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► **To cite this version:**

Eric Simon, Fanny Jallu, Bertrand Perot, Stéphane Plumeri. Feasibility study of fissile mass quantification by photofission delayed gamma rays in radioactive waste packages using MCNPX. Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment, 2016, 840, pp.28-35. 10.1016/j.nima.2016.09.047 . cea-01992404

**HAL Id: cea-01992404**

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Submitted on 4 Dec 2019

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# 1 Feasibility study of fissile mass quantification by photofission 2 delayed gamma rays in radioactive waste packages using MCNPX

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8 **Keywords:** Photofission, Radioactive waste package, MCNPX, Uranium

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9 **Abstract:** The feasibility of fissile mass quantification in large, long-lived medium activity  
10 radioactive waste packages using photofission delayed gamma rays has been assessed with  
11 MCNPX. The detection limit achievable is lower than the expected uranium mass in these waste  
12 packages, but the important sensibility to the waste matrix density and sample localization  
13 imposes to get an accurate measurement of these parameters. An isotope discrimination method  
14 based on gamma-ray ratios has been evaluated showing that photofission delayed gamma rays  
15 can be used to measure the fissile mass as well as the total uranium mass.

16

17

## 18 1.Introduction

19 An important issue in the management of nuclear waste repository is the characterization of  
20 radioactive waste packages. Waste characteristics are to be compliant with specifications of the  
21 French National Radioactive Waste Management Agency (Andra) before disposal to ensure the  
22 waste repository safety. Many non-destructive methods have been studied on large waste  
23 packages to address this characterization. Among them, active interrogation methods have  
24 shown promising results to quantify the global mass of actinides or the fissile mass present in  
25 dense, potentially heterogeneous packages, either using incident neutrons or high energy  
26 photons. Depending on the type of waste packages, these methods are more or less efficient,  
27 being mainly sensitive to different parameters like hydrogen content of the matrix for neutrons  
28 or density and effective atomic number for photons.

29 Active neutron interrogation has been successfully applied onto medium sized waste (maximum  
30 220L) packages [1][2][3][4], but larger packages having a dense, hydrogenated matrix cannot be  
31 accurately examined by neutron interrogation followed by the detection of fission neutrons  
32 because of unacceptable uncertainties due to high and variable attenuation. For instance, the  
33 poor knowledge of hydrogen concentration in 1 m<sup>3</sup> concrete packages would introduce decades  
34 of uncertainties on the fissile mass when it is heterogeneously distributed in the waste. Previous  
35 methods [7] have been investigated using delayed neutron from photofission but suffer from  
36 similar drawbacks with outgoing neutron attenuation. The preferred method is then to use an  
37 incident high energy photon beam to produce photofission in actinides and to measure delayed  
38 gamma rays [5][6]. We present here a feasibility study of uranium quantification in 870L  
39 radioactive produced by CEA [8] waste packages having a hydrogenated matrix and  
40 heterogeneous waste, by detection of photofission delayed gamma rays. This study has been

1 performed using the Monte Carlo code MCNPX 2.7.0 [9]. The study was carried out by first  
 2 designing the examination geometry, and then by assessing the passive and active backgrounds  
 3 in view to determine the detection limits of uranium mass for the main delayed gamma rays of  
 4 interest.

5 The simulated measurements are performed with high resolution HPGe gamma detector in view  
 6 to analyze the different delayed gamma rays following photofission of  $^{235}\text{U}$  and  $^{238}\text{U}$  isotopes.  
 7 Due to GDR (Giant Dipolar Resonance) photofission cross section behavior, both actinides of odd  
 8 and even mass numbers may be subject to photofission. Uranium content is first investigated  
 9 thanks to its known nuclear photofission data [10]. The other key element in the waste  
 10 packages, plutonium, still lacks reliable nuclear photofission data and could be assessed in the  
 11 same way once these data are completed. The effects of waste density and sample localization in  
 12 the 870L waste package are also characterized.

13 In order to get a discrimination signal from the  $^{238}\text{U}/^{235}\text{U}$  isotopes, the ratios of photofission  
 14 gamma rays with close energies are used so as to eliminate the dependence of attenuation as a  
 15 function of energy.

## 16 2. Design of the system using numerical simulations

17 One of the key issue in photofission examination is related to interfering neutron fission by  
 18 neutrons produced outside or inside the fissile sample [13]. Tungsten is commonly used as  
 19 Bremsstrahlung breaking target but it is also a strong photoneutron emitter. Therefore, a new  
 20 converter has been designed in order to minimize the emission of external photoneutrons  
 21 impinging the waste package together with the Bremsstrahlung beam. Comparing the  
 22 Bremsstrahlung yield above the photofission threshold, which is in general around 5 MeV [14],  
 23 and the photoneutron emission of potential targets by MCNPX calculations, a silicon thick target  
 24 has been selected. Tables 1 and 2 summarize the main characteristics of possible  
 25 Bremsstrahlung converters. Photoneutron yields and photofission cross sections are computed  
 26 for the whole Bremsstrahlung spectrum.

**Table 1**

Bremsstrahlung yield and integrated uranium photofission cross section in different evaluated Bremsstrahlung converters.

	Target thickness (mm)	Bremsstrahlung yield above 5 MeV (photon per e <sup>-</sup> )	Photon flux at 1 m (0°), full energy range (cm <sup>-2</sup> per e <sup>-</sup> )	Photoneutron yield at 1 m (cm <sup>-2</sup> per e <sup>-</sup> )	<sup>238</sup> U photofission cross section (mb)	<sup>235</sup> U photofission cross section (mb)
<b>W (15 MeV)</b>	2.1	2.04 10 <sup>-1</sup>	6.66 10 <sup>-5</sup>	7.66 10 <sup>-10</sup>	6.42	14.8
<b>Cu (12 MeV)</b>	4.7	6.02 10 <sup>-2</sup>	2.81 10 <sup>-5</sup>	2.06 10 <sup>-12</sup>	1.94	3.77
<b>Mo (12 MeV)</b>	4.0	7.78 10 <sup>-2</sup>	2.98 10 <sup>-5</sup>	3.48 10 <sup>-11</sup>	2.16	4.21
<b>Cr (12 MeV)</b>	5.9	5.19 10 <sup>-2</sup>	2.89 10 <sup>-5</sup>	2.94 10 <sup>-13</sup>	1.85	3.58
<b>Si (12 MeV)</b>	17.1	3.93 10 <sup>-2</sup>	2.55 10 <sup>-5</sup>	2.28 10 <sup>-15</sup>	1.63	3.13
<b>Si (15 MeV)</b>	17.1	7.02 10 <sup>-2</sup>	9.01 10 <sup>-5</sup>	1.24 10 <sup>-13</sup>	4.24	9.64

