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Exceptional Composite Dark Matter

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ABSTRACT: We study the dark matter phenomenology of non-minimal composite Higgs models with $SO(7)$ broken to the exceptional group G_2 . In addition to the Higgs, three pseudo-Nambu-Goldstone bosons arise, one of which is electrically neutral. A parity symmetry is enough to ensure this resonance is stable. In fact, if the breaking of the Goldstone symmetry is driven by the fermion sector, this \mathbb{Z}_2 symmetry is automatically unbroken in the electroweak phase. In this case, the relic density, as well as the expected indirect, direct and collider signals are then uniquely determined by the value of the compositeness scale, f . Current experimental bounds allow to account for a large fraction of the dark matter of the Universe if the dark matter particle is part of an electroweak triplet. The totality of the relic abundance can be accommodated if instead this particle is a composite singlet. In both cases, the scale f and the dark matter mass are of the order of a few TeV.

Contents

1	Introduction	1
2	Viability of the \mathbb{Z}_2 symmetry	3
2.1	Gauge bosons	4
2.2	Fermions	6
3	Collider signatures	8
4	Searches for dark matter	10
4.1	Direct detection	10
4.2	Indirect detection	12
5	Singlet case	16
6	Conclusions	19
A	Representation theory of $SO(7)$ and G_2	22
B	$SU(2)_L \times U(1)_Y$ quantum numbers of the pNGBs	23
C	The case of composite leptons	24

1 Introduction

Composite Higgs Models (CHM) [1–3] are among the best motivated extensions of the Standard Model (SM) of particle physics. First of all, the hierarchy problem can be solved by assuming the Higgs to be a bound state of a new strongly interacting sector. This sector is supposed to respect an approximate global symmetry \mathcal{G} , which in turn is spontaneously broken to $\mathcal{H} \subset \mathcal{G}$ at a scale $f \sim \text{TeV}$. The Higgs is then expected to be naturally lighter than the scale of compositeness by further assuming that it is a pseudo Nambu-Goldstone Boson (pNGB) of this symmetry breaking pattern. Moreover, this approach could also help to understand the puzzling hierarchy of fermion masses in the SM. Indeed, the explicit breaking of \mathcal{G} by linear interactions between the SM fermions and composite operators [4, 5] translates into mixings between elementary fields and fermionic resonances at the confinement scale f . The Yukawa couplings emerge in the physical basis before electroweak (EW) symmetry breaking, being very much dependent on the dimension of the composite operators [6]. Therefore, making the mixing of different flavours depend on the dimension of their respective operators, their masses at the EW scale could be very different. In particular, the top quark Yukawa coupling can be much larger than the other

ones without any previous enhancement in the UV. In such a case, the explicit breaking of the global symmetry is triggered by the top quark linear mixing.

The requirement that one Higgs doublet is part of the pNGB spectrum restricts the amount of possible cosets. An exhaustive list of small groups can be found for instance in Reference [7]. In light of this background and the ongoing tests of the scalar sector at the LHC, a systematic study of non-minimal CHMs is a timely target that is worth aiming for.¹ With this spirit, in this paper we consider a model based on the symmetry breaking pattern $SO(7)/G_2$ [9], which gives rise to seven pNGBs transforming as $\mathbf{7} = (\mathbf{2}, \mathbf{2}) + (\mathbf{3}, \mathbf{1})$ under $SU(2) \times SU(2) \subset G_2$. Depending on which of the two $SU(2)$ groups is weakly gauged (and therefore identified with the SM $SU(2)_L$) the three additional pNGBs transform as a scalar real triplet or as three singlets of the EW group. The former constitutes a version of the inert triplet model [10] free of the hierarchy problem, in which we concentrate throughout most of the paper. We will highlight the main differences with the singlet case in the last section. In both cases, the neutral scalar can be forced to be odd under a \mathbb{Z}_2 symmetry which is shown to be compatible with the strong sector dynamics. Thus, this sector respects the symmetry $O(7) \cong SO(7) \times \mathbb{Z}_2$.² The neutral extra pNGB can then account for part or all of the observed dark matter (DM) relic abundance, depending on its $SU(2)_L$ quantum numbers.

The model presents several advantages in contrast to its elementary counterpart. Indeed, the larger symmetry on the strong sector constrains the number of independent free parameters. If the breaking of the Goldstone symmetry is mainly driven by the fermion sector, the scalar potential depends only on three quantities, two of which can be traded by the measured values of the Higgs mass and quartic coupling. The remaining parameter is just the compositeness scale f . Besides, the \mathbb{Z}_2 symmetry is automatically unbroken in the EW phase. On another front, the symmetry breaking pattern we consider provides a more interesting phenomenology than the minimal CHM of Reference [8]. First of all, it contains a DM candidate. Since direct and indirect DM searches bound the compositeness scale f from above, they also set a robust upper limit on the mass of the new fermionic resonances, which otherwise could not be estimated by other means than fine-tuning arguments. Moreover, since these new resonances decay into the extra scalars (for which there are no dedicated searches), constraints on vector-like fermions in light of current LHC data could therefore be weakened.

The structure of the paper is as follows. In Section 2 we demonstrate that the \mathbb{Z}_2 symmetry mentioned above can be respected by the strong sector; and we compute the pNGB sigma model for the triplet case. There, we also discuss the representation theory for fermions and derive the scalar potential. The possible collider signatures are described in Section 3. The computation of the relic density, as well as the analysis of potential direct and indirect detection signals are presented in Section 4. Finally, in Section 5 we consider the possibility that the three additional scalars transform as $SU(2)_L$ singlets

¹The adjective *non-minimal* refers to CHMs that present an extended scalar sector, contrary to the minimal model based on $SO(5)/SO(4)$ [8].

