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On the impact of beamforming strategy on mm-wave localization performance limits

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keeping the architecture complexity lower. In fact, as shown in [16]–[18], where transmitarrays (i.e., a particular type of phased arrays consisting of a focal source illuminating a planar array) have been proposed, PSs are usually realized using switches. Therefore, as it is often unfeasible to obtain a continuous phase value ranging from 0° to 360° with real antennas, the resulting quantization errors should be taken into account in the analysis. Thus, this paper proposes a CRLB-based investigation on how a proper choice of the beamforming strategy can lead to different levels of localization accuracy and of array complexity.

The rest of the paper is organized as follows. In Sec. II we describe the considered array configurations, whereas in Sec. III we discussed an ad-hoc signal model for the analyzed multi-antennas schemes. Sec. IV shows the PEB derivation, where results are given in Sec. V. Final conclusions are successively drawn in Sec. VI.

II. ANTENNA ARRAY GEOMETRIC CONFIGURATION

We consider a 3D localization scenario consisting of a N_{rx} -sized receiving array located in known position (i.e., $\mathbf{p}^r = [x_0^r, y_0^r, z_0^r]^T = [0, 0, 0]^T$) and a transmitting array with N_{tx} antennas whose position, $\mathbf{p}^t = [x_0^t, y_0^t, z_0^t]^T = [x, y, z]^T$, is to be inferred by the estimation process. We indicate with $\boldsymbol{\theta} = [\theta, \phi]^T$ the direction-of-arrival (DOA), i.e., the angle formed between the two arrays geometric centers. Moreover, if classical beamforming is considered, the steering angles will be indicated with $\boldsymbol{\theta}_0 = [\theta_0, \phi_0]^T$.

In both arrays, the antennas coordinates with respect to the array centroid can be expressed as

$$\mathbf{p}_{i/m}^{t/r}(\boldsymbol{\vartheta}^{t/r}) = \begin{bmatrix} x_{i/m}^{t/r} \\ y_{i/m}^{t/r} \\ z_{i/m}^{t/r} \end{bmatrix}^T = \rho_{i/m}^{t/r} \mathbf{R}(\boldsymbol{\vartheta}^{t/r}) \mathbf{d}^T(\boldsymbol{\theta}_{i/m}^{t/r}) \quad (1)$$

with $i = 1, 2, \dots, N_{\text{tx}}$, $m = 1, 2, \dots, N_{\text{rx}}$ being the 1D transmitter (TX)/receiver (RX) antenna index, $\mathbf{R}(\boldsymbol{\vartheta}^{t/r})$ being the 3D rotational matrix with $\boldsymbol{\vartheta}^{t/r} = [\vartheta^{t/r}, \varphi^{t/r}]^T$ being the transmitting/receiving array orientation with respect to its geometric center. The direction cosine in (1) is given by

$$\mathbf{d}(\boldsymbol{\theta}) = [\sin(\theta) \cos(\phi), \sin(\theta) \sin(\phi), \cos(\theta)]. \quad (2)$$

Finally, $\rho_{i/m}^{t/r} = \|\mathbf{p}_{i/m}^{t/r}(\boldsymbol{\vartheta}^{t/r}) - \mathbf{p}^t\|_2$ and $\boldsymbol{\theta}_{i/m}^{t/r} = [\theta_{i/m}^{t/r}, \phi_{i/m}^{t/r}]^T$ represent the transmitting/receiving spherical coordinates.