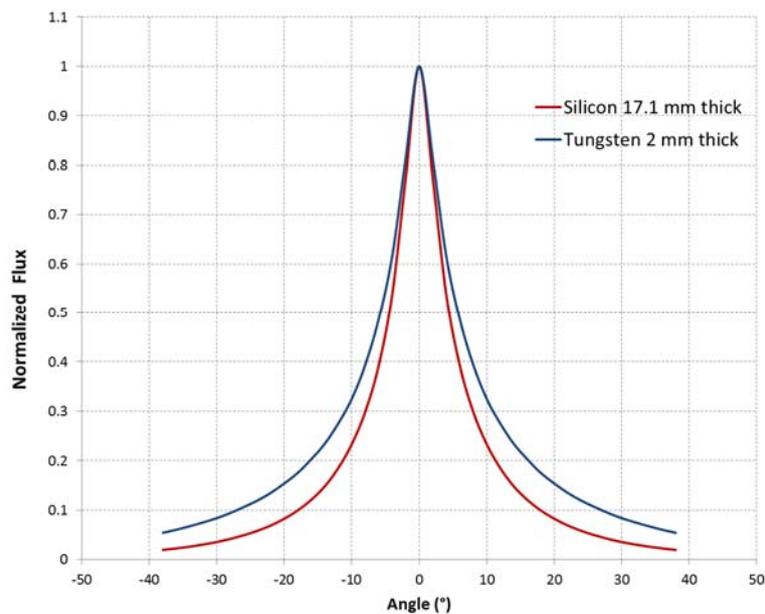
**Table 2**

Photonuclear characteristics of Bremsstrahlung target materials. [14]

Target material	$(\gamma,n)$ cross section (mb)			Activation products	Half life
	12 MeV	13 MeV	15 MeV		
<b>W</b>	300	420	420	<sup>181</sup> W	121.2 d
				<sup>185</sup> W	75.1 d
				<sup>185m</sup> W	1.6 min
<b>Cu</b>	12	20	50	<sup>62</sup> Cu	9.6 min
				<sup>64</sup> Cu	12.7 h
<b>Mo</b>	~20	~50	150	<sup>99</sup> Mo	2.75 d
				<sup>91</sup> Mo	15.49 min
<b>Cr</b>	0.5	1	20	<sup>51</sup> Cr	27 d
				<sup>49</sup> Cr	42.3 min
<b>Si</b>	0.05	0.05	0.07	-	-

1

2 Despite a lower Bremsstrahlung yield, a 17 mm thick silicon target produces a superior total  
3 photon flux in the forward direction compared to a 2 mm thick tungsten target (the Si/W photon  
4 flux ratio is 1.14). On the other hand, the X-ray flux intensity from the silicon converter is  
5 decreasing more rapidly at wider angles from the beam centerline (Fig. 1).



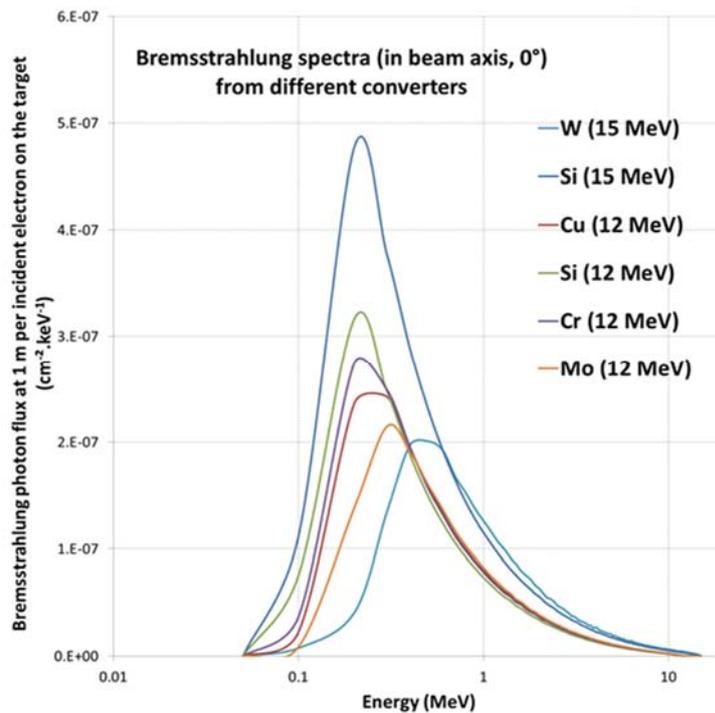
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**Fig. 1.** Bremsstrahlung beam anisotropy from the silicon 17.1 mm thick target and tungsten 2 mm thick target above 5 MeV (MCNPX calculations).

9 The photoneutron production of silicon at 15 MeV is greatly reduced compared to other evaluated  
10 target materials. Another benefit of using silicon is the absence of neutron activation.  
11 Figure 2 presents the computed Bremsstrahlung spectra from different converters on the beam axis  
12 (0°) and for incident electron energies of 12 MeV and 15 MeV.



1  
2 **Fig. 2.** Bremsstrahlung photon spectra from different converter at 12 MeV or 15 MeV (MCNPX simulations).

3 The nuclear waste package under investigation is the so called CEA “870L” package [8]. The average  
4 uranium content of this package is around 700 g of <sup>238</sup>U and 30 g of <sup>235</sup>U.

5 The 870L model used in these evaluations contains 5 compacted primary waste, surrounded by an  
6 hydraulic cement matrix and enclosed in a 3 mm thick steel container (Fig. 3). The primary waste  
7 matrix is considered heterogeneous, containing both metallic and organic materials. The modelled  
8 elemental compositions of the waste and hydraulic binder are shown in tables 3 and 4. The effects  
9 related to the location of the uranium sample inside the waste package are evaluated by modelling  
10 a penalizing location, i.e. centered in the package, and a more favorable one, in the periphery.