²Note that in what concerns the composite sector alone, the scalars are exact Goldstones and hence their interactions are shift invariant.

rather than as a triplet, highlighting the phenomenological differences. We conclude in Section 6. Further details on the algebra of $SO(7)$ and G_2 are provided in Appendices A and B, while in Appendix C we stress the main phenomenological consequences of sizable explicit symmetry breaking in the lepton sector.

2 Viability of the \mathbb{Z}_2 symmetry

For a generic symmetry breaking pattern, let T^i and X^a represent the unbroken and coset generators, respectively. Let us also define $\Pi = \Pi_a X^a$, where Π_a runs over all pNGBs. The $d_\mu = d_\mu^a X^a$ symbol from the Maurer-Cartan one form

$$\omega_\mu = -iU^{-1}\partial_\mu U = d_\mu^a X^a + E_\mu^i T^i, \quad \text{with} \quad U = \exp\left(i\frac{\Pi}{f}\right), \quad (2.1)$$

entering the non-linear sigma model, reads

$$\begin{aligned} d_\mu = \sum_{k=0}^{\infty} \frac{(-i)^k}{f^{k+1}(k+1)!} \text{ad}_\Pi^k(\partial_\mu \Pi)_X &= \frac{1}{f} \partial_\mu \Pi - \frac{i}{2f^2} [\Pi, \partial_\mu \Pi]_X - \frac{1}{6f^3} [\Pi, [\Pi, \partial_\mu \Pi]]_X \\ &+ \frac{1}{24f^4} [\Pi, [\Pi, [\Pi, \partial_\mu \Pi]]]_X + \dots \end{aligned} \quad (2.2)$$

where we have denoted $\text{ad}_A(B) = [A, B]$ and the subindex X means the projection into the broken generators. It is well known that the pNGB interactions in symmetric spaces contain only even powers of $1/f$. Indeed, for symmetric cosets, $[X^a, X^b] = if^{abi}T^i$, and hence all even powers in the expression above vanish. Consequently, the leading-order Lagrangian in derivatives describing the pNGB fields,

$$\mathcal{L}_\sigma = \frac{1}{2} f^2 \text{Tr}(d_\mu d^\mu), \quad (2.3)$$

constructed out of the trace of two d_μ symbols, contains only terms with even number of fields.

This concerns models like $SO(6)/SO(5)$ [11, 12], $SO(7)/SO(6)$ [13] or $SO(6)/SO(4) \times SO(2)$ [14], for example. We are instead interested on the coset $SO(7)/G_2$. The corresponding generators can be found in the Appendix A. They are normalized in such a way that $\text{Tr}(T^a T^b) = \delta^{ab}$ and $\text{Tr}(X^a X^b) = \delta^{ab}$. Besides, $\text{Tr}(T^i X^a) = 0$. A straightforward computation shows that this space is not symmetric. For example, $[N_1, N_2] = -i(M_3 + N_3/\sqrt{2})/\sqrt{3}$. Nevertheless, the leading-order sigma model still contains only even powers of f . This result relies on two properties. First, all commutators with odd powers of f in Equation 2.2 are parallel; likewise for all even powers. More concretely,

$$d_\mu = \frac{1}{f} \partial_\mu \Pi + g_1 \hat{\Pi}^2 [\Pi, \partial_\mu \Pi]_X + g_2 \hat{\Pi}^3 [\Pi, [\Pi, \partial_\mu \Pi]]_X, \quad (2.4)$$

with

$$g_1 = \frac{i}{a_1} \left[-1 + \cos\left(\frac{\sqrt{a_1} \hat{\Pi}}{f}\right) \right], \quad g_2 = \frac{1}{a_2} \left[-\frac{\Pi}{f} + \frac{1}{\sqrt{a_2}} \sin\left(\frac{\sqrt{a_2} \hat{\Pi}}{f}\right) \right]. \quad (2.5)$$

In the equations above, $a_1 = 5/6$, $a_2 = 11/18$, and

$$\hat{\Pi} = \sqrt{\Pi^a \Pi^a} . \quad (2.6)$$

Clearly, g_1 consists of only even powers of $1/f$, while g_2 contains only odd terms. And second, one can easily check that both $\text{Tr}(\partial_\mu \Pi [\Pi, \partial_\mu \Pi]_X)$ and $\text{Tr}([\Pi, \partial_\mu \Pi]_X [\Pi, [\Pi, \partial_\mu \Pi]_X])$ vanish, and so no odd powers of $1/f$ appear in the Lagrangian at leading order in derivatives. Given this, $SU(2)_L$ invariance implies that only terms with an even number of new multiplets are allowed, irrespectively of whether they are singlets or triplets.

We can then impose a \mathbb{Z}_2 symmetry under which the multiplet containing the new neutral scalar changes sign, regardless of whether it is a singlet or a triplet. Clearly, in light of the discussion above, this does not spoil the two-derivative Lagrangian containing the kinetic term of the propagating fields. Higher-order terms, instead, might be forbidden by this symmetry without observable phenomenological consequences.

