



Temperature dependence of the sorption isotherms of cement-based materials: Heat of sorption and Clausius–Clapeyron formula

Stéphane Poyet*, Sébastien Charles

CEA, DEN, DPC, SCCME, Laboratoire d'Étude du Comportement des Bétons et des Argiles, F-91191 Gif sur Yvette Cedex, France

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ABSTRACT

In the field of radioactive waste management the concrete structures are expected to undergo significant heating due to the waste thermal power and significant drying (in the French design, the temperature is not expected to exceed 80 °C). The durability assessment of such structures thus requires the knowledge of the evolution of the water vapour sorption properties versus temperature. The latter can be easily estimated using the Clausius–Clapeyron (CC) equation: the approach presented hereafter requires the knowledge of the isosteric heat of adsorption and one desorption isotherm (at ambient or any other temperature). Moreover, it is shown that using the CC equation and the desorption isotherms at two different temperatures, it is possible to estimate accurately the desorption isotherm at any other temperature.

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1. Introduction

The durability assessment of concrete structures over long term periods requires the accurate knowledge of their hydric properties, since the water content appears to have a great impact on most durability related properties (creep, shrinkage, transport...). The water retention of any material is usually characterized using a water vapour sorption isotherm. The latter represent the amount of evaporable (free) water retained at equilibrium with an external environment as a function of its relative humidity (RH) for a given constant temperature (isothermal conditions). In the case of cementitious materials, a lot of work has been done since the pioneering studies of Powers and Brownyard [1] and many materials have been characterized, from hardened C₃S pastes to modern concretes (high-performance or self-leveilling concretes...). The great majority of these results were acquired at ambient temperature (that is to say at about 20 °C).

Nevertheless in the framework of radioactive waste management, the concrete structures for interim storage are expected to undergo significant heating due to the waste thermal power. In the French design of subsurface structures, the cooling should be achieved using natural convection with air taken from the outside. The concrete temperature is expected to reach up to 80 °C in nominal conditions (without exceeding it) and the concrete structure is expected to undergo severe drying (due to the temperature increase of the ambient air) [2,3]. The durability assessment of these structures over 300 years thus requires the accurate knowledge of the sorption properties of concretes at such unusual

temperature levels with particular interest in the first desorption (corresponding to the drying process).

Very few articles were published regarding the effect of temperature on water sorption isotherms of cementitious materials with special interest in the first desorption. In a recent study [4] the first desorption of a high-performance concrete (cured at 20 °C, the concrete composition is given in Table 1 of Appendix A) was characterized at 30 °C and 80 °C. The results are depicted in Fig. 1; the GAB model [5] was used to fit the results as a guide for the eyes. The GAB model is an evolution of the well-known BET model introducing a third parameter k which extends its domain of validity almost over the whole RH range. More information about the fitting can be found in [4], the GAB model is described in detail in [5–7]. The equation of the GAB model is:

$$w = \frac{Ckw_m h}{(1 - kh)[1 + (C - 1)kh]} \quad (1)$$

where w is the water content (by mass, it is equal to the ratio of the mass of water and the mass of dry solid), h is the relative humidity and C , k and w_m are three positive parameters. The values of the three parameters of the GAB model are reported in Table 2 of Appendix A.

One can see the important effect of temperature on the experimental curve: at 30 °C the isotherm is almost a straight line whereas at 80 °C the shape is greatly modified (non linearity). This leads to the significant decrease of the amount of adsorbed water for a given relative humidity (RH) at higher temperatures. This effect is not the same over the whole RH range: for instance at saturation (RH = 100%) the reduction is about 0.9% (absolute value), whereas it is about 2.5% at RH = 80% [4].

* Corresponding author.

E-mail address: stephane.poyet@cea.fr (S. Poyet).

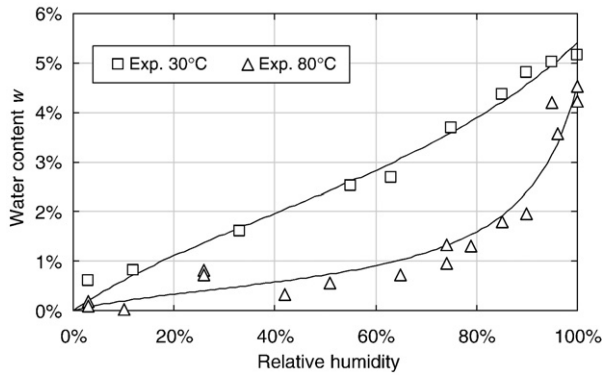


Fig. 1. Experimental characterization of the first desorption isotherms at 30 and 80 °C of a high performance concrete cured at 20 °C [4]. The two solid lines represent the fitting of the results using the GAB model.

The same conclusions can be drawn on the basis of the results obtained by Hundt and Kantelberg [8] and more recently by Ishida et al. [9]. In addition, Hundt and Kantelberg have characterized the first desorption isotherm of different cementitious materials (from cement paste to concrete) for four temperatures (20 °C, 45 °C, 57.5 °C and 70 °C): They have shown that the impact of temperature was also significant even at 45 °C (see the results in Fig. 2). The origin of this phenomenon was discussed in a previous article [4]. It is believed by the author that it is neither due to the microstructure modification induced by temperature nor the water properties evolution. As a matter of fact, adsorption is known to be an exothermic process [10,11]; according to the principle of Le Chatelier and the law of Van't Hoff [12] which state that an exothermic process is hindered when temperature is increased (and reciprocally it is enhanced when temperature is decreased) a temperature increase promotes desorption. This leads to a decrease of the number of adsorbed molecules and then a fall in the water content [4].