11 **Table 3**  
12 Waste matrix elemental composition

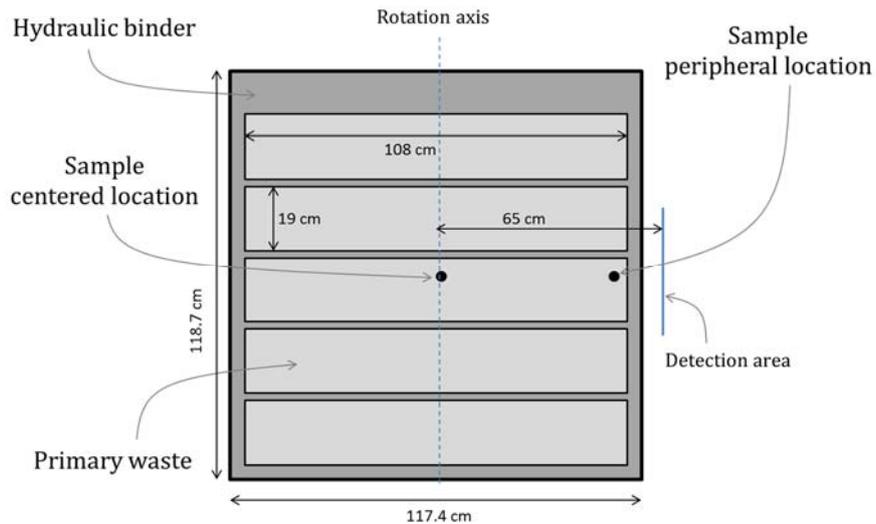
element	% weight
Fe	30
C	15
O	15
Si	15
N	5
H	5
Al	15

13  
14 **Table 4**  
15 Hydraulic binder elemental composition

element	% weight	element	% weight
Si	30.52	P	3 10 <sup>-2</sup>

Al	2.19	O	52.96
Fe	$9.1 \cdot 10^{-1}$	S	$3.78 \cdot 10^{-1}$
Ca	9.8	Cl	$6.4 \cdot 10^{-3}$
Mg	$4.7 \cdot 10^{-1}$	Mn	$2 \cdot 10^{-2}$
Na	$7 \cdot 10^{-2}$	N	$3 \cdot 10^{-5}$
K	$8.3 \cdot 10^{-1}$	H	1.33
Ti	$1.1 \cdot 10^{-1}$		

1



2

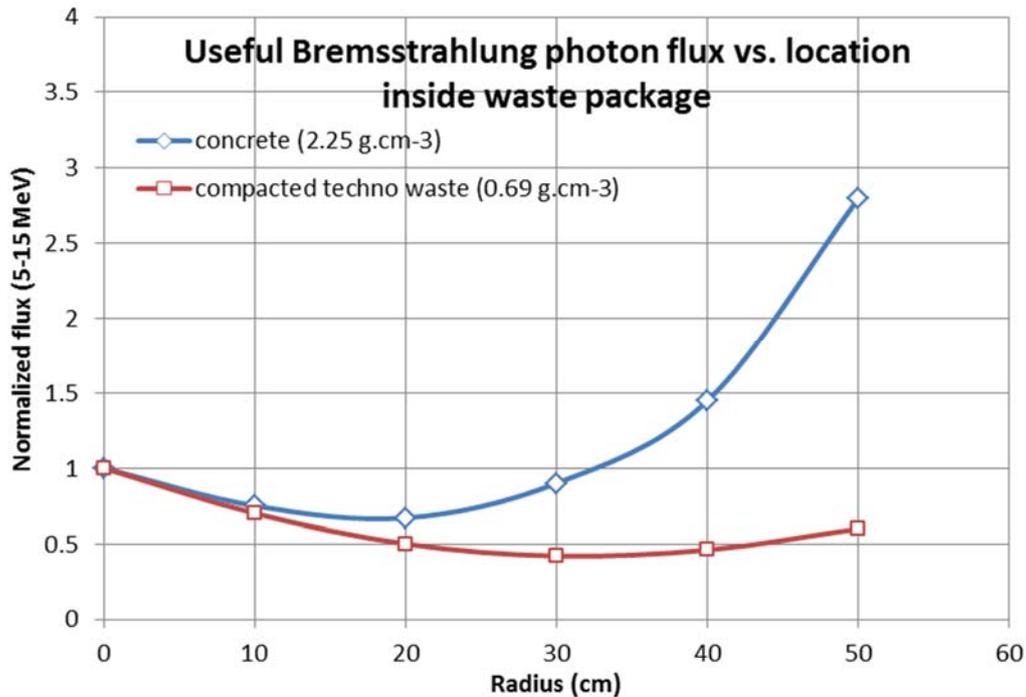
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4

**Fig. 3.** Geometry of the modelled 870 L package.

5 In order to maximize the incident Bremsstrahlung flux in the waste package, the Bremsstrahlung  
6 target is located 1 meter away from the center of a package. Because of the anisotropic nature of the  
7 photon beam (Fig. 1), a rotation of the package is required to perform a homogenous irradiation.

8 In order to keep the photoneutron background as low as possible, no lead or tungsten collimator is  
9 used to angularly sharpen the Bremsstrahlung beam. With this configuration, the flux received by a  
10 sample inside the package varies as a function of its distance from the center radius. This X-ray flux  
11 modulation is also dependent upon the nature and density of the waste matrix. Figure 4 presents  
12 the evolution of the Bremsstrahlung flux between 5 MeV and 15 MeV (which is the useful range for  
13 photofission) for samples located at different radii inside the package filled with two kinds of  
14 matrix materials. The values are integrated over a  $360^\circ$  rotation. The effect of sample localization  
15 increases with the material density ( $2.25$  vs.  $0.69 \text{ g}\cdot\text{cm}^{-3}$ ).



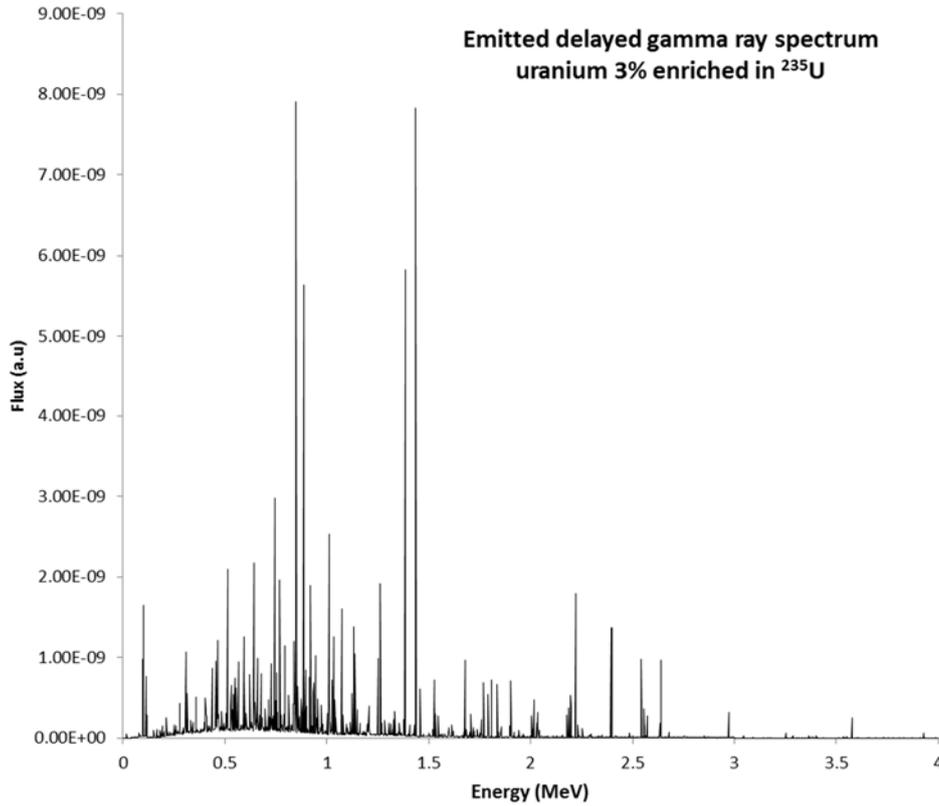
**Fig. 4.** Integral X-ray flux (5 MeV – 15 MeV) as a function of the radial location of the uranium sample inside the package. Here the package of Fig. 2 is considered to be fully filled, either by the cement binder or by the waste matrix.