2.1 Gauge bosons

Let us focus now on the triplet case. We can compute the leading-order covariant derivative Lagrangian for the pNGBs by promoting the derivatives in ω_μ and d_μ to covariant derivatives, *i.e.*, $\partial_\mu \rightarrow \partial_\mu - ig\sqrt{3}W_\mu^i M_i - ig'B_\mu F_3$ (see Appendix A for the expressions of M_i and F_3). At lowest order in derivatives, this leads to

$$\begin{aligned} \mathcal{L}_\sigma = & |D_\mu H|^2 \left(1 - \frac{1}{3f^2} |\Phi|^2\right) + \frac{1}{2} |D_\mu \Phi|^2 \left(1 - \frac{2}{3f^2} |H|^2\right) - \frac{1}{6f^2} \left[\Phi^\dagger t^i (D_\mu \Phi)\right] \left[(D^\mu \Phi)^\dagger t^i \Phi\right] \\ & + \frac{1}{3f^2} \partial^\mu (H^\dagger H) (\Phi^\dagger D_\mu \Phi) - \frac{2}{3f^2} |H|^2 |D_\mu H|^2 + \frac{1}{6f^2} \left[\partial_\mu (H^\dagger H)\right]^2 + \mathcal{O}\left(\frac{1}{f^4}\right) , \end{aligned} \quad (2.7)$$

where we have defined the following $SU(2)_L \times U(1)_Y \subset SO(4)$ multiplets:

$$H = \frac{1}{\sqrt{2}} (h_1 - ih_2, h_3 + ih_4)^T \sim \mathbf{2}_{1/2}, \quad \Phi = (\kappa_1 + i\kappa_2, -\eta, -\kappa_1 - i\kappa_2)^T \sim \mathbf{3}_0, \quad (2.8)$$

and $\kappa_1, \kappa_2, \eta, h_1, h_2, h_3, h_4$ are the pNGBs associated to the broken generators N_1, N_2, \dots, N_7 . H is identified with the SM-like Higgs doublet living in the $\mathbf{7}$ representation of G_2 and Φ with the remaining real triplet. Besides, t^i , with $i = 1, 2, 3$, read

$$t^1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}, \quad t^2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & -i & 0 \\ i & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \quad t^3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & -1 \end{pmatrix}. \quad (2.9)$$

We have also redefined $f \rightarrow -f/(2\sqrt{2/3})$. We will keep this convention henceforth. We also identify $h = h_3$ with the physical Higgs boson. The part of the above Lagrangian involving only h can be easily summed to all orders in $1/f^2$, resulting in

$$\mathcal{L}_\sigma \supset \frac{1}{2} (\partial_\mu h)^2 + \left[\frac{1}{4} g^2 f^2 \sin^2\left(\frac{h}{f}\right) W_\mu^+ W^{\mu-} + \frac{1}{8} (g^2 + g'^2) f^2 \sin^2\left(\frac{h}{f}\right) Z_\mu^+ Z^{\mu-} \right], \quad (2.10)$$

where we have defined

$$Z_\mu = \cos \theta_W W_\mu^3 - \sin \theta_W B_\mu, \quad A_\mu = \sin \theta_W W_\mu^3 + \cos \theta_W B_\mu \quad (2.11)$$

and $\tan \theta_W = g'/g$ as usual. In particular, we can see that after EW symmetry breaking (EWSB), the W and Z bosons get masses

$$m_W^2 = \frac{1}{4} g^2 f^2 \sin^2 \left(\frac{\langle h \rangle}{f} \right), \quad m_Z^2 = \frac{1}{4} (g^2 + g'^2) f^2 \sin^2 \left(\frac{\langle h \rangle}{f} \right), \quad (2.12)$$

with $\langle h \rangle$ the Higgs vacuum expectation value (VEV), which differs from the SM EW VEV $v = f \sin(\langle h \rangle/f) \sim 246$ GeV. It is also clear that $\rho = m_W^2/m_Z^2 c_W^2 = 1$, as expected due to the custodial symmetry $SO(4) \subset G_2$. The ratio of the tree level coupling between the Higgs and the massive gauge bosons to the corresponding SM coupling differs from unity by the amount:

$$R_{hVV} = \sqrt{1 - \xi}, \quad \xi = \frac{v^2}{f^2}. \quad (2.13)$$

Clearly, given that $f \sim \text{TeV}$, the ratio $\xi \ll 1$. If the SM group $SU(2)_L \times U(1)_Y$ of $SO(7)$ is the only gauged group in the EW sector, the global symmetry $SO(7)$ is broken explicitly. This becomes manifest in the (non-vanishing) scalar potential. In order to compute it, we promote the $SU(2)_L \times U(1)_Y$ gauge bosons to be in the adjoint of the global $SO(7)$ with the help of *spurion* fields. For this aim, let us order the generators of $SO(7)$ as $T^{\hat{a}} = \{F^1, \dots, F^7, M^1, \dots, M^7, N^1, \dots, N^7\}$. We can then write

$$A_\mu^{\hat{a}} = W_\mu^i \Xi^{i\hat{a}} + B_\mu \Upsilon^{\hat{a}}, \quad \hat{a} = 1, \dots, 21, \quad i = 1, 2, 3. \quad (2.14)$$

The spurions $\Xi^{i\hat{a}}$ and $\Upsilon^{\hat{a}}$ are given explicitly by the expressions:

$$\Xi^{i\hat{a}} = \sqrt{3} \delta^{(i+7)\hat{a}}, \quad \Upsilon^{\hat{a}} = \delta^{\hat{a}3}. \quad (2.15)$$

Formally, they also transform in the **21** of $SO(7)$. The *dressed* field $A_\mu^D = U^{-1} A_\mu^{\hat{a}} T^{\hat{a}} U$ transforms under $g \in SO(7)$ as $h(\Pi, g) A_\mu^D h^{-1}(\Pi, g)$, with $h \in G_2$, and decomposes as a sum of irreps of G_2 . The same happens to the dressed spurions $\Xi_D^i = U^{-1} \Xi^{i\hat{a}} T^{\hat{a}} U$ and $\Upsilon_D = U^{-1} \Upsilon^{\hat{a}} T^{\hat{a}} U$, with the difference that the index i spans an $SU(2)_L$ triplet.