From those results, it can be concluded that the impact of temperature on the first desorption of cementitious materials is very important. As a consequence, it appears compulsory to account for this phenomenon in the durability assessment of concrete structures subjected to temperatures higher than the ambient, and the evolution of the first desorption isotherm versus temperature must be known. Experimental characterization of this evolution would be problematic due to the time needed to reach equilibrium and the number of experiments needed to cover the whole temperature range. It appears clearly that a method for accurate prediction of the isotherm evolution versus temperature would be a great help.

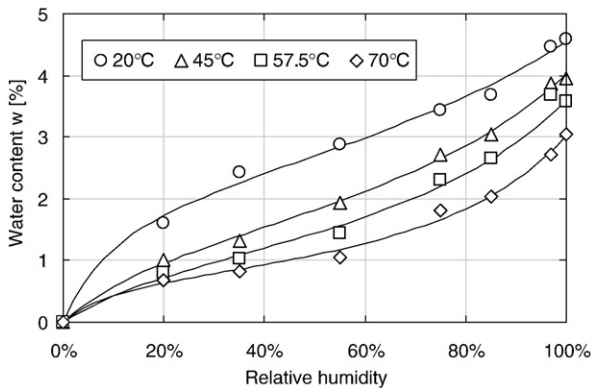


Fig. 2. First desorption isotherm of a concrete (labelled 'beton 5') for four temperatures, after Hundt and Kantelberg [8]. The solid lines stand for the fitting of the experimental results using the GAB model.

Such a method is presented in this article. It is assumed that the isotherm evolution is only due to the “thermal desorption”: that is to say the shift of equilibrium (adsorbed water-vapour) induced by the temperature increase. The potential microstructure changes are not considered. The method is based on the Clausius–Clapeyron (CC) formula which describes the heat involved in the sorption process. This method allows, on the basis of the results obtained at only two temperatures, an accurate and reliable estimation of the isotherm for any other temperature. It is based on the description of the evolution of the sorption heat as a function of the amount of water adsorbed. As illustration and validation, this method is applied to the high performance concrete [4] and then to the concrete characterized by Hundt and Kantelberg [8].

2. Theoretical considerations

2.1. Equation of Clausius–Clapeyron

The Clausius–Clapeyron (CC) equation can be used to describe the heat involved in the sorption process [10]:

$$Q_{st}(w) = -R \left[\frac{\partial \ln(p)}{\partial (1/T)} \right]_w \quad (2)$$

where p and T are the pressure of the adsorbate (water vapour in our case) at equilibrium (in Pa) and the absolute temperature (in K); R is the ideal gas constant ($R = 8.314$ J/mol/K) and Q_{st} stands for the amount of energy involved in the sorption process; it is known as the isosteric heat of sorption (it is also known as the enthalpy of sorption in J/mol). Note that in Eq. (2), the subscript w indicates that the derivation operation must be carried out for a constant amount adsorbed w (in isosteric conditions).

The demonstration of this equation can be found for instance in [13–16]. It is based on two approximations: the adsorbate is considered as an ideal gas and the volume of the adsorbed phase is neglected in comparison to the gas bulk phase. These two assumptions are reasonable at atmospheric pressure (that is always the case for water vapour adsorption in cementitious materials) yet they are known to induce deviation from reality for high pressures (up to several atmospheres) [17].

2.2. Isosteric heat of sorption

Integrating Eq. (2) between the two equilibrium states (T_1, p_{v1}) and (T_2, p_{v2}) for any arbitrary constant water content w leads to Eq. (3):

$$Q_{st}(w) = R \ln \left[\frac{p_{v1}(w)}{p_{v2}(w)} \right] \left(\frac{T_1 T_2}{T_1 - T_2} \right) \quad (3)$$

where the two absolute temperatures T_1 and T_2 are different and p_{v1} and p_{v2} are the vapour pressures at equilibrium with the (constant) water content w . This Eq. (3) can be used to estimate the heat of sorption of the high performance concrete which has been characterized at 30 °C and 80 °C in [4] (Fig. 1). Obviously, the number of experimental temperatures (only two) is too low to give an accurate evolution of the isosteric heat of sorption; the goal of this application is to serve as an illustration of the use of the CC equation. It is also expected to yield valuable information about water vapour adsorption in cementitious materials.

Due to the lack of experimental data the calculation of the isosteric heat of sorption was carried out using the fitted GAB functions. The vapour pressure at equilibrium with the arbitrary water content w at the temperature T_i was calculated using the GAB reciprocal relation:

$$p_{vi}(w) = \frac{p_{vs}(T_i)}{2k_i(1-C_i)} \left[\alpha_i - \sqrt{\alpha_i^2 - 4(1-C_i)} \right] \quad (4)$$

where $p_{vs}(T_i)$ is the saturation vapour pressure for the temperature T_i and α_i is equal to:

$$\alpha_i = 2 + \left[\frac{w_{mi}}{w} - 1 \right] C_i \quad (5)$$

where C_i , k_i and w_{mi} are the three parameters of the GAB model for the fitting of the experimental results obtained at the temperature T_i (see Table 2). Taking arbitrary values for w allows calculating the vapour pressures at equilibrium for the two temperatures 30 °C and 80 °C and then the corresponding isosteric heat of sorption $Q_{st}(w)$. In practise a total number of 32 different water content values were used, ranging from 0% to 4.60% (the maximal value obtained experimentally at 80 °C).

The variation of the pressure at equilibrium with the constant amount of adsorbed water w as a function of the inverse of the temperature applied is plotted in Fig. 3. Each line stands for a different constant water content w . The low water contents are located at the bottom of the graph (low vapour pressure) whereas the high water contents are located in the upper part of the graph (high vapour pressure). This chart is a graphical illustration of the CC equation, since according to Eq. (2) the slope of each line is equal to $-Q_{st}(w)/R$.