Irradiation is simulated using pulse time characteristics achievable with a standard LINAC: 4.5  $\mu$ s pulses are repeated with a 200 Hz frequency during 2 hours, and delayed gamma rays are counted after 60 seconds cooling time; the 4 hour post-irradiation gamma-ray spectrum is segmented in 60 min sub-spectra in order to optimize detection limits of the different delayed gamma rays.

The Bremsstrahlung incident beam is produced by impinging 15 MeV electrons in pulsed mode for 2 hours with a current generating a 20 Gy/min dose rate at 1 m in the electron beam direction. The existence of asymmetric geometrical configurations in real waste packages leads to take into account their rotation during examination to reduce localization effects. Instead of multiplying time consuming simulations, the rotation of the waste package is simulated by placing multiple Bremsstrahlung photon sources around the cylindrical waste package.

The delayed gamma-ray production is computed using the ACT FISSIION card of MCNPX 2.7.0 and ENDF/BVII photonuclear libraries (Fig.5). Although CPU time when using this feature of MCNPX can become huge, the DG=LINES option (which allows to obtain the delayed gamma-ray lines instead of energy groups) has been selected in order to get the spectral data. One of the main purposes of our photofission based examination is indeed to demonstrate the capability to discriminate between uranium fissile ( $^{235}\text{U}$ ) and fertile ( $^{238}\text{U}$ ) isotopes to quantify the fissile mass.

The use of delayed gamma-ray emission for discriminating the isotopic composition of a waste package content has been previously investigated mainly in two ways. The first method is based upon a spectrometric analysis and the computation of specific gamma-ray ratios. The gamma rays are selected to have close energies, and thus having similar attenuation during their transport towards the detector [11][12]. This method using peak ratios could then be rather independent of matrix and sample location heterogeneities. The gamma lines of interest are summarized in table 5. A second method is based on the measurement of the differential decay time constants of the integral count rate of high energy delayed gamma rays (typically above 3 MeV) emitted after irradiation.



2

3 **Fig. 5.** Emitted photofission delayed gamma-ray spectrum from uranium (3% mass fraction of <sup>235</sup>U, 97% of <sup>238</sup>U)  
4 produced with MCNPX ACT FISSION card.

5

6

**Table 5**

Gamma-ray lines of interest from photofission products [5].

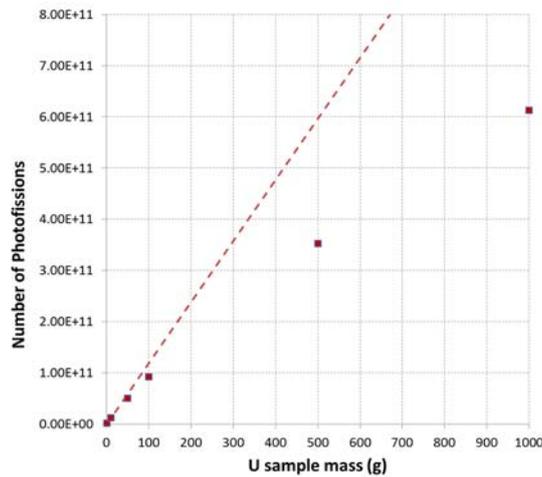
Energy (keV)	Fission product	Half-life
1384	<sup>92</sup> Sr	2.61 h
1436	<sup>138</sup> Cs	33.4 m
1768	<sup>138</sup> Xe	14.1 m
1791	<sup>135</sup> I	6.57 h
1806	<sup>134</sup> I	52.6 m
2016	<sup>138</sup> Xe	14.1 m
2032	<sup>101</sup> Mo	14.6 m
2176	<sup>95</sup> Y	10.5 m
2196	<sup>89</sup> Rb	15.32 m
2218	<sup>138</sup> Cs	32.2 m
2392	<sup>88</sup> Kr	2.82 h
2398	<sup>142</sup> La	1.32 h

7 The only detector able to separate the lines of Tab. 5 is high purity germanium (HPGe). In order to  
8 be used in a photofission system with a high flux of photoneutrons, it has to be radiation hardened  
9 (N type HPGe crystal). In addition, it must have good detection efficiency for gamma rays above 1  
10 MeV. A multiple detector system comprising five HPGe detectors (45% efficiency) with a 2 keV  
11 resolution at 1332 keV has been considered. The detector cluster is intended to be protected from  
12 scattered photons, photoneutrons and prompt fission and photofission neutrons by a dedicated  
13 shielding wall during the irradiation phase. At the end of irradiation, the detector cluster will be  
14 moved to its measurement location near the waste package. The distance taken into account

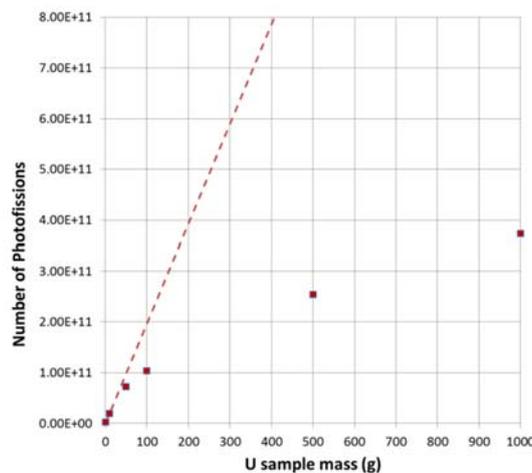
1 between the detectors entrance window and the package axis is 65 cm (i.e. around 15 cm from its  
2 wall).