The gauge contribution to the scalar potential consists therefore of the different invariants that can be built out of the G_2 irreps within Ξ_D^i and Υ_D and can be expressed as an expansion in powers of g/g_ρ and g'/g_ρ , with g_ρ the characteristic coupling of the strong sector vector resonances. Taking into account that Ξ_D^i and Υ_D decompose as $\mathbf{7} \oplus \mathbf{14}$ under G_2 , we obtain only one independent invariant at leading order:

$$V_{\text{gauge}}(\Pi) = \frac{3}{4} \frac{m_\rho^4}{(4\pi)^2} \left(\frac{g}{g_\rho} \right)^2 \frac{1}{\hat{\Pi}^2} \left[\left(6\tilde{c}_1 + 2\tilde{c}_2 \frac{g'^2}{g^2} \right) |H|^2 + 8\tilde{c}_1 |\Phi|^2 \right] \sin^2 \left(\frac{\hat{\Pi}}{f} \right), \quad (2.16)$$

where $\tilde{c}_{1,2}$ are $\lesssim 1$ dimensionless numbers, $m_\rho \sim g_\rho f$ is the typical mass of the vector resonances, and we have used naive dimensional analysis [15–17] to account for the \hbar and mass dependence of the radiative potential.

2.2 Fermions

The mixing between the elementary fermions and the composite sector breaks explicitly the global symmetry $SO(7)$, because the former transform in complete representations of the EW subgroup only. Let us first focus on the quark sector. The mixing Lagrangian can be written as:

$$\mathcal{L}_{\text{mix}} \sim \lambda_q^{ij} \bar{q}_{\alpha L}^i (\Delta_q^\alpha)^I (\mathcal{O}_q^j)_I + \lambda_u^{ij} \bar{u}_R^i (\Delta_u)^I (\mathcal{O}_u^j)_I + \lambda_d^{ij} \bar{d}_R^i (\Delta_d)^I (\mathcal{O}_d^j)_I + \text{h.c.} \quad (2.17)$$

The indices $i, j = 1, 2, 3$ run over the three quark generations. $\alpha = 1, 2$ and I are instead $SU(2)_L$ and $SO(7)$ indices, respectively. The couplings λ_{33}^q and λ_{33}^u are supposed to be order one, and, at any rate, much larger than all other couplings. This is expected from the dependence of the quark Yukawas on these numbers, namely $y_{u,d}^{ij} \sim \lambda_q^{\dagger ik} \lambda_{u,d}^{kj} / g_*$ where g_* is the typical coupling of the strong sector fermionic resonances. The spurion fields Δ are incomplete multiplets of $SO(7) \times U(1)_X$.³ Formally, they transform in the same representations as the corresponding composite operators, \mathcal{O} . We assume that the third generation right and left quarks mix with composite operators transforming in the $\mathbf{1}_{2/3}$ and the $\mathbf{35}_{2/3}$ of $SO(7) \times U(1)_X$, respectively. This is motivated by the following branching rules under $G_2 \times U(1)_X$ and the EW gauge group:

$$\mathbf{35} = \mathbf{1}_{2/3} \oplus \mathbf{7}_{2/3} \oplus \mathbf{27}_{2/3} = \mathbf{1}_{2/3} \oplus \mathbf{2}_{\pm 1/2} \oplus \mathbf{3}_0 \oplus \mathbf{1}_{2/3} \oplus \mathbf{2}_{\pm 1/2} \oplus \dots \quad (2.18)$$

where the ellipsis stands for higher-dimensional representations in the branching rule of the $\mathbf{27}$.⁴ In order not to break the EW symmetry, the spurions Δ_q^α can only have non-zero entries in the doublets. However, the \mathbb{Z}_2 symmetry requires the components along the second one to vanish.⁵ Its explicit expression can be found in Appendix A. Similarly to the gauge boson case, the dressed spurion $\Delta_{qD}^\alpha = U^{-1} \Delta_q^\alpha U$ transforms under $g \in SO(7)$ as $\Delta_{qD}^\alpha \rightarrow h(\Pi, g) \Delta_{qD}^\alpha h^{-1}(\Pi, g)$ with $h \in G_2$ and decomposes as a sum of irreps: $\Delta_{qD}^\alpha = \bigoplus_m \Delta_q^{\alpha m}$. The fermion contribution to the scalar potential can be written as

$$V_{\text{fermion}}(\Pi) \approx m_*^4 \frac{N_c}{(4\pi)^2} \left[\left(\frac{|\lambda_q|}{g_*} \right)^2 \sum_j c_j V_j(\Pi) + \left(\frac{|\lambda_q|}{g_*} \right)^4 \sum_k c'_k V'_k(\Pi) + \dots \right], \quad (2.19)$$

where $m_* \sim g_* f$ is the typical mass scale of the fermionic resonances and again we have used naive dimensional analysis to estimate the parametric dependence of the potential, with $N_c = 3$ and c_i and c'_i order one dimensionless numbers. $V_j(\Pi)$, $V'_k(\Pi)$ and the terms indicated by the ellipsis are the different invariants that can be built out of two, four and higher number of insertions of Δ_{qD}^m , respectively. For simplicity, we have also defined

³The addition of the extra (unbroken) $U(1)_X$ is necessary to accommodate the SM fermion hypercharges.