The evolution of the isosteric heat of sorption versus the water content (as obtained from the slopes of lines in Fig. 3) is plotted in Fig. 4 (the values obtained are reported in Table 4). One can note that for low water contents, the isosteric heat first increases and reaches a maximal value ($Q_{st} \approx 68$ kJ/mol) for $w \approx 0.5\%$. It then decreases slowly and tends towards 43 kJ/mol for high water contents. The high values observed for low water contents are representative of strong bonding between the adsorbed water molecules and the cementitious substrate. The isosteric heat decrease according to the increase of water content can be related to the decrease of the influence of the substrate with the increase of the distance between the adsorbed water molecules and the substrate. The value reached at high water contents (~ 43 kJ/mol) is representative of the average water condensation enthalpy between 30 and 80 °C [18]: it can be considered that there is no more influence of the substrate, water molecules are bound the ones to the others.

3. Prediction of the effect of temperature

3.1. Presentation of the methodology and main results

We have just seen that the CC formula can be used on the basis of sorption isotherms at different temperatures to calculate the isosteric heat of sorption. Nevertheless, knowing the evolution of the isosteric heat of sorption, it can also be used to estimate the impact of

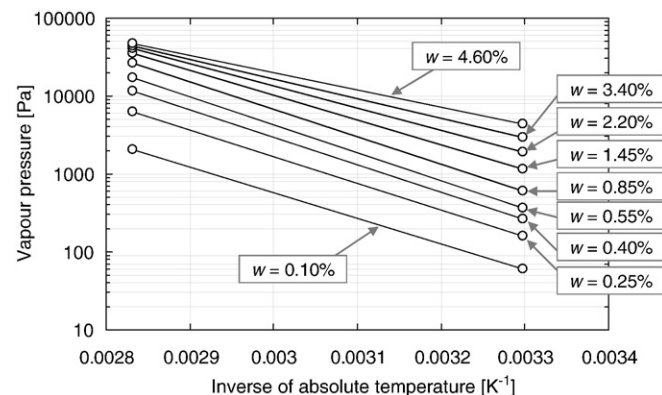


Fig. 3. Isosteric chart (isosteres of desorption) of the experimental results for the high performance concrete tested in [4]: application of Eq. (3) between 30 °C and 80 °C. Each line corresponds to a different (constant) water amount w .

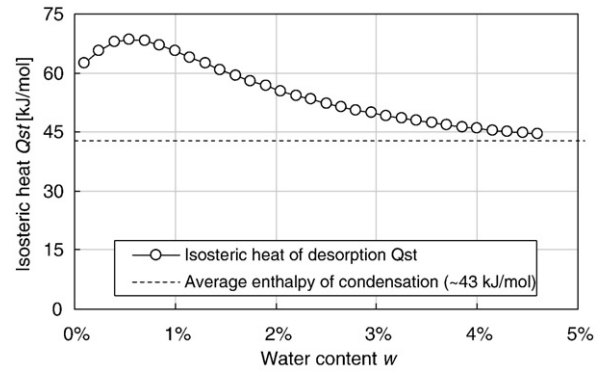


Fig. 4. Isosteric heat of sorption Q_{st} as a function of the water content w for the high performance concrete tested in [4].

temperature and yield a prediction of the evolution of sorption isotherms for different temperatures. Integrating Eq. (2) between the two states (T_1, p_{v1}) and (T_2, p_{v2}) at equilibrium with the constant water content w leads to:

$$RH(T_1, w) = RH(T_2, w) \frac{p_{vs}(T_2)}{p_{vs}(T_1)} \exp \left[\frac{Q_{st}(w)}{R} \left(\frac{T_1 - T_2}{T_1 T_2} \right) \right] \quad (6)$$

where $RH(T_i, w)$ is the relative humidity at equilibrium with the adsorbed water content w at the temperature T_i (with $i = \{1; 2\}$). In Eq. (6), the sorption isotherm is assumed to be known at the temperature T_2 (the relation between the water content w and the relative humidity RH is known) in order to compute its evolution at the temperature T_1 .

Eq. (6) was applied to the high performance concrete described earlier [4] on the basis of the results obtained at 30 °C and 80 °C, the desorption isotherms were then computed for temperatures ranging from 5 °C to 105 °C. An arbitrary constant water content w was chosen and $RH(T_1, w)$, the relative humidity at equilibrium at the temperature T_1 (80 °C) with the water content w , was computed using Eq. (6). The relative humidity at equilibrium at the temperature T_2 (30 °C) was estimated using the GAB inverse function defined in Eqs. (4)–(5). The isosteric heat of sorption determined above (depicted in Fig. 4) was used and the reference curve was the one obtained at 30 °C. It was also verified that the same results were obtained using the 80 °C results as a reference.