Having indicating with D the maximum diameter and with $d = \|\mathbf{p}^r - \mathbf{p}^t\|_2$ the distance between the two arrays, we suppose that they are sufficiently far from each other, i.e., $D \ll d$, in order to assume an identical angle of incidence at all the array antennas. Note that this hypothesis is especially verified at mm-wave where the array dimensions are very small thanks to the reduced wavelength. Given this assumption, it is possible to express the propagation delay and the amplitude between the m th receiving and the i th transmitting antenna, respectively, as

$$1) \tau_{im} \approx \tau + \tau_i^t(\boldsymbol{\theta}, \boldsymbol{\vartheta}^t) - \tau_m^r(\boldsymbol{\theta}, \boldsymbol{\vartheta}^r) \quad 2) a_{im} \approx a \quad (3)$$

where $\tau_{im} \triangleq \|\mathbf{p}_m^r - \mathbf{p}_i^t\|_2/c$ is the time-of-arrival (TOA) between the m th receiving and the i th transmitting antenna,

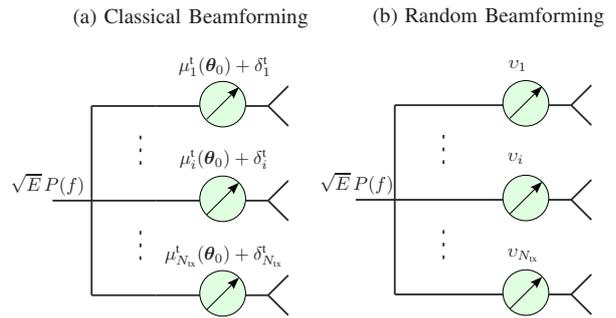


Fig. 2. Classical and random beamforming schemes.

$\tau \triangleq \|\mathbf{p}^r - \mathbf{p}^t\|_2/c = d/c$ is the TOA between the arrays centers and $\tau_{i/m}^{t/r}(\boldsymbol{\theta}, \boldsymbol{\vartheta}^{t/r})$ is the transmitting/receiving inter-antenna delay given by

$$\tau_{i/m}^{t/r}(\boldsymbol{\theta}, \boldsymbol{\vartheta}^{t/r}) = \frac{1}{c} \mathbf{d}(\boldsymbol{\theta}) \mathbf{p}_{i/m}^{t/r}(\boldsymbol{\vartheta}^{t/r}) \quad (4)$$

with c being the speed of light.

III. BEAMFORMING SCHEMES AND SIGNAL MODEL

In this section, the two array beamforming strategies present in Fig. 2 will be analysed from a signal processing point-of-view and by focusing on how the different signaling phasing schemes translate in different localization capabilities.

A. Transmitted Signal Model and Beamforming

The transmitted signal at the i th transmitting antenna is denoted with $g(t) = \sqrt{E} \Re\{p(t) e^{j2\pi f_c t}\}$ with $p(t)$ being the unitary energy equivalent low-pass signal, and f_c the carrier frequency. We consider a constraint on the total transmitted energy E_{tot} which is uniformly allocated among antennas, thus $E = E_{\text{tot}}/N_{\text{tx}}$ represents the normalized energy at each antenna element. We introduce the Fourier transform of $p(t)$ as $P(f) = \mathcal{F}\{p(t)\}$, with $\mathcal{F}\{\cdot\}$ denoting the Fourier transform operation in a suitable observation interval T_{obs} . For further convenience, the vector $\mathbf{p}(f) = P(f) \mathbf{1}_{N_{\text{tx}} \times 1}$ contains all the baseband transmitted signals with $\mathbf{1}_{N_{\text{tx}} \times 1}$ being a N_{tx} -sized vector of all ones.

In multi-antenna systems, beamforming is obtained by applying different weights at each array element. In classical beamforming, the objective of this operation is to coherently sum up signals towards the intended steering direction, i.e. $\boldsymbol{\theta}_0$. Considering the signal bandwidth W , when $W \ll f_c$ holds, this process can be realized using only PSs. The corresponding array structure is referred as phased array. Contrarily, in random beamforming, weights are randomly generated resulting in a non-directive radiation pattern but in an extremely low-complexity array design. In both cases, the beamforming weights are collected in a matrix that can be defined as

$$\mathbf{B} = \text{diag}(\omega_1, \omega_2, \dots, \omega_i, \dots, \omega_{N_{\text{tx}}}) \quad (5)$$

where the i th PS generic element can be written as

$$\omega_i = \begin{cases} e^{j2\pi f_c \tau_i^t(\boldsymbol{\theta}_0)} = e^{j\mu_i^t(\boldsymbol{\theta}_0)} & \text{Classical Beam.} \\ e^{jv_i} & \text{Random Beam.} \end{cases} \quad (6)$$

with v_i uniformly distributed between 0 and 2π , i.e., $v_i \sim \mathcal{U}(0, 2\pi)$.