⁴Under $SO(4) \cong SU(2)_L \times SU(2)_R \subset G_2$: $\mathbf{7} = (\mathbf{2}, \mathbf{2}) \oplus (\mathbf{3}, \mathbf{1})$ and $\mathbf{27} = (\mathbf{1}, \mathbf{1}) \oplus (\mathbf{2}, \mathbf{2}) \oplus (\mathbf{3}, \mathbf{3}) \oplus (\mathbf{4}, \mathbf{2}) \oplus (\mathbf{5}, \mathbf{1})$.

⁵Let (i, j) run over the non-vanishing entries of the spurions Δ_q^1 and Δ_q^2 (see Appendix A). Then, note that under the \mathbb{Z}_2 , the elements (i, j) of the U matrix do not change sign. Therefore, the spurions are even eigenstates: $\mathbb{Z}_2(\Delta_q^1) = \Delta_q^1$ and $\mathbb{Z}_2(\Delta_q^2) = \Delta_q^2$. On the contrary, the spurion accommodating the second doublet includes, for example, a non-vanishing entry in $(1, 4)$, while $U_{14} \sim h_1 \kappa_1$, that changes sign.

$\lambda_q = \lambda_q^{33}$. Note that no terms proportional to λ_u appear, because the right-top mixing, being a full singlet, does not break the global symmetry.

The scalar potential consists then of the left-handed top-induced and the gauged-induced potentials. However, the latter can be neglected if

$$\tilde{c}_1 g^2 g_\rho^2 \lesssim 2\pi^2 \lambda_H \Rightarrow \tilde{c}_1 g_\rho^2 \lesssim 8, \quad (2.20)$$

where $\lambda_H \sim 0.13$ is the SM Higgs quartic coupling and we have disregarded the hypercharge contribution for simplicity. Indeed, if this inequality holds, all observables computed taking into account only the top-induced potential are (almost) unaffected when the gauge potential is also included. This occurs, in particular, for $\tilde{c}_1 \sim 0.1$ and moderately large values of g_ρ ; and also if $\tilde{c}_1 \sim 1$ and $g_\rho \sim 1$. Whereas the former possibility may involve some additional tuning, the latter arises naturally at large values of f , which, as we will see, are the ones preferred to account for the observed DM relic abundance. We consider this scenario hereafter. Then,

$$V(\Pi) \approx m_*^2 f^2 \frac{N_c}{16\pi^2} y_t^2 [c_1 V_1(\Pi) + c_2 V_2(\Pi)], \quad (2.21)$$

where $|\lambda_q|$ has been traded by the top Yukawa coupling y_t (see below) and we have defined

$$\sum_\alpha |(\Delta_{qD}^\alpha)_{88}|^2 \sim V_1(\Pi) = \frac{|H|^2}{\hat{\Pi}^2} \sin^2 \left(\frac{2\hat{\Pi}}{f} \right), \quad (2.22)$$

$$\sum_\alpha \sum_{i=1}^7 |(\Delta_{qD}^\alpha)_{i8}|^2 \sim V_2(\Pi) = \frac{|H|^2}{\hat{\Pi}^2} \cos \left(\frac{4\hat{\Pi}}{f} \right) + \frac{3|H|^2 + 2|\Phi|^2}{\hat{\Pi}^2} \cos \left(\frac{2\hat{\Pi}}{f} \right). \quad (2.23)$$

The scalar potential above depends only on two independent unknowns, c_1 and c_2 . They parametrize the two invariants constructed out of $\mathbf{1} \times \mathbf{1}$ and $\mathbf{7} \times \mathbf{7}$ in Equation 2.18, respectively. Note that the potential features only an even number of powers of Φ . This is actually true at any order in λ_q/g_* , because the spurions are \mathbb{Z}_2 -even and the \mathbb{Z}_2 invariance of the potential requires Φ to appear always squared. Let us further keep the leading-order potential in the expansion in powers of $1/f^2$. This can be matched to the renormalizable piece

$$V_{\text{renorm}}(H, \Phi) = \mu_H^2 |H|^2 + \lambda_H |H|^4 + \frac{1}{2} \mu_\Phi^2 |\Phi|^2 + \frac{1}{4} \lambda_\Phi |\Phi|^4 + \lambda_{H\Phi} |H|^2 |\Phi|^2. \quad (2.24)$$

The five parameters in Equation 2.24 can be expressed in terms of the parameters c_1 and c_2 . These can be traded by the measured values of the SM EW VEV and the Higgs quartic coupling, λ_H . Up to the scale f , all parameters of phenomenological relevance are then *predictions*. These are given in Table 1. It can be checked that $\langle \Phi \rangle = 0$ in the EW phase, since $\mu_\Phi^2 > 0$ and $\lambda_{H\Phi} > 0$. And so, as anticipated, the \mathbb{Z}_2 symmetry is not spontaneously broken.

It is also worth stressing that, after EWSB, the masses of the charged and neutral components of Φ are both equal to

$$m_\Phi^2 = \mu_\Phi^2 + v^2 \lambda_{H\Phi} = \frac{2}{3} f^2 \lambda_H \left[1 - \frac{9 v^2}{4 f^2} \right] + \dots, \quad (2.25)$$

Parameter	μ_H^2	μ_Φ^2	λ_Φ	$\lambda_{H\Phi}$
Value	$-v^2\lambda_H$	$\frac{2}{3}f^2\lambda_H\left(1 - \frac{8}{3}\frac{v^2}{f^2}\right)$	$-\frac{4}{9}\lambda_H\left(1 - \frac{8}{3}\frac{v^2}{f^2}\right)$	$\frac{5}{18}\lambda_H\left(1 + \frac{32}{15}\frac{v^2}{f^2}\right)$

Table 1. Values of the different parameters of the renormalizable scalar potential as a function of f , to order $\mathcal{O}(v^2/f^2)$. $v \sim 246$ GeV and $\lambda_H \sim 0.13$ stand for the SM EW VEV and the Higgs quartic coupling, respectively.

where the ellipsis stands for terms that are further suppressed by powers of v^2/f^2 . The splitting between the masses of the charged components and that of the neutral one comes only from (subdominant) radiative EW corrections. It can be estimated to be $\Delta M \sim 166$ MeV [18].