### 3. Signal and background calculations

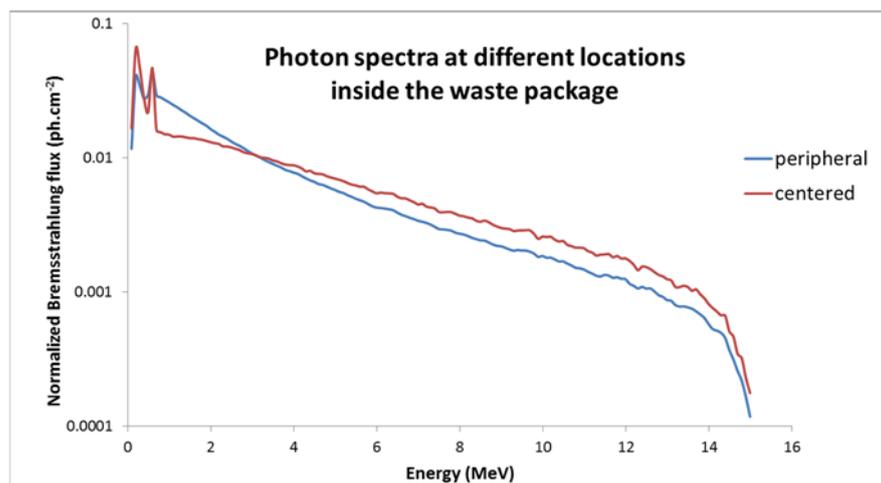
4 The number of photofission reactions has been calculated as a function of the mass of an uranium  
5 sample enriched at 20% in  $^{235}\text{U}$  from 1 g up to 1000 g, and for two different sample locations  
6 (centered and peripheral). The photofission rate follows a non-linear evolution as a function of the  
7 sample mass, due to self-shielding of incident interrogating photons (Fig. 6 and 7). This non-  
8 linearity is less pronounced in the central location due to the hardening of the incident X-ray beam  
9 reaching the sample. Fig. 8 shows the spectrum shape computed by MCNPX at the two sample  
10 locations within the package (peripheral and centered), showing the differential attenuation (beam  
11 hardening). In the linear range region of Fig. 6 and 7 (low uranium masses), the photofission rate  
12 sensitivity is  $1.65 \cdot 10^5 \text{ s}^{-1}\cdot\text{g}^{-1}$  with the centered sample and  $2.72 \cdot 10^5 \text{ s}^{-1}\cdot\text{g}^{-1}$  in peripheral location. The  
13 difference is small compared to other techniques such as neutron interrogation, for which the  
14 signal would be reduced by more than a decade between the outer and center positions, because of  
15 the high absorption of thermal interrogating neutrons by hydrogen nuclei. Indeed, thermal neutron  
16 interrogation is highly sensitive to any absorbing elements that might be present in the waste  
17 matrix, such as hydrogen, boron, chlorine, cadmium, etc.



18  
19 **Fig. 6.** Number of photofissions induced in the 20% enriched uranium sample in centered location inside 870L waste  
20 package, after 2 h irradiation.



21  
22 **Fig. 7.** Number of photofissions induced in the 20% enriched uranium sample in peripheral location inside 870L waste  
23 package, after 2h irradiation.



**Fig. 8** : Spectrum hardening between peripheral and centered locations within the waste package. Low energy events visible in both spectra are annihilation and Compton scattering photons from beam interactions.

1  
2  
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4  
5 The main source of parasitic fission signal in photofission examination is due to either external  
6 photoneutrons or to neutrons produced in the sample itself (photoneutrons or prompt fission  
7 neutrons produced in uranium). Their impact on the total fission signal has been evaluated by  
8 computing the neutron flux arriving at the surface of the uranium sample, with and without  
9 uranium in the model, and by convoluting these fluxes with the neutron fission cross section (using  
10 the MCNPX tally multiplier card). The obtained fission rates have then been compared to the total  
11 (mainly photo-) fission rate. Table 6 summarizes the evaluation of these spurious neutron fission  
12 events in the two geometrical sample configurations.

13 The spurious neutron fissions produced by external neutrons, mainly coming from interactions of  
14 the X-ray beam with the package, only represents less than 0.2% of the total fissions. The origin of  
15 the external neutrons has been estimated by modifying some elements of geometry (calculations of  
16 the neutron flux inside package with or without the uranium sample), showing that a proportion  
17 (around 1%) comes from the silicon target, most of the photoneutrons being produced within the  
18 package before reaching the center of the matrix.

19 On the other hand, fissions due to neutrons produced inside uranium are more numerous (up to  
20 17% for the 500 g sample in the periphery). Nevertheless, they will not lead to an excessive  
21 overestimation of the uranium mass measured by photofission.

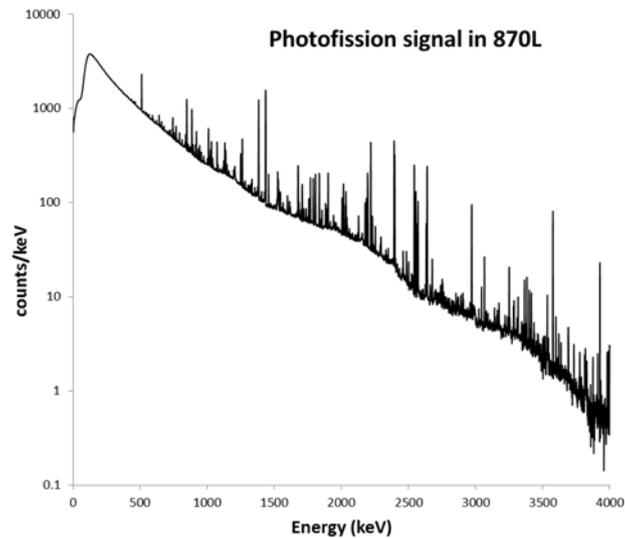
**Table 6**

22  
23 Proportion of parasitic neutron fissions with respect to total (mainly photo-)  
24 fissions, as a function of sample mass (20% enriched uranium).  
25

		<b>10 g</b>	<b>100g</b>	<b>500g</b>
Centered location	Fissions from external neutrons	0.08%	0.14%	0.16%
	Fissions from sample neutrons	1.42%	5.90%	1.32%
	Total	1.53%	6.04%	10.48%
Peripheral location	Fissions from external neutrons	0.03%	0.09%	0.14%
	Fissions from sample neutrons	4.47%	9.34%	16.74%
	Total	4.50%	9.43%	16.88%

26

1 The useful photofission signal is computed from the photofission rate calculated above and from  
2 the ACT fission card. The time dependence of the delayed gamma-ray emission is computed by  
3 segmenting with a time card the outgoing gamma-ray flux with a F4 tally. Then the pulse height  
4 spectrum (F8 tally) in the HPGe detector corresponding to the different time windows is calculated  
5 by considering a normal photon incidence on the detector entrance window (Fig. 9). The total count  
6 rate due to photofission events is low ( $134 \text{ counts}\cdot\text{s}^{-1}$  in the configuration of Fig. 3).