In addition, even when classical beamforming is adopted, some technological issues could induce errors in the beamforming vector resulting in an increased side-lobe level (SLL), decreased array maximum gain and angular resolution. In fact, in practical implementations, digitally controlled PSs are often adopted in place of their high-resolution analog counterparts inducing quantization errors, to be accounted for in the localization performance analysis [19].

In the presence of such non-perfect weights, a matrix accounting for non-idealities is introduced

$$\mathbf{Q} = \text{diag}(\varsigma_1, \varsigma_2, \dots, \varsigma_i, \dots, \varsigma_{N_{\text{rx}}}) \quad (7)$$

where ς_i takes into account the i th beamforming weight quantization error, i.e., $\varsigma_i = \exp(j\delta_i^t)$ with δ_i^t being the phase error. For further convenience, let indicate with $\tilde{\omega}_i = \exp(j(\mu_i^t(\boldsymbol{\theta}_0) + \delta_i^t))$ the quantized weights in classical beamforming; whereas $\tilde{\omega}_i = \omega_i$ in random beamforming.

B. Received Signal Model

All the received signals are gathered in a vector $\mathbf{r}(f) = [R_1(f), \dots, R_m(f), \dots, R_{N_{\text{rx}}}(f)]^T$, where $R_m(f) = \mathcal{F}\{r_m(t)\}$ is evaluated in T_{obs} and $r_m(t)$ is the equivalent low-pass received signal at the m th receiving antenna. Specifically, the received signal vector can be written as $\mathbf{r}(f) = \mathbf{x}(f) + \mathbf{n}(f)$, where the set of useful received signals is

$$\begin{aligned} \mathbf{x}(f) &= [X_1(f), \dots, X_m(f), \dots, X_{N_{\text{rx}}}(f)]^T \\ &= \sqrt{E} \mathbf{a}^t(f, \boldsymbol{\theta}, \boldsymbol{\vartheta}^t) \mathbf{c}(f, \tau) \mathbf{A}^t(f, \boldsymbol{\theta}, \boldsymbol{\vartheta}^t) \mathbf{Q} \mathbf{B} \mathbf{p}(f) \end{aligned} \quad (8)$$

and $\mathbf{n}(f) = [N_1(f), \dots, N_m(f), \dots, N_{N_{\text{rx}}}(f)]^T$ is the noise vector with $N_m(f) = \mathcal{F}\{n_m(t)\}$, with $n_m(t) \sim \mathcal{CN}(0, N_0)$ being a circularly symmetric, zero-mean, complex Gaussian noise. The receiving and transmitting direction matrices for the inter-antennas delays and TX orientation are

$$\mathbf{a}^t(f, \boldsymbol{\theta}, \boldsymbol{\vartheta}^t) = [e^{j\gamma_1^t}, \dots, e^{j\gamma_m^t}, \dots, e^{j\gamma_{N_{\text{rx}}}^t}]^T \quad (9)$$

$$\mathbf{A}^t(f, \boldsymbol{\theta}, \boldsymbol{\vartheta}^t) = \text{diag}(e^{-j\gamma_1^t}, \dots, e^{-j\gamma_m^t}, \dots, e^{-j\gamma_{N_{\text{rx}}}^t}) \quad (10)$$