Finally, we can also compute the top Yukawa Lagrangian:

$$\begin{aligned} \sum_\alpha \bar{q}_L^\alpha (\Delta_{qD}^\alpha)^\dagger_{88} t_R + \text{h.c.} &\sim \mathcal{L}_{\text{yuk}} = c_t \lambda_q \left(\bar{q}_L \tilde{H} t_R \right) \frac{f}{\hat{\Pi}} \sin\left(\frac{2\hat{\Pi}}{f}\right) + \text{h.c.} \\ &= -y_t (\bar{q}_L \tilde{H} t_R) \left[1 - \frac{2}{3f^2} \Phi^2 + \dots \right] + \text{h.c.}, \end{aligned} \quad (2.26)$$

where c_t is an order one dimensionless parameter encoding the UV dynamics and the product $-2c_t\lambda_q$ has been traded by the top Yukawa, y_t . This Lagrangian is explicitly \mathbb{Z}_2 -invariant. If we add all terms involving only the Higgs boson, the ratio of the tree level coupling of the Higgs to the massive top quark to the corresponding SM coupling is:

$$R_{htt} = \frac{1 - 2\xi}{\sqrt{1 - \xi}}, \quad \xi = \frac{v^2}{f^2}. \quad (2.27)$$

3 Collider signatures

Different collider searches bound f from below. Among the more constraining ones, we find monojet analyses, searches for disappearing tracks, measurements of the Higgs to diphoton rate and EW precision tests. The small probability for an emission of a hard jet in association with two invisible Φ particles makes monojet searches less efficient than the other two.

The Higgs decay width into photons is modified by order ξ due to the non-linearities of the Higgs couplings, as stated in Eqs. 2.13 and 2.27, and, to a smaller extent, due to the new charged scalars that can run in this loop-induced process. The width (taking into account both effects) is given by [19, 20]:

$$\Gamma(h \rightarrow \gamma\gamma) = \frac{\alpha^2 v^2 m_h^3}{1024\pi^3} \left[\frac{g^2}{2m_W^2} \sqrt{1 - \xi} A_1(\tau_W) + \frac{4y_t^2}{3m_t^2} \frac{1 - 2\xi}{\sqrt{1 - \xi}} A_{1/2}(\tau_t) + \frac{\lambda_{H\Phi}}{m_\kappa^2} A_0(\tau_\kappa) \right]^2 \quad (3.1)$$

where $\tau_i = 4m_i^2/m_h^2$, $A_0(x) = -x^2(x^{-1} - F(x^{-1}))$, $A_{1/2}(x) = 2x^2(x^{-1} + (x^{-1} - 1)F(x^{-1}))$ and $A_1(x) = -x^2(2x^{-2} + 3x^{-1} + 3(2x^{-1} - 1)F(x^{-1}))$, while the function F is given by

$F(x) = \arcsin^2 \sqrt{x}$. The Higgs production cross section via gluon fusion is also modified by order ξ effects:

$$\sigma(gg \rightarrow h) = \frac{(1 - 2\xi)^2}{1 - \xi} \sigma^{\text{SM}}(gg \rightarrow h) , \quad (3.2)$$

with σ^{SM} the SM production cross section. Given that $\xi > 0$ and $\lambda_{H\Phi} > 0$ (see Table 1), the production cross section times branching ratio is always smaller than in the SM. A combination of 7 and 8 TeV data from both ATLAS and CMS [21] sets a lower bound of 0.66 on $\sigma(gg \rightarrow h \rightarrow \gamma\gamma)/\sigma_{\text{SM}}(gg \rightarrow h \rightarrow \gamma\gamma)$ at 95% C.L. This translates into a bound on $f \gtrsim 800$ GeV. EW precision tests [22] push this bound to $f \gtrsim 900$ GeV. Searches at future colliders (see for example Reference [23]) would determine the Higgs to diphoton cross section with a much better accuracy. In particular, the region $f \lesssim 1.5$ TeV is expected to be probed in Higgs searches at future facilities.

Finally, searches for disappearing tracks are sensitive to pair-production and the subsequent decay of the new scalars. Indeed, the small splitting between the charged and the neutral components of Φ implies that the former has a decay length exceeding a few centimeters. This produces tracks in the tracking system that have no more than a few associated hits in the outer region, in contrast with most of the SM processes. To our knowledge, the most constraining search of this kind was performed by the ATLAS Collaboration in [24] (similar results were found in the CMS analysis of Reference [25]). Searches of this type using 13 TeV data are not yet published.

The ATLAS search is optimized for a Wino (*i.e.* a generic triplet fermion, χ) with a width of ~ 160 MeV, corresponding to a lifetime of ~ 0.2 ns, whose charged components therefore decay predominantly into the neutral one and a soft pion. In this respect, the search applies equally well to our scalar triplet. The search rules out any mass below ~ 270 GeV, corresponding to a production cross section of ~ 0.25 pb. The latter takes into account the production of all $\chi^+\chi^-$, $\chi^+\chi^0$ and $\chi^-\chi^0$. The corresponding bound on f is therefore given by the value at which the production cross section in the scalar case equals the previous number (note that, for the same mass, the scalar and triplet cross sections can be very different).