The resulting predicted desorption isotherms for different temperatures are presented in Fig. 5. The two solid lines stand for the experimental results at 30 °C and 80 °C fitted using the GAB model and used for the calculation of the isosteric heat of sorption. The other curves (with open symbols) stand for the prediction for temperatures ranging from 5 °C up to 105 °C. One can note the spectacular impact of

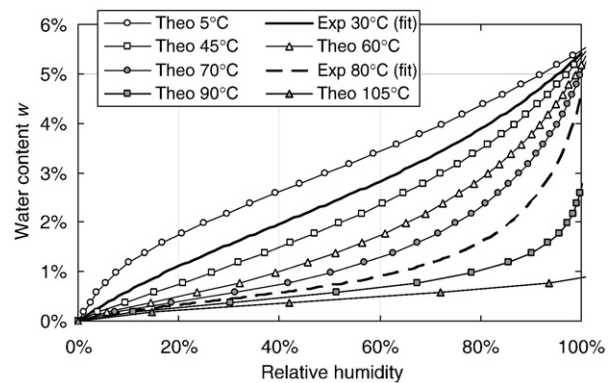


Fig. 5. Prediction of the impact of temperature (from 5 °C up to 105 °C) on the first desorption isotherms for the concrete described in [4] (solid lines stand for the experimental results obtained at 30 °C and 80 °C fitted using the GAB model and dotted lines stand for the predictions for temperatures ranging from 5 °C to 105 °C).

temperature on the (estimated) first desorption isotherm of the studied high-performance concrete.

The general shape of the isotherm can be greatly modified according to the considered temperature: thanks to the measurements it was found to be almost a straight line at 30 °C and a non linear curve with an upward deviation at 80 °C, whereas the CC equation yields an almost type I isotherm at 105 °C (representative of monomolecular adsorption without capillary condensation).

Another expected consequence of the temperature variation is the evolution of the adsorbed water amount: the lower the temperature, the higher the amount of adsorbed water. This phenomenon is expected to be observed at any temperature over the whole RH range and even at saturation (*i.e.* for $RH = 100\%$). This can also be witnessed on the results of Hundt and Kantelberg [8].

Another important point concerning the impact of temperature is the absence of temperature threshold: any temperature modification is expected to induce the modifications presented above on the desorption curve. For instance, the desorption isotherm at 20 °C is expected to be different from the one measured at 30 °C in spite of the low difference of temperature. Moreover, it appears that the evolution of the desorption isotherm between 5 °C and 30 °C (which are assumed to be representative of the ambient temperature variation for an average concrete structure in France) cannot be considered negligible: for instance, at $RH = 40\%$ the water content is expected to fall from 2.6% at 5 °C down to 2.0% at 30 °C.

All the conclusions above are drawn on the basis of the application of the CC formula using the first desorption isotherm of a high-performance concrete obtained experimentally at 30 °C and 80 °C. The confidence in these conclusions relies on the following validation.

3.2. Validation of the methodology

The methodology introduced in the previous paragraph was applied to some of the results of Hundt and Kantelberg [8] in order to estimate the ability of the CC equation to predict the evolution of the desorption curves as a function of temperature. The results presented in Fig. 2 were used (labelled 'beton 5' in Ref. [8]). In this part, the isosteric heat of sorption was calculated using the results obtained at only two temperatures and the desorption isotherm was computed using Eq. (6), for the two other temperatures and then compared to the experimental results.

First, the isosteric heat of sorption was estimated (the values obtained are reported in Table 5) using the experimental results obtained at 20 °C and 70 °C (see Fig. 7) and the theoretical desorption isotherm at 45 °C and 57.5 °C was then computed. The experimental curve at 20 °C was used as a reference for the calculation, it was verified that the same results were obtained using the experimental isotherm at 70 °C as reference. Fig. 6 presents the comparison

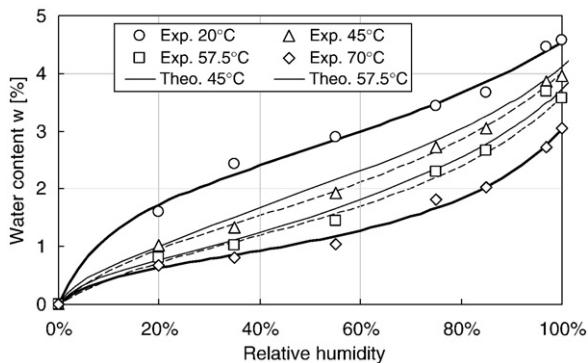


Fig. 6. Comparison between the desorption isotherms measured and predicted at 45 °C and 57.5 °C on the basis of the measured results at 20 °C and 70 °C only (from Hundt and Kantelberg [8]). The two dotted lines stand for the GAB fitting of the experimental results at 45 °C and 57.5 °C.

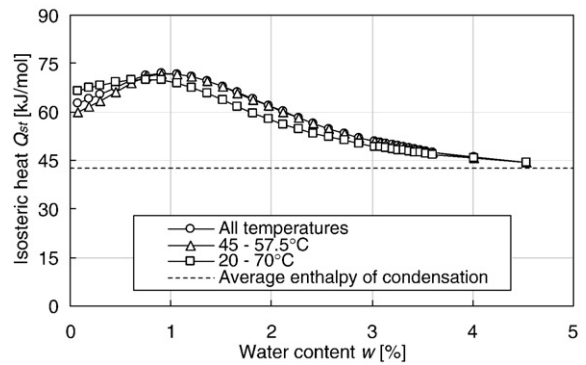


Fig. 7. Evolution of the isosteric heat of sorption Q_{st} for 'beton 5' on the basis of the results obtained by Hundt and Kantelberg [8].

between the predicted isotherm at 45 °C and 57.5 °C and the experimental results obtained by Hundt and Kantelberg [8]. One can see the good correspondence between the measurements and the theoretical curves predicted using CC.

Nevertheless, the estimation of the isotherms was done on the basis of the results for the two extreme temperature values for which the measured difference is maximal. One can thus expect this calculation to give the best results. Another set of predictions was then carried out: the isosteric heat of sorption was determined (the values obtained are reported in Table 5) on the basis of the results obtained at 45 °C and 57.5 °C (see Fig. 7) and the desorption isotherms at 20 °C and 70 °C was then estimated using CC. The results are presented in Fig. 8. Once more the correspondence between the measured and the predicted results is good.