with $\gamma_{i/m}^{tr} = 2\pi(f + f_c)\tau_{i/m}^{tr}(\boldsymbol{\theta}, \boldsymbol{\vartheta}^{tr})$. The channel vector is indicated with $\mathbf{c}(f, \tau) = \alpha \mathbf{1}_{1 \times N_{\text{rx}}}$ being the $1 \times N_{\text{rx}}$, whose generic element is $\alpha = a \exp(-j2\pi(f + f_c)\tau)$. For further convenience, define $\nu_t = E_t/N_0 = \nu N_{\text{rx}}$, with $\nu = E/N_0$. The SNR at each receiving antenna element is $\text{SNR}_t = N_{\text{rx}} \text{SNR}_1$, where $\text{SNR}_1 = a^2 \nu$ represents the SNR component related to the direct path between a generic couple of TX-RX antenna elements.

IV. POSITION ERROR BOUND

In the following, we will derive the asymptotic limits of the TX position (i.e., \mathbf{p}^t) estimation error starting from the set of received waveforms $\mathbf{r}(f)$. Thus, we define the unknown parameters vector as $\boldsymbol{\psi} = [(\mathbf{p}^t)^T, a]^T$. We assume that an initial search between the TX and RX is conducted in order to coarsely infer the TX position and to allow the TX setting

its own beamforming weights to point towards the RX in the case in which classical beamforming is operated.

The performance of any unbiased estimator $\hat{\boldsymbol{\psi}} = \hat{\boldsymbol{\psi}}(\mathbf{r}(f))$ can be bounded by the Cramér-Rao bound (CRB) defined as [20]

$$\mathbb{E}_{\mathbf{r}, \boldsymbol{\psi}} \left\{ \left[\hat{\boldsymbol{\psi}} - \boldsymbol{\psi} \right] \left[\hat{\boldsymbol{\psi}} - \boldsymbol{\psi} \right]^T \right\} \succeq \mathbf{J}_{\boldsymbol{\psi}}^{-1} = \text{CRB}(\boldsymbol{\psi}) \quad (11)$$

where $\mathbf{J}_{\boldsymbol{\psi}}$ is the Fisher Information Matrix (FIM) given by

$$\mathbf{J}_{\boldsymbol{\psi}} \triangleq -\mathbb{E}_{\mathbf{r}, \boldsymbol{\psi}} \left\{ \nabla_{\boldsymbol{\psi}}^2 \ln f(\mathbf{r}|\boldsymbol{\psi}) \right\} = \begin{bmatrix} \mathbf{J}_{\text{pp}} & \mathbf{J}_{\text{pa}} \\ \mathbf{J}_{\text{ap}} & J_{aa} \end{bmatrix} \quad (12)$$

with the symbol $\nabla_{\boldsymbol{\psi}}^2 = (\partial^2/\partial\boldsymbol{\psi}\partial\boldsymbol{\psi})$ indicating the second partial derivatives with respect to the elements in $\boldsymbol{\psi}$ and

$$\mathbf{J}_{\text{pp}} = \begin{bmatrix} J_{xx} & J_{xy} & J_{xz} \\ J_{yx} & J_{yy} & J_{yz} \\ J_{zx} & J_{zy} & J_{zz} \end{bmatrix}, \quad \mathbf{J}_{\text{pa}} = \begin{bmatrix} J_{xa} \\ J_{ya} \\ J_{za} \end{bmatrix}. \quad (13)$$

Since the observations at each receiving antenna element are independent, the log-likelihood function $\ln f(\mathbf{r}|\boldsymbol{\psi})$ can be written as

$$\ln f(\mathbf{r}|\boldsymbol{\psi}) \propto -\frac{1}{N_0} \sum_{m=1}^{N_{\text{rx}}} \int_W |R_m(f) - X_m(f)|^2 df. \quad (14)$$