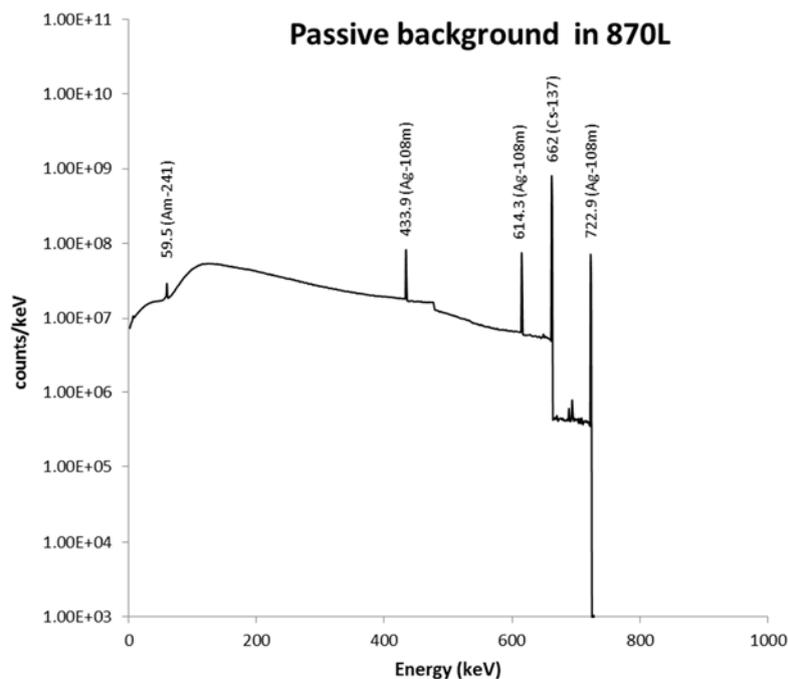


7

8 **Fig. 9.** Photofission signal spectrum of the 870L package (2 h irradiation, 3 h counting).

9 The passive gamma background of the 870L package has been evaluated by modelling the average  
10 gamma emission of the main isotopes.

11 The gamma-ray source is considered homogeneously distributed in the volume of the primary  
12 compacted waste inside the 870L package. The simulated source includes 6 isotopes representing  
13 the essential of the gamma emission of the 870L waste package. Fig. 10 shows the passive  
14 background spectrum computed for 3 h counting in a 45% relative efficiency germanium detector  
15 located at 65 cm away from the package axis.



16

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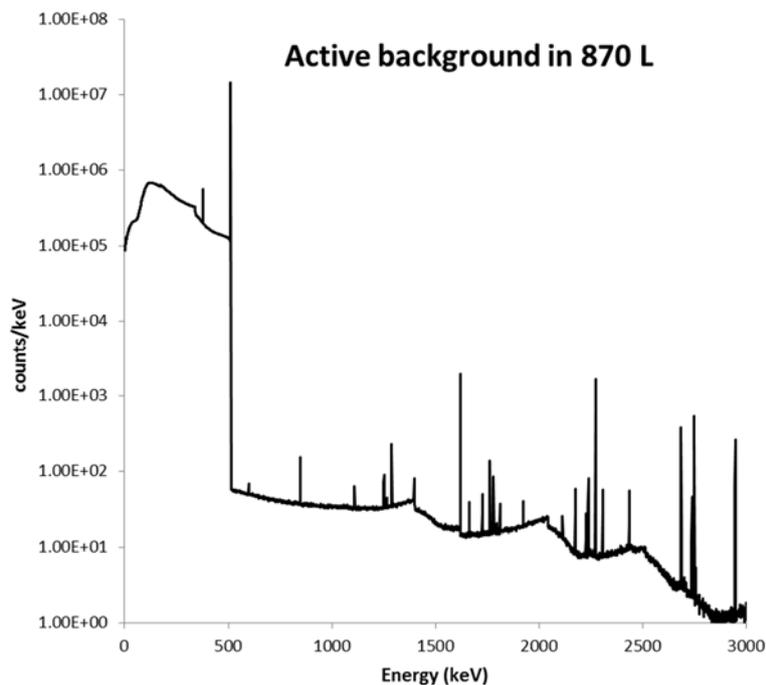
**Fig. 10.** Passive background spectrum of the 870L package (3 h counting).

1 The count rate is very large, around  $1.5 \cdot 10^6$  counts.s<sup>-1</sup>, but the passive gamma background is  
2 entirely below 1 MeV, dominated by the 662 keV line of <sup>137</sup>Cs. The acquisition electronics should be  
3 carefully optimized in order to not disturb the high energy part of the spectrum by pulse pile-up  
4 effects (the delayed gamma rays of interest shown in further Table 8 are above 1.3 MeV).

5 In order to reduce the passive background, a detector collimation could be used, in particular when  
6 the uranium sample has been previously localized (by transmission imaging or photofission  
7 tomography as discussed in the conclusion).

8 On the other hand, the detection of photofission delayed gamma rays might be perturbed by the  
9 delayed gamma emission of nonnuclear materials activated during the irradiation phase. This  
10 active background is mainly composed of isotopes produced by neutron and photonuclear  
11 activation. To quantify this active background, the calculation is performed in several steps. First,  
12 the rates of all reactions of interest are computed using MCNPX in the cement binder and in the  
13 compacted waste separately. Then, the activity of background isotopes is calculated during the  
14 counting period of photofission delayed gamma rays. Finally, active background gamma-ray spectra  
15 are computed using the MCNPX pulse height tally in the detector. The considered activation  
16 reactions considered are: ( $\gamma,n$ ), ( $\gamma,p$ ), ( $n,p$ ), ( $n,2n$ ), ( $n,\alpha$ ), ( $n,\gamma$ ). More than 40 isotopes are taken into  
17 account for this evaluation.

18 The activation of the package is dominated by <sup>13</sup>N (half-life 9.96 min), <sup>11</sup>C (half-life 20.33 min), and  
19 <sup>15</sup>O (half-life 122 s). These  $\beta^+$  emitters indeed lead to an intense 511 keV annihilation line (Fig. 11).  
20 The total count rate of the active background is  $1.8 \cdot 10^4$  counts.s<sup>-1</sup>, which is two orders of magnitude  
21 lower than passive background. However, many gamma lines are present in the useful area of the  
22 spectrum between 1.3 MeV and 3 MeV.



23  
24 **Fig. 11.** Active background spectrum of the 870L package (2 h irradiation, 3 h counting).  
25

26 The gamma lines of the active background responsible of the Compton continuum present in the  
27 useful area of the spectrum are detailed in Table 7. The single escape line of 2686 keV gamma ray  
28 (<sup>53</sup>Fe) at 2175 keV interferes with the 2176 keV delayed photofission gamma ray (see Tab. 8). The  
29 subtraction of the 2686 keV single escape line (SE) should however be possible thanks to the 2686  
30 keV full-energy line and the associated double escape line (DE) at 1664 keV, knowing the HPGe  
31 detector respective efficiencies of the 3 peaks by MCNPX simulations.