In both cases, the prediction of the isotherm yield good results: the shape of the curves is clearly reproduced and the difference between the measured and the predicted water contents remains limited. The latter was characterized using the following function:

$$E(T, RH) = \frac{|w_{theo}(T, RH) - w_{exp}(T, RH)|}{w_{exp}(T, RH)} \quad (7)$$

where E is the relative difference between measurements and prediction and w_{theo} and w_{exp} are the water content calculated using CC and obtained experimentally respectively. Fig. 9 presents the evolution of the relative difference E between the measured water contents and the ones predicted using CC. One can note that in most cases the relative difference remains very limited (its values range from 1% up to 8%, with a mean value which is less than 5%) except for $RH = 35\%$ and $RH = 55\%$ for which the relative difference reaches

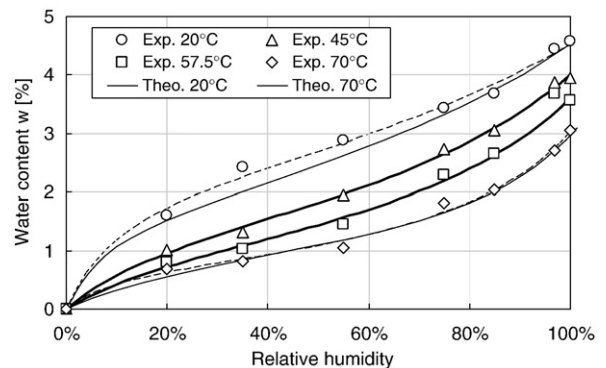


Fig. 8. Comparison between the desorption isotherms measured and predicted at 20 °C and 70 °C on the basis of the results measured at 45 °C and 57.5 °C only, (from Hundt and Kantelberg [8]). The two dotted lines stand for the GAB fitting of the experimental results at 20 °C and 70 °C.

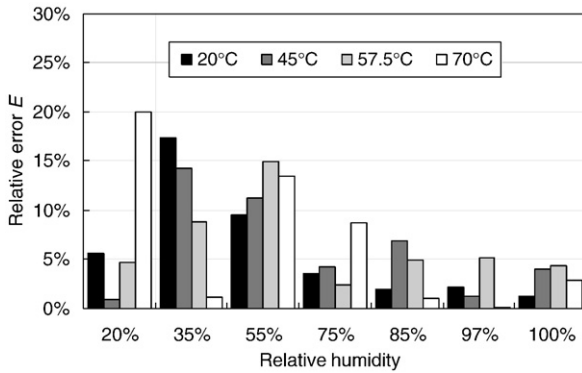


Fig. 9. Evolution of the relative difference between the estimated and measured adsorbed water amounts for different RH in the case of beton 5 [8].

values ranging from 10% to 20%. This is mainly due to the scattering observed in the fitting of the experimental results using the GAB model for these two RHs (Fig. 2).

4. Discussion

4.1. Heat of sorption of cementitious materials

Fig. 5 shows the important impact of temperature on the first desorption isotherm. The only parameter controlling this evolution versus temperature is the isosteric heat of sorption Q_{st} (see Eq. (2)).

There are very few results in the scientific literature about the heat of sorption for cementitious materials. According to the authors' knowledge, Powers and Brownyard [1] were the first to characterize the heat of sorption of cementitious materials. They used the so-called heat-of-solution method and two different cement pastes ($W/C = 0.50$). The experiment consisted in the dissolution of dry pastes followed by the dissolution of similar samples containing adsorbed water. The comparison of the heat involved in the two processes allowed them to estimate the differential heat of adsorption Q_a [cal/g] and to propose the following function:

$$Q_a = \frac{858}{\left(1.31 + \frac{w}{w_m}\right)^2} \quad (8)$$

where w_m is the monolayer capacity of the studied cement pastes: the ratio (w/w_m) represents the number of adsorbed layers. According to the Hess's law [1,12,19], the isosteric heat Q_{st} [kJ/mol] can thus be estimated by adding the latent heat of condensation $L = 42.7$ kJ/mol:

$$Q_{st} = (L + Q_a) = 42.7 + \frac{64.6}{\left(1.31 + \frac{w}{w_m}\right)^2} \quad (9)$$

Fig. 10 presents the evolution of the heat of sorption (differential and isosteric) according to the law proposed by Powers and Brownyard [1]. The heat of sorption is a decreasing function of the water content: the more the water content, the lower the heat of sorption. The maximal value of the isosteric heat is about 80 kJ/mol. According to Eq. (9), the value decreases with the increase of the water content and the curve tends towards the latent heat of condensation (42.7 kJ/mol) for high water contents.

Results of the same kind have been obtained using three hardened cement pastes (two were steam-cured at 97 °C and the last one was cured at room temperature) with various W/C ratios by Radjy et al. [20] and Sellevold and Bjøntegaard [21]. The experiments were carried out using the so-called Thermo Piestic Analyser system (TPA system) and the sorption isotherms were characterized for temperatures ranging from 0 °C to 80 °C. The isosteric heat of sorption was

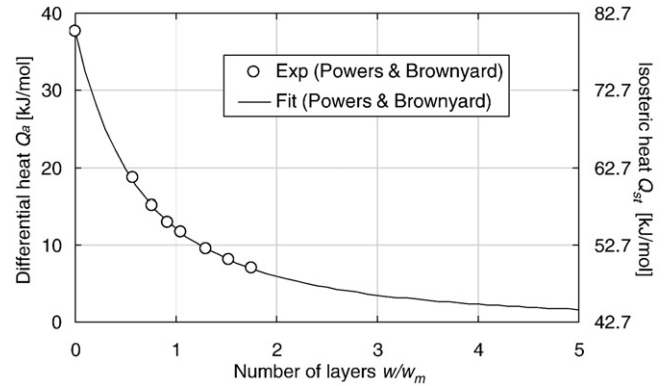


Fig. 10. Evolution of the differential (Q_a) and isosteric (Q_{st}) heats of sorption as functions of the water content w (according to Powers and Brownyard [1]).

then estimated on the basis of the results acquired for all the materials tested. Similar evolution as the one depicted on Fig. 10 was obtained: the maximal value reached is about 80 kJ/mol for the three cement pastes, the isosteric heat decreases when the water content increases and it tends towards 42.7 kJ/mol for high water contents.