According to (12)-(14), it is possible to compute the elements of the FIMs as

$$\begin{aligned} J_{p_b p_a} &= 8\pi^2 \nu a^2 \sum_{mij} \Re \{ \tilde{\omega}_{ij} \xi_{ij} \chi_{ij}(2) \} \nabla_{p_a}(\tau_{im}) \nabla_{p_b}(\tau_{jm}) \\ J_{aa} &= 2\nu \sum_{mij} \Re \{ \tilde{\omega}_{ij} \xi_{ij} R_{ij}^p(\Delta\tau_{ij}) \} \\ J_{p_b a} &= 4\pi a \nu \sum_{mij} \Im \{ \tilde{\omega}_{ij} \xi_{ij} \chi_{ij}(1) \} \nabla_{p_b}(\tau_{im}) = 0 \end{aligned} \quad (15)$$

where $p_{a/b}$ indicate two elements in the set $\{x, y, z\}$, $\sum_{mij} = \sum_{m=1}^{N_{\text{rx}}} \sum_{i=1}^{N_{\text{rx}}} \sum_{j=1}^{N_{\text{rx}}}$, $\tilde{\omega}_{ij} = \tilde{\omega}_i (\tilde{\omega}_j)^*$, $\xi_{ij} = e^{-j2\pi f_c \Delta\tau_{ij}}$ with $\Delta\tau_{ij} = \tau_{im} - \tau_{jm}$, and

$$\begin{aligned} \chi_{ij}(2) &= \int_W (f + f_c)^2 e^{-j2\pi f \Delta\tau_{ij}} |P(f)|^2 df \\ \chi_{ij}(1) &= \int_W (f + f_c) e^{-j2\pi f \Delta\tau_{ij}} |P(f)|^2 df \\ R_{ij}^p(\Delta\tau_{ij}) &= \int_W e^{-j2\pi f \Delta\tau_{ij}} |P(f)|^2 df. \end{aligned} \quad (16)$$

The derivatives translating the TOA and DOA in position information can be expressed as

$$\nabla_p(\tau_{im}) = \frac{1}{c} \left\{ c \nabla_p(\tau) + \nabla_p(\mathbf{d}(\boldsymbol{\theta})) \left[\mathbf{p}_i^t(\boldsymbol{\vartheta}^t) - \mathbf{p}_m^t(\boldsymbol{\vartheta}^t) \right] \right\} \quad (17)$$

with

$$\begin{aligned} \nabla_p(\mathbf{d}(\boldsymbol{\theta})) &= \nabla_p(\theta) \cos(\theta) \begin{bmatrix} \cos(\phi) \\ \sin(\phi) \\ -\tan(\theta) \end{bmatrix}^T \\ &+ \nabla_p(\phi) \sin(\theta) \begin{bmatrix} -\sin(\phi) \\ \cos(\phi) \\ 0 \end{bmatrix}^T. \end{aligned} \quad (18)$$

$$\begin{aligned} \nabla_{\mathbf{pp}}(\tau_{im}, \tau_{jm}) &= \begin{bmatrix} \nabla_x(\tau_{im}) \nabla_x(\tau_{jm}) & \nabla_x(\tau_{im}) \nabla_y(\tau_{jm}) & \nabla_x(\tau_{im}) \nabla_z(\tau_{jm}) \\ \dots & \nabla_y(\tau_{im}) \nabla_y(\tau_{jm}) & \nabla_y(\tau_{im}) \nabla_z(\tau_{jm}) \\ \dots & \dots & \nabla_z(\tau_{im}) \nabla_z(\tau_{jm}) \end{bmatrix} \\ &= \frac{d_{\text{ant}}^2}{(cy)^2} \begin{bmatrix} (m_x - i_x)(m_x - j_x) & \frac{y}{d_{\text{ant}}} (m_x - i_x) & (m_x - i_x)(j_z - m_z) \\ \dots & \frac{y}{d_{\text{ant}}} & \frac{y}{d_{\text{ant}}}(j_z - m_z) \\ \dots & \dots & (i_z - m_z)(j_z - m_z) \end{bmatrix} \end{aligned} \quad (19)$$

Moreover, by further analyzing (15), one can notice the dependence of the FIM from the beamforming weights given by the coefficients $\tilde{\omega}_{ij}$.