1  
2

**Table 7**  
Gamma ray lines present in the useful area of the spectrum.

Line (keV)	Origin	Line (keV)	Origin
1397	<sup>53</sup> Fe	2238	SE from 2749 keV
1620	<sup>53</sup> Fe	2274	<sup>53</sup> Fe
1664	DE from 2686 keV	2308	<sup>53</sup> Fe
1727	DE from 2749 keV	2436	SE from 2947 keV
1763	SE from 2274 keV	2523	<sup>56</sup> Mn
1779	<sup>28</sup> Al	2686	<sup>53</sup> Fe
1797	SE from 2308 keV	2738	SE from 3249 keV
1811	<sup>56</sup> Mn	2749	<sup>53</sup> Fe
1925	DE from de 2947 keV	2754	<sup>24</sup> Na
2113	<sup>56</sup> Mn	2947	<sup>53</sup> Fe
<b>2175</b>	<b>SE from 2686 keV</b>	2960	<sup>56</sup> Mn
2227	DE from 3249 keV		

3

4 **4. Detection limits and spectroscopy of delayed gamma rays**

5 The mass detection limit is computed for each of the 12 photofission delayed gamma-ray lines of  
6 interest from the useful signal S (counts in the net area per uranium mass unit) and background B  
7 (counts in the area of interest for both the passive and the active backgrounds), for 2 hour  
8 irradiation and 3 h counting times, using eq.(1) [15] :

9 
$$LD (g) = \frac{2.71+3.29\sqrt{B\left(1+\frac{n}{2m}\right)}}{S} \quad (\text{eq. 1})$$

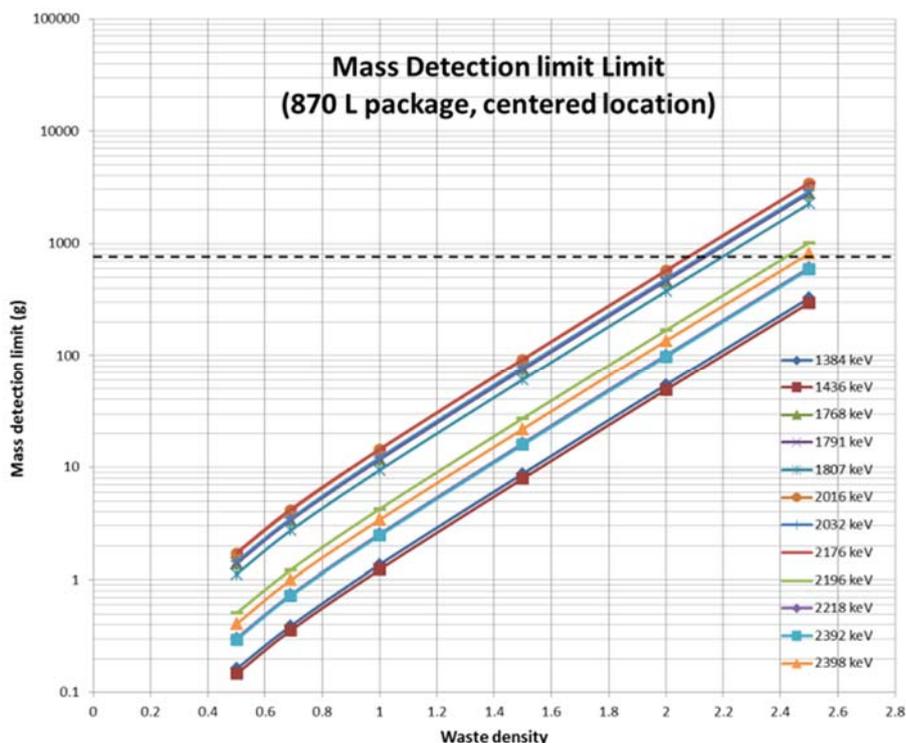
10 where n is the number of bins in the peak, and m is the number of bins used to compute the  
11 background on both sides of the peaks.

12 The mass detection limit for each line of interest is given in table 8.

13 **Table 8**  
14 Detection limit for the 12 lines of interest

Line (keV)	L <sub>D</sub> (counts)	L <sub>D</sub> (g)	
		centered	peripheral
1384	75	0.31	0.022
1436	115	0.36	0.026
1768	86	3.43	0.264
1791	86	3.43	0.291
1807	83	2.78	0.240
2016	105	4.18	0.42
2032	107	3.56	0.497
2176	63	4.22	0.434
2196	61	1.22	0.117
2218	63	0.74	0.071
2392	65	0.72	0.022
2398	65	1.00	0.026

1  
 2 Figure 12 shows the evolution of the mass detection limit obtained for each line of interest as a  
 3 function of the waste density. The mass detection limit increases rapidly when the waste density  
 4 increases from 0.5 to 2.5. In this density range, the mass detection limit drops by a factor of around  
 5 3 decades. Despite this strong evolution which highlights the necessity to measure the waste  
 6 density (for instance by photon tomodensitometry with the same LINAC), all lines of interest  
 7 exhibit a detection limit lower than the expected average uranium mass content in the package  
 8 (~750 g) up to a waste density of 2.0, and for 6 lines up to a density of 2.5.



9  
 10 **Fig. 12.** Uranium detection limits of the photofission delayed gamma rays of interest (2 h irradiation, 3 h counting), for a  
 11 sample in the center of the 870L package. The average uranium mass content of the package is figured by the horizontal  
 12 dashed line.

13 Seven delayed gamma peak ratios have been calculated as a function of uranium enrichment in  
 14 view to test the feasibility of  $^{235}\text{U}$  vs.  $^{238}\text{U}$  discrimination. These ratios have been evaluated with the  
 15 12 above lines of interest for two sample locations, centered and peripheral, as reported in tables 9  
 16 and 10, respectively. The ratios are remarkably similar from one sample location to the other.