Nielsen and Kronholm [19] studied the RH at equilibrium above a mortar ($W/C = 0.2$) for temperatures ranging from 20 °C to 35 °C. They derived the differential sorption enthalpy using the CC equation. Their results show a good correspondence with the empirical formula proposed by Powers and Brownyard [1] (see Eq. (8)) for two experiments (among three): the same order of magnitude was found and the same decrease with the increase of RH was observed. Nonetheless, their results do not cover the whole RH range (typically from 50% to 95%) and one experiment deviated from the proposed formula (the values obtained are twice as much as the empirical equation).

Fig. 11 depicts the comparison between the isosteric heats of sorption as obtained in this study, and after Hundt and Kantelberg (beton 5) [8] and Powers and Brownyard [1]. The three curves show a similar pattern yet the two curves obtained using the results from Poyet [4] and Hundt and Kantelberg [8] slightly differ from the curve proposed by Powers and Brownyard [1]. The isosteric heat of sorption first increases with the water content until a maximum is reached, it then decreases and tends towards the heat of condensation $L = 42.7$ kJ/mol. Note that the slope of both increasing and decreasing phases is different for the two concretes. Also note that the two maximal values reached are different (68 and 72 kJ/mol for Poyet and Hundt and Kantelberg respectively). This comparison tends to indicate that the evolution of the isosteric heat of sorption depends on the considered cementitious material.

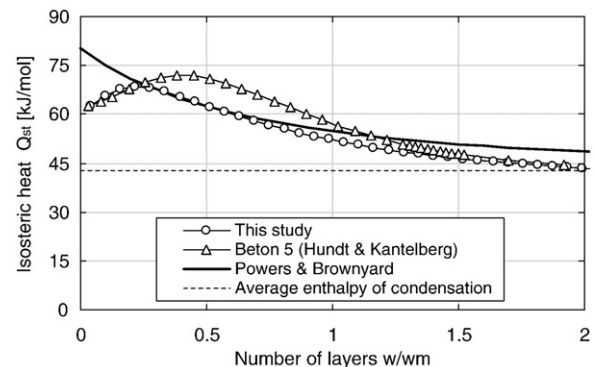


Fig. 11. Comparison between the isosteric heats of sorption obtained in this study, derived from the results of Hundt and Kantelberg [8] and proposed by Powers and Brownyard [1].

In the scientific literature the decrease of the isosteric heat of sorption with the increase of the water content and an asymptotic value about 45 kJ/mol is generally observed for many different materials: food or aromatic leaves [22–30], soils and minerals [31–36] or engineered materials [37–43]. A monotonic decrease is generally reported. The latter is generally explained by the reduction of the influence of the hydrophilic surface (attractive forces) induced by the increase of the numbers of adsorbed layers [44]. The asymptotic value of 45 kJ/mol is representative of water-to-water bonding (liquid state).

Yet an increase for low water contents was observed for porous carbons [40–43] and carbohydrate polymers [37]. In the case of porous carbons the low initial isosteric heat of sorption (between 15 and 20 kJ/mol) is explained by a very small number of hydrophilic sites. The increase is attributed to the creation of water clusters (H-bonding between water molecules). In the case of carbohydrate polymers [37] the initial heat of sorption was found to be higher than 45 kJ/mol (about 60 kJ/mol), the increase (up to 70–80 kJ/mol) was associated to the polymer matrix swelling which would activate new adsorption sites. Similar increase for low water contents were observed with carrot [45] and bentonite [46] but no clear explanation was given.

In the case of montmorillonite, Zhang and Low [47] studied the evolution of the heat of immersion in relation to the initial water content. They showed that the heat of immersion did not decrease continuously: the latter passed by a minimum and then a maximum to eventually tend towards zero. They thus showed that energy was consumed in order to expand the montmorillonite layers. In our case, it is difficult to draw any conclusion. One has to keep in mind that the increase of the isosteric heat of sorption was found on the basis of smoothed experimental results. Moreover the small number of results for low water contents is expected to induce uncertainties in estimating the isosteric heat of sorption. The maximum observed in the evolution of the isosteric heat of desorption might just be an artefact of the estimation process as well as representative of a real phenomenon. It then appears that more studies on cementitious materials are needed, with a special interest in low water contents.

4.2. About the prediction of the effect of temperature

It was shown above that the CC equation is a powerful tool for the prediction of the impact of temperature on the first desorption isotherm. Only one parameter is needed (the isosteric heat of sorption Q_{st}) to describe the evolution of desorption isotherms versus temperature: knowing the desorption curve at one temperature and using CC, one can accurately predict the curves for any other temperature (see an example on Fig. 5 and see Figs. 6 and 8 for the validation).

The main issue of this method is that the isosteric heat of sorption Q_{st} must be known. It was shown above that the latter can be identified using two different isotherms (at two different temperatures). Of course the reliability of the method (and then of the results obtained) depends on the quality of the input data (experimental results).