Finally, by using the Schur complement, the PEB expression can be easily derived as

$$\begin{aligned} \text{PEB} &= \sqrt{\text{tr}(\text{CRB}(\mathbf{p}^t))} = \sqrt{\text{tr}\left(\left(\mathbf{J}_{\mathbf{pp}} - \mathbf{J}_{\mathbf{pa}} \mathbf{J}_{\mathbf{aa}}^{-1} \mathbf{J}_{\mathbf{pa}}^H\right)^{-1}\right)} \\ &= \sqrt{\text{tr}\left(\mathbf{J}_{\mathbf{pp}}^{-1}\right)} \end{aligned} \quad (20)$$

where $\text{tr}(\cdot)$ is the trace operation.

Equation (20) is a general bound valid for any beamforming strategy and accounting for signal weights quantization effects. Specialized expressions can be derived from (20) for specific cases to get insights on the key parameters affecting the performance as it will be done in the following.

A. Absence of Quantized Weights in Classical Beamforming

Here we provide an example on how the general expression (20) can be simplified in absence of beamforming weights errors. Given the FIM in (15), it can be easily found that for classical beamforming it is

$$\text{PEB} = \sqrt{\text{tr}\left(\mathbf{G}^{-1} \check{\mathbf{J}}_{\mathbf{pp}}^{-1}\right)} \quad (21)$$

where we have separated the effect of signal design $\check{\mathbf{J}}_{\mathbf{pp}}$ (i.e., that related to (16)) from that of the geometry \mathbf{G} (i.e., that related to (17)). Specifically for phased arrays, we have

$$\check{\mathbf{J}}_{\mathbf{pp}} = 8\pi^2 \text{SNR}_1 (\beta^2 + f_c^2) \quad (22)$$

$$\mathbf{G} = \sum_{mij} \nabla_{\mathbf{pp}}(\tau_{im}, \tau_{jm}) \quad (23)$$

where $\nabla_{\mathbf{pp}}(\tau_{im}, \tau_{jm})$ is a 3×3 matrix and β^2 is the squared baseband effective bandwidth of $p(t)$.

The matrix \mathbf{G} provides, through derivatives, the relationship between the TOA-DOA at each TX-RX antenna element couple and the TX position. To improve the comprehension of (21), in the next paragraph the particular case of planar arrays will be discussed considering a fixed orientation $\boldsymbol{\vartheta}^t = \boldsymbol{\vartheta}^r = [0, 0]^T$.

1) *Special Case: Planar Array:* For squared arrays with antennas spaced of d_{ant} , we can compute a simplified version of (17). Specifically, it is possible to obtain:

$$\begin{aligned} \nabla_p(\tau_{im}) &= \frac{1}{c} [c \nabla_p(\tau) + d_{\text{ant}} ((i_x - m_x) \nabla_p(\phi) \\ &\quad + (m_z - i_z) \nabla_p(\theta))] \end{aligned} \quad (24)$$

with $m_x = m_z = -\frac{\sqrt{N_{\text{tx}}}}{2}, \dots, \frac{\sqrt{N_{\text{tx}}}}{2}$ and $i_x = i_z = j_x = j_z = -\frac{\sqrt{N_{\text{rx}}}}{2}, \dots, \frac{\sqrt{N_{\text{rx}}}}{2}$. From (24), it is straightforward to derive (19). Then, by considering the summations present in (22), it is possible to obtain the elements of the position CRB matrix as

$$\begin{aligned} \text{CRB}(x) &= \text{CRB}(z) = \text{CRB}_0 \frac{12}{S} \frac{1}{N_{\text{tx}}(N_{\text{rx}} - 1)} \\ \text{CRB}(y) &= \frac{\text{CRB}_0}{N_{\text{tx}} N_{\text{rx}}} \end{aligned} \quad (25)$$

where CRB_0 represents the CRB of the ranging error one would obtain using single antenna which can be written as

$$\text{CRB}_0 = \frac{c^2}{8\pi^2 \text{SNR}_1 (\beta^2 + f_c^2)} \quad (26)$$

and $S = A^r/y^2$ with $A^r = N_{\text{rx}} d_{\text{ant}}$.