In order to compute this cross section at the same level of accuracy as the one considered in the experimental reference, *i.e.* at NLO in QCD, we first implement the renormalizable part of our model in `Feynrules v2` [26]. UV and R_2 terms [27] are subsequently computed by means of `NLCOT` [28]. The interactions are then exported to an `UFO` model that is finally imported in `MadGraph v5` [29] to generate parton-level events from which the total cross section is computed for all values of f in the range 500, 600, ..., 1500 GeV. The bound on f turns out to be only $f \gtrsim 650$ GeV. However, future facilities could easily exceed the reach of Higgs searches. Indeed, a naive reinterpretation of the results in Reference [30] (see also [31]) suggests that values of f as large as ~ 3.5 TeV could be tested in a future 100 TeV pp collider.

4 Searches for dark matter

In this section of the paper we analyze the extent to which η , the neutral component of the scalar triplet Φ of our model, can contribute to the DM of the Universe, given the current experimental constraints. As we anticipated in the Introduction, the compatibility of a global \mathbb{Z}_2 symmetry with the breaking pattern $SO(7)/G_2$ allows to forbid η decays. This neutral particle, which couples to the SM through weak interactions and does not couple directly to the photon is, a priori, a good weakly interacting massive particle (WIMP) DM candidate with the adequate mass scale. Remarkably, the mass of η and its relic abundance are, in our case, entirely determined by the scale f , which makes the model extremely predictive. In this last respect, the model is on par with other simple implementations of the WIMP idea, such as the Minimal DM model [18].

We recall that the total annihilation rate, $\langle\sigma v\rangle$, and the relic abundance, Ωh^2 , of any thermal relic satisfy the approximate relation

$$\Omega h^2 \sim \frac{3 \times 10^{-27}}{\langle\sigma v\rangle} \text{ cm s}^{-1}, \quad (4.1)$$

where the brackets indicate the average over the thermal velocity distribution. Thus, if a thermal relic explains the totality of the DM abundance ($[\Omega h^2]_{\text{DM}} \sim 0.11$ [32]), it must have an annihilation rate of the order of $\langle\sigma v\rangle \sim 3 \times 10^{-26} \text{ cm s}^{-1}$.

Given the expression 4.1, the relic abundance turns to be roughly proportional to the mass squared of the thermal relic. The relic abundance for the neutral component of a scalar triplet as a function of its mass was computed in [33]. Including non-perturbative effects, it was found that a mass of ~ 2.5 TeV is required to obtain the measured DM abundance. In Figure 1, we recast this result as a function of the compositeness scale f of our model, which is related to the mass of the neutral component of the triplet, η , through Equation 2.25.⁶ As shown in Figure 1, a scale $f \sim 8.6$ TeV is required in this case to account for the totality of the DM in the Universe. In the remaining of this section we explore whether this scale is compatible with the current bounds from the LHC and direct and indirect detection experiments; and we determine how much DM can be accounted for by η .

4.1 Direct detection

The cross section for spin-independent scattering of DM on nucleons has a tree-level contribution proportional to the portal coupling $\lambda_{H\Phi}$ [34]:

$$\sigma(\eta N \rightarrow \eta N)_{\text{tree}} = \frac{\lambda_{H\Phi}^2 m_N^4 f_N^2}{\pi m_h^4 m_\Phi^2} \approx \frac{25 m_N^4 f_N^2}{864 \pi f^2 v^4 \lambda_H} \left(1 + \frac{391 v^2}{60 f^2}\right), \quad (4.2)$$

which scales with the inverse of the DM mass squared and arises from the tree level exchange of a Higgs boson on t -channel (see Figure 2 (a)), where

$$f_N = \sum_q f_q = \sum_q \frac{m_q}{m_N} \langle N | \bar{q} q | N \rangle = 0.30 \pm 0.03, \quad (4.3)$$

⁶The result shown in Figure 1 assumes that the portal coupling $\lambda_{H\Phi}$ is negligible. This is indeed the case in our model, since $\lambda_{H\Phi}$ is roughly an order of magnitude smaller than the gauge couplings.

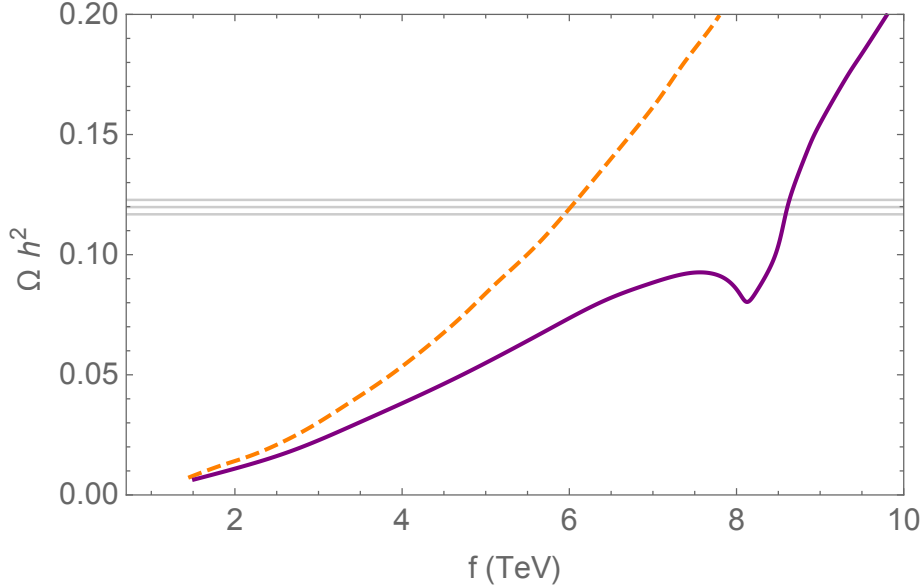


Figure 1. The dependence of the relic abundance Ωh^2 of η as a function of the compositeness scale f , with (continuous) and without (dashed) non-perturbative effects; see [33]. The horizontal lines show the measured central value and a 95% C.L. interval around it as determined by Planck [32].