Nonetheless, obtaining the sorption isotherm at different temperatures is a long and difficult task which may be hard to accomplish. The main question is thus: can the isotherms at different temperatures of a concrete be estimated using the isosteric heat of sorption obtained on another concrete? Or using a generic evolution such the one proposed by Powers and Brownyard [1]? These questions are interesting given that the three evolutions drawn on Fig. 11 show a similar pattern.

To answer this question the desorption isotherm of beton 5 [8] at 45 °C, 57.5 °C and 70 °C was estimated using CC. The reference curve was the one obtained at 20 °C. Three different isosteric heats of sorption were used for the computations: the one obtained in this study, the one proposed by Powers and Brownyard [1] and the proper one derived from the results obtained at the four temperatures. Fig. 12 presents the comparison between the three isosteric heats of sorption

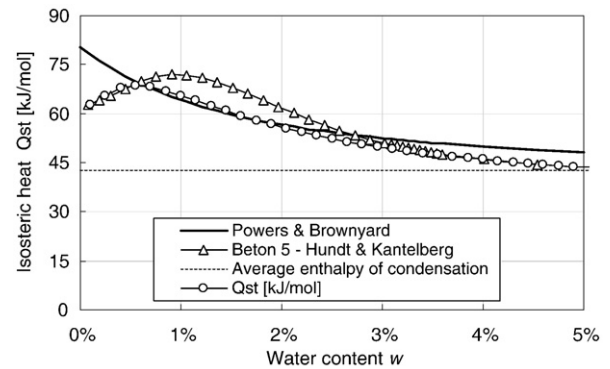


Fig. 12. Evolution of the isosteric heats of sorption Q_{st} used for the estimation of the desorption isotherm evolution versus temperature for beton 5 [8].

versus the water content w of beton 5. One can note that beyond $w \approx 1\%$ the three curves are very similar.

Fig. 13 presents the isotherm at 70 °C predicted using the three isosteric heats of sorption depicted on Fig. 12. One can see that the curve (dotted line) estimated using the data derived from the experimental points for the four temperatures fit very well the experimental results as demonstrated earlier. The two other curves (obtained using the isosteric heats of sorption proposed by Powers and Brownyard and estimated in this study) do not fit as well. In each case, the experimental pattern is clearly not reproduced (for instance using Powers and Brownyard heat of sorption, the knee and the upward deviation are not reproduced). Moreover, it can be seen that the water contents predicted using the heats of sorption from Powers and Brownyard and this study greatly differ from the values obtained experimentally. The difference was characterized using the relative error E defined in Eq. (7); the results are presented in Fig. 14. One can see that the relative error obtained using unrelated isosteric heats can be very large (up to 75%) whereas the use of proper data leads to an error included in the range 0%–12%. Note that the relative error presented in Fig. 14 is different from the one from Fig. 9. This is due to the fact that the isosteric heat used in Fig. 14 was identified using the data of the four temperatures (20, 45, 57.5 and 70 °C) whereas only two temperatures were used in Fig. 9 (20 and 70 °C and 45 and 57.5 °C).

It can be concluded from these results that the prediction of desorption isotherm evolution with temperature is strongly sensitive to the isosteric heat of sorption. A reliable prediction thus requires an accurate description of the isosteric heat of sorption for the cementitious material in question. Generic equations such as the one proposed by Powers and Brownyard [1] or the two other evolutions derived in this study (from Poyet [4] and Hundt and

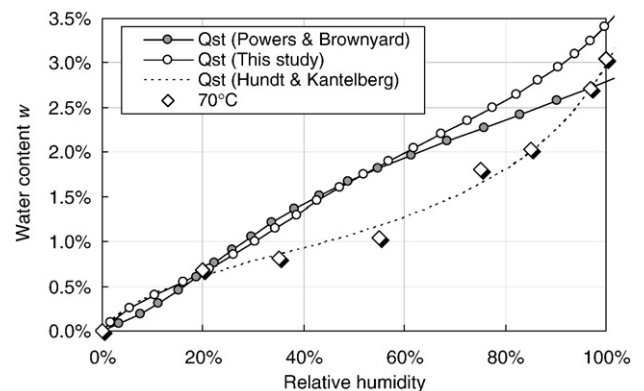


Fig. 13. Desorption isotherm at 70 °C of beton 5 estimated using the isosteric heat of sorption obtained in this study, proposed by Powers and Brownyard and derived from Hundt and Kantelberg.

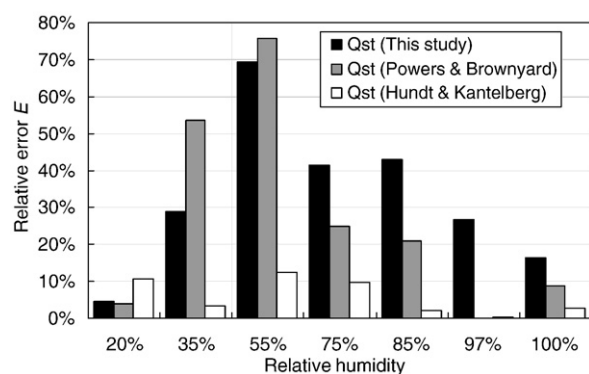


Fig. 14. Relative error between experimental water contents (at 70 °C for beton 5 [8]) and predicted values using three different isosteric heats of sorption.

Kantelberg [8]) can only be used to give a rough estimate of the impact of temperature on the desorption isotherm.

5. Conclusion

In the framework of radioactive waste management in France, concrete structures would be likely to undergo heating (up to 80 °C) and significant drying induced by the temperature increase. The durability assessment of such structures necessitates the knowledge of the evolution of the sorption isotherms versus temperature (in order to describe the induced water transfers).