From (25) it is possible to remark that the CRB of the estimation error in the y -coordinate is inversely proportional to N_{tx} and N_{rx} : in fact, the N_{tx} term accounts for the SNR enhancement due to the beamforming process while the N_{rx} term accounts for the number of independent measurements available at the RX.

V. NUMERICAL RESULTS

In this section, numerical results are reported considering the two discussed beamforming schemes. For what the antennas spatial deployment is regarded, planar arrays are accounted for as they represent the most conventional structure to be integrated in small-sized devices. Differently from Sec. IV-A1, here we compare results with fixed and averaged RX orientations, thus giving the possibility to appreciate the impact of the array rotation on the localization performance.

We consider a scenario with a single RX with the centroid placed in $\mathbf{p}^r = [0, 0, 0]^T$, and a TX located in $\mathbf{p}^t = [0, 5, 0]^T$ ($d = 5$ m). As previously assumed, the RX has a perfect knowledge of the TX steering direction.

Results are obtained for $f_c = 60$ GHz and $W = 1$ GHz (the signal duration is $\tau_p = (1 + \beta)/W = 1.6$ ns) in free-space conditions. Root raised cosine (RRC) transmitted pulses centered at frequency $f_c = 60$ GHz and roll-off factor $\beta = 0.6$ are adopted, being compliant with the Federal Communications Commission (FCC) mask at 60 GHz [21]. A noise figure of $N_F = 4$ dB and a fixed transmitted power of $P_t = 10$ mW are considered, if not otherwise indicated.

The performance is evaluated in terms of PEB averaged over $N_{\text{cycle}} = 500$ Monte Carlo iterations. For each cycle, a different 3D RX array orientation is generated. The antennas are spaced apart of $d_{\text{ant}} = \lambda_L/2$, where $\lambda_L = c/f_L$ and

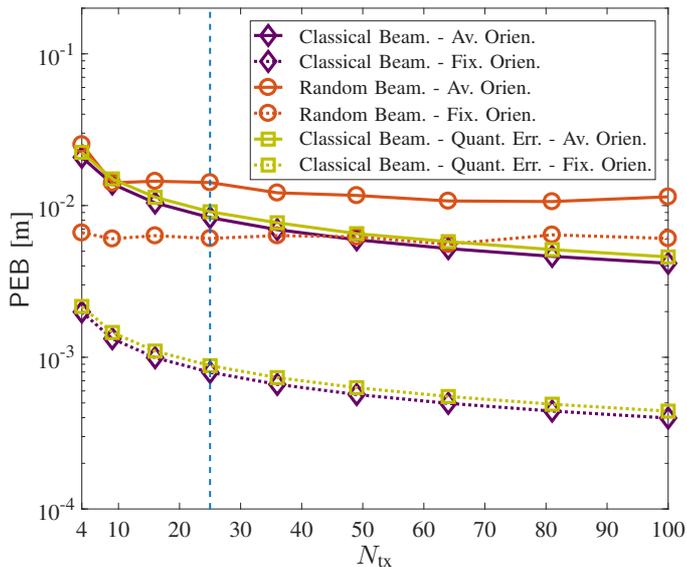


Fig. 3. Classical and random beamforming PEB vs. N_{tx} , $N_{rx} = 25$.

$f_L = f_c - W/2$. When present, the PSs quantization errors are $\delta_i^t \sim \mathcal{U}(-\pi/4, \pi/4)$ and the random beamforming weights $v_i \sim \mathcal{U}(0, 2\pi)$.

A. Results

Results have been obtained in free space conditions as a function of the number of antennas; of the beamforming schemes (i.e., classical vs. random); of the presence or absence of quantization errors; and as a function of arrays orientation.