17 **Table 9**

18 Peak ratios computed for a centered 100 g sample, from pure  $^{238}\text{U}$  to 25% enriched uranium.

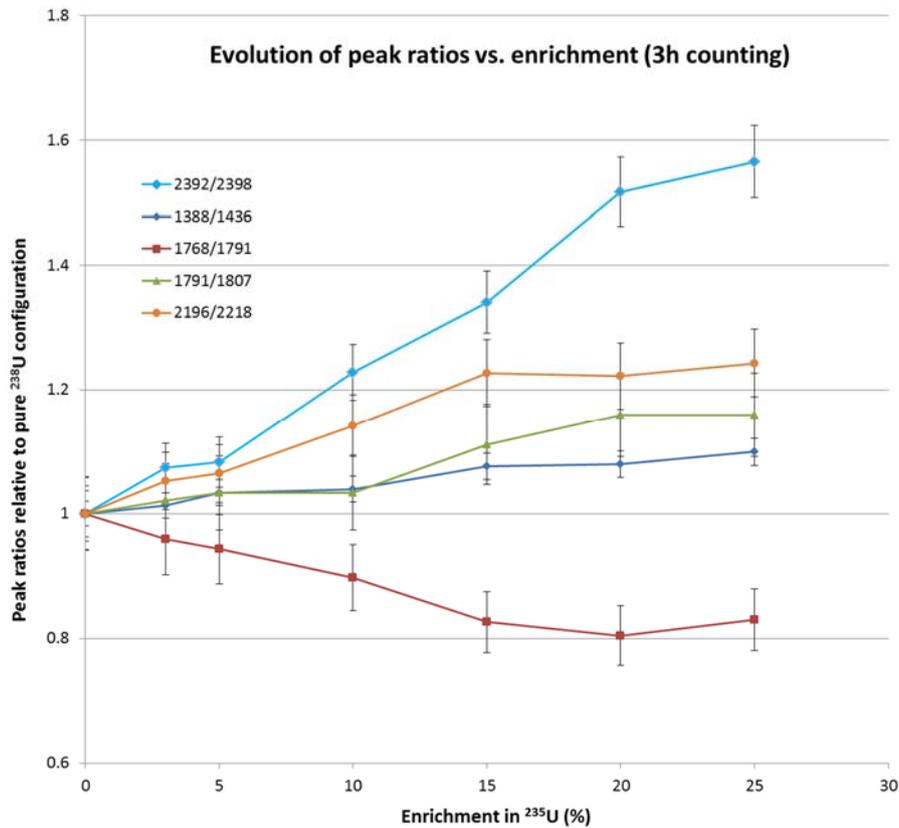
Peak ratio	Uranium-235 enrichment (%)						
	0	3	5	10	15	20	25
1384 / 1436	0.623	0.630	0.644	0.646	0.669	0.672	0.684
1768 / 1791	1.290	1.224	1.216	1.159	1.054	1.026	1.007
1791 / 1807	0.733	0.745	0.743	0.760	0.823	0.854	0.856
2016 / 2032	0.806	0.816	0.798	0.815	0.801	0.807	0.774
2176 / 2196	0.314	0.307	0.308	0.301	0.267	0.279	0.291
2196 / 2218	0.481	0.505	0.514	0.550	0.593	0.589	0.599

2392 / 2398      0.927      0.994      1.003      1.129      1.235      1.398      1.443

1 **Table 10**  
 2 Peak ratios computed for a peripheral 100 g sample, from pure U-238 to 25% enriched uranium.

Peak ratio	Uranium-235 enrichment (%)						
	0	3	5	10	15	20	25
1384 / 1436	0.644	0.652	0.666	0.668	0.693	0.694	0.707
1768 / 1791	1.309	1.279	1.262	1.184	1.087	1.048	1.038
1791 / 1807	0.737	0.742	0.740	0.757	0.816	0.850	0.858
2016 / 2032	0.831	0.841	0.833	0.855	0.833	0.833	0.810
2176 / 2196	0.324	0.315	0.315	0.304	0.272	0.283	0.296
2196 / 2218	0.480	0.505	0.511	0.550	0.590	0.589	0.601
2392 / 2398	0.923	0.990	0.999	1.129	1.236	1.404	1.447

3  
 4 Among the seven evaluated ratios, the 1768 keV/1791keV and 2392 keV/2398 keV ones show  
 5 respectively 20.7% and 56.8% variation between 0% and 25% enrichment of <sup>235</sup>U, which is a priori  
 6 a sufficient contrast to estimate the uranium enrichment (Fig. 13).



7  
 8 **Fig. 13.** Peak ratios as a function of uranium enrichment.

9 **4. Discussion and conclusion**

10 A non-destructive examination system of a 870L nuclear waste package based on the detection of  
 11 photofission delayed gamma rays has been assessed with MCNPX calculations. The envisaged set-  
 12 up involving a 15 MeV Linac Bremsstrahlung beam and a cluster of 5 HPGe detectors would be a  
 13 priori sufficient to measure the fissile mass through a spectroscopic analysis of photofission  
 14 delayed gamma rays.

1 The achievable detection limits of the delayed gamma rays of interest are lower than the average  
2 uranium mass (~750 g) in the waste package, even for a wide range of waste densities and sample  
3 localizations. However, these two parameters have a high impact on measurement sensitivity. This  
4 expected behavior indicates the necessity to accurately assess both the localization of uranium and  
5 the density of the waste in order to precisely quantify uranium (total or fissile mass). This  
6 additional information could be supplied in two ways. First by implementing high energy photon  
7 tomo-densitometry [16][17][18], with the same Bremsstrahlung beam but specific imaging  
8 detectors. Second, by using photofission emission tomography [19][20], either with delayed  
9 neutrons or gamma rays.

10 The high gamma-ray background encountered with in this kind of detectors close to the 870 L  
11 irradiant package is also of concern. Even if the useful photofission signal is free from direct  
12 interferences with gamma rays from the package emitted at lower energy, the high count-rate  
13 should be taken into account to limit saturation and pulse pile-up effects, which could significantly  
14 impair the detection capability of photofission delayed gamma rays. A detector collimation could be  
15 envisaged for this purpose, leading to the examination of a restricted area in the waste package.

16 On the other hand, in order to estimate the fissile mass in nuclear waste packages, plutonium must  
17 be measured along with uranium. The feasibility of its quantification using delayed gamma rays  
18 from photofission is the next step to address. In this view, nuclear data regarding delayed gamma  
19 rays from photofission of plutonium isotopes will be evaluated by computational means. The  
20 plutonium mass in the waste packages is generally much lower than the uranium mass, but the  
21 fraction of fissile isotopes ( $^{239}\text{Pu}$ ,  $^{241}\text{Pu}$ ) is larger. Finally, mixed uranium and plutonium samples  
22 will be studied, first numerically and then experimentally.

23 The encouraging results obtained for uranium photofission delayed gamma rays in the 870L  
24 package pave the way to examinations of other types of dense, hydrogenous, and heterogeneous  
25 waste packages whose fissile mass cannot be accurately quantified by neutron-based active  
26 interrogation.

## 27 **Acknowledgement**

28 This work is supported by the French National Radioactive Waste Management Agency (Andra)  
29 under the CHK contract in the field of nuclear waste management.

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