This paper presents briefly the theoretical background needed to describe the impact of temperature on the sorption properties: the Clausius–Clapeyron equation and isosteric heat of sorption. The two of them allow describing the energy involved in the sorption process and then account for the impact of temperature on sorption isotherms. One can use CC to estimate the isosteric heat of sorption on the basis of the desorption isotherms obtained at only two different temperatures. One can then use the result obtained to compute the desorption isotherm at any other temperature. The consistency of the calculation depends on the quality of the experimental results used for the estimation of the isosteric heat.

The comparison between the evolutions of the isosteric heat of sorption obtained in this study (high-performance concrete) and previously published results shows a very similar pattern with values of the same order of magnitude. The three considered cementitious materials present the same general behaviour.

Nevertheless, the computation of the evolution of the desorption isotherm using CC proved to be very dependent on the isosteric heat of sorption: a reliable prediction of the sorption isotherms versus temperature requires the accurate knowledge of the isosteric heat of sorption for the material of interest. The use of a generic equation/evolution (such as the one proposed by Powers and Brownyard) can only be used to yield an estimate of the impact of temperature on the desorption isotherms.

Appendix A

Table 1
Formulation of the high-performance concrete used by Poyet [4].

Component	Nature	Origin	Quantity	Unit
Cement	CEM I 52.5	Lafarge Val d'Auzergues, France	400	kg/m ³
Sand	Calcareous [0–5]	Boulonnais quarry, France	858	kg/m ³
Gravel	Calcareous [5–12.5]	Boulonnais quarry, France	945	kg/m ³
Water	–	–	172	L/m ³
Superplasticizer	Glenium 27	BASF	10	kg/m ³

Table 2
Data for the fitting of the experimental results obtained at 30 °C and 80 °C [4].

Temperature (°C)	C	k	w _m (%)
30	4.690	0.592	2.534
80	6.010	0.897	0.480

Table 3
Data for the fitting of the experimental results obtained by Hundt and Kantelberg [8].

Temperature (°C)	C	k	w _m (%)
20	16.794	0.507	2.364
45	7.434	0.627	1.616
57.5	6.400	0.679	1.239
70	13.006	0.753	0.767

Table 4
Isosteric heat of desorption obtained in this study.

Water content w (%)	Coverage w/w _m	Q _{st} (w) [kJ/mol]
0.10	0.04	62.48
0.25	0.10	65.56
0.40	0.16	67.75
0.55	0.22	68.49
0.70	0.28	68.03
0.85	0.34	66.91
1.00	0.39	65.48
1.15	0.45	63.92
1.30	0.51	62.36
1.45	0.57	60.83
1.60	0.63	59.36
1.75	0.69	57.97
1.90	0.75	56.67
2.05	0.81	55.45
2.20	0.87	54.32
2.35	0.93	53.27
2.50	0.99	52.30
2.65	1.05	51.40
2.80	1.10	50.58
2.95	1.16	49.81
3.10	1.22	49.11
3.25	1.28	48.46
3.40	1.34	47.86
3.55	1.40	47.30
3.70	1.46	46.79
3.85	1.52	46.31
4.00	1.58	45.87
4.15	1.64	45.45
4.30	1.70	45.07
4.45	1.76	44.71
4.60	1.82	44.37

The coverage is equal to the ratio between the water content w and the monolayer capacity w_m obtained at 30 °C.

Table 5
Isosteric heat of desorption obtained for beton 5 on the basis of the results published by Hundt and Kantelberg [8].

w (%)	w/w _m	Isosteric heat of desorption Q _{st} (w) [kJ/mol]		
		20–70 °C	45–57.5 °C	All temperatures
0.08	0.03	60.04	66.54	62.64
0.19	0.08	61.66	67.36	63.99
0.30	0.13	63.49	68.16	65.48
0.45	0.19	66.18	69.10	67.66
0.61	0.26	68.86	69.79	69.79
0.76	0.32	70.89	70.06	71.37
0.91	0.38	71.82	69.80	72.04
1.06	0.45	71.69	68.94	71.82
1.21	0.51	70.80	67.54	70.93
1.36	0.58	69.41	65.75	69.57
1.51	0.64	67.71	63.75	67.90
1.67	0.70	65.82	61.69	66.04
1.82	0.77	63.84	59.70	64.07
1.97	0.83	61.84	57.86	62.07

Table 5 (continued)

w (%)	w/w _m	Isothermic heat of desorption Q _{st} (w) [kJ/mol]		
		20–70 °C	45–57.5 °C	All temperatures
2.12	0.90	59.88	56.18	60.09
2.27	0.96	58.01	54.67	58.21
2.42	1.02	56.27	53.33	56.44
2.57	1.09	54.67	52.14	54.82
2.72	1.15	53.23	51.09	53.36
2.88	1.22	51.94	50.15	52.06
3.03	1.28	50.79	49.32	50.89
3.08	1.31	50.39	49.02	50.49
3.14	1.33	50.01	48.75	50.10
3.20	1.35	49.64	48.48	49.73
3.26	1.38	49.29	48.22	49.37
3.31	1.40	48.95	47.98	49.03
3.37	1.43	48.63	47.74	48.71
3.43	1.45	48.33	47.51	48.40
3.48	1.47	48.03	47.29	48.10
3.54	1.50	47.75	47.08	47.82
3.60	1.52	47.48	46.88	47.54
4.01	1.70	45.83	45.62	45.88
4.54	1.92	44.27	44.39	44.31

The coverage is equal to the ratio between the water content w and the monolayer capacity w_m obtained at 20 °C. The reported temperatures correspond to the temperatures used for the estimation of the isosteric heat of sorption Q_{st} .

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