. These observations open promising perspectives which should lead to reconsider the precise role of oxygen on the evolution of the mechanical properties of titanium alloys for example. They also

open a wide scientific field on the role of other possible alloying elements on this ordering tendency: it is not excluded that this ordering may also be actually observed in titanium alloys with a more complex chemistry. Finally, a whole study is to be conducted to understand the thermodynamic origin of this ordering with respect to the thermo-mechanical path followed for these alloys.

## Acknowledgements

M. Quiquandon and D. Gratias are gratefully acknowledged for their help with the TEM diffraction simulations.

## Disclosure statement

No potential conflict of interest was reported by the author(s).

## Funding

BIOTECH DENTAL company is gratefully acknowledged for its financial support on R.P. grant (Industrial CIFRE doctoral fellowship). The French National Research Agency (ANR) is also acknowledged for the funding of Titol Project [ANR-19-CE08-0032].

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