and $m_N = \frac{1}{2}(m_n + m_p) \sim 1 \text{ GeV}$ is the nucleon mass. However, due to the presence of derivative interactions $\sim i\Phi \overleftrightarrow{\partial}_\mu \Phi W^\mu$ in the Lagrangian, there is also a loop induced contribution independent of m_Φ . It comes from the virtual exchange of W bosons (which is insensitive to $\lambda_{H\Phi}$), because they bring down a $p^2 \approx m_\Phi^2$ term which precisely cancels the $1/m_\Phi^2$ factor coming from the phase space integral, see *e.g.* the diagrams in Figures 2 (b)-(d). Such cross section has been computed in the heavy WIMP effective theory (HWET) [35–38]. The leading term in the $1/m_\Phi$ expansion (valid therefore for $m_\Phi \gg m_W \gg m_q$) reads

$$\sigma(\eta N \rightarrow \eta N)_{\text{HWET}} = 1.3_{-0.5-0.3}^{+0.4+0.4} \times 10^{-2} \text{ z b} . \quad (4.4)$$

This value includes contributions from two-loop diagrams and is *universal*, in the sense that it only depends on the $SU(2)_L$ quantum numbers of the heavy particle, while further details of the model (such as the spin of the WIMP or its possible interaction with the Higgs) enter only through $1/m_\Phi$ corrections.

In order to provide a conservative estimate of the sensitivity of current and projected direct detection experiments to this model, we show in Figure 3 the sum of both contributions to the spin-independent cross section as a function of the compositeness scale (purple) versus the latest limits from LUX [39] (dashed orange) together with the projected sensitivities for LZ (dashed green) [40] and XENON1T (dashed red) [41]. The latter are properly rescaled by $[\Omega h^2]_{\text{DM}}/\Omega h^2$, which takes into account that η could be just a subcomponent of the whole relic abundance. In order to be more conservative, we have used the 1σ upper

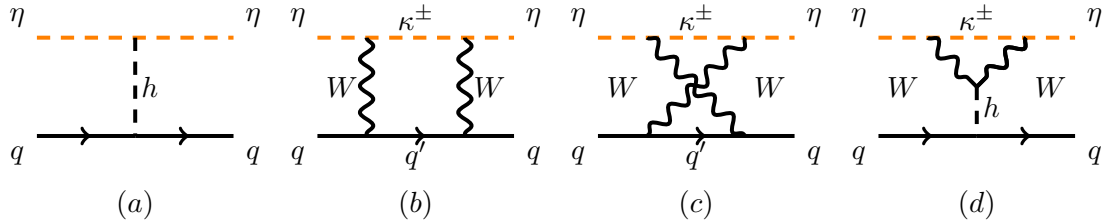


Figure 2. (a): Tree level contribution to the cross section for spin-independent scattering of DM on nucleons. (b)-(d): Representative examples of loop-induced diagrams which are relevant for the m_{Φ} -independent piece of the cross section.

values for both contributions in $\sigma(\eta N \rightarrow \eta N)$. It should be noted that this is only an estimate of the DM-nucleon cross section, since the validity of the HWET breaks down for low values of f (and hence low masses). Besides, we are neglecting possible interference effects. In any case, the low sensitivity of current experiments ensures that making more accurate predictions is not needed. Interestingly, the order of magnitude of the estimated cross section is in the ballpark of the aimed sensitivity for LZ, making the model accessible via direct detection in the near future.

4.2 Indirect detection

Indirect DM searches use astrophysical and cosmological observations to look for the effects of SM particles into which DM is assumed to decay or annihilate. Concretely, they focus on the Cosmic Microwave Background (CMB) and the detection of gamma and cosmic rays originating from decays or annihilations of DM. We consider the effects due to the W boson pairs that are produced in the annihilation of η particles, which is the main relevant channel in our case. We restrict our attention to three different kinds of indirect probes, which provide the current most constraining bounds on the annihilation rate of WIMPs: the CMB, gamma rays coming from dwarf spheroidal galaxies and gamma rays from the center of the Milky Way. The last of these two observables have intrinsic uncertainties due to our limited knowledge about the DM distribution inside galaxy halos; and therefore the CMB leads to a more robust bound.

In Figure 4 we compare the theoretical prediction for the annihilation rate $\langle\sigma v\rangle$ of η particles from [33],⁷ as a function of the scale f , with the current bounds from Planck, H.E.S.S. and FERMI+MAGIC. The shape of all the curves, peaking around ~ 8.2 TeV is due to the use of Figure 1 to rescale the bounds on $\langle\sigma v\rangle$ from the various collaborations. This is needed to account for the fact that the event rate of any annihilation process scales as the square of the local density of annihilating particles, which in the case of WIMPs can be assumed to be approximately proportional to the relic density Ωh^2 . The usual indirect detection upper bounds on the DM annihilation rate assume that all the DM in the Universe corresponds to a single WIMP species of a given mass. In order to include the possibility that η explains only a fraction of the total DM abundance, the experimental bounds have

⁷See Figure 3 in Reference [33] for a scalar triplet.