In Fig. 3, the PEB performance is reported as a function of N_{tx} , for $N_{rx} = 25$ and averaged over different RX's orientations, apart for results referring to the fixed orientation (i.e., $\vartheta^r = [0, 0]^T$). It can be observed that classical beamforming is very sensitive to the particular geometric configuration chosen when compared with its random counterpart, and performance can drastically decrease when a rotational angle is considered. On the other side, the impact of quantization errors is not much appreciable both in fixed and averaged RX orientations.

For what random beamforming is regarded, it shares the structure simplicity of phased arrays but it does not allow the formation of a high gain main beam pointing towards the RX, and thus, the positioning accuracy results degraded with respect to that achievable with classical beamforming. Nevertheless, as previously mentioned, it results more insensitive with respect to the RX orientation. Consequently, if the localization accuracy required by the application of interest is not so stringent, random beamforming can be an interesting option to guarantee both a sub-centimeter positioning accuracy (e.g., for $N_{rx} = 50$ and $N_{rx} = 25$, $PEB \approx 1$ cm) and an easy implementation in future devices operating at mm-wave frequencies. For example, it could be employed for an initial coarse users localization estimation useful as a preliminary step before a precise beamforming operation. For what the number of TX antennas is concerned, it can be observed that the localization performance for $N_{tx} > 25$ is almost constant

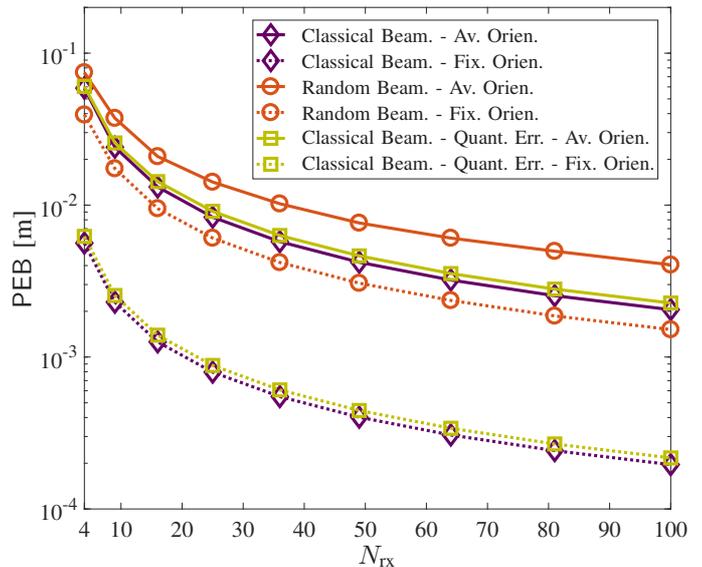


Fig. 4. Classical and random beamforming PEB vs. N_{rx} , $N_{tx} = 25$.

for all the configurations, and thus, it can be relaxed in order to guarantee an easy integration in portable devices.

In Fig. 4, the PEB results are reported as a function of the receiving antennas with N_{tx} fixed to 25. The same considerations drawn for Fig. 3 hold with the exception of those regarding the dependence on N_{rx} . Indeed, in this case, a higher number of antennas translates in a higher number of collected measurements and thus, in an increased localization accuracy.

VI. CONCLUSION

In this paper, we have considered a new scenario where a single-anchor localization exploiting mm-wave massive arrays has been put forth for next 5G applications. The theoretical PEB has been evaluated for different beamforming strategies, i.e., classical vs. random beamforming. Moreover, phase quantization errors and arrays orientation have been taken into account in the analysis.

From numerical results, we can conclude that classical beamforming permits to achieve a better localization performance thanks to the capability of focusing the power towards a precise direction in space; nevertheless, random beamforming attains a sub-centimeter accuracy even when the number of antennas is not extremely massive. Finally, the impact of quantization errors can be considered negligible. Consequently, whenever the localization requirements are not too stringent, it is possible to relax the implementation constraints (i.e., adoption of switches instead of analog PSs) without severely degrading the localization performance.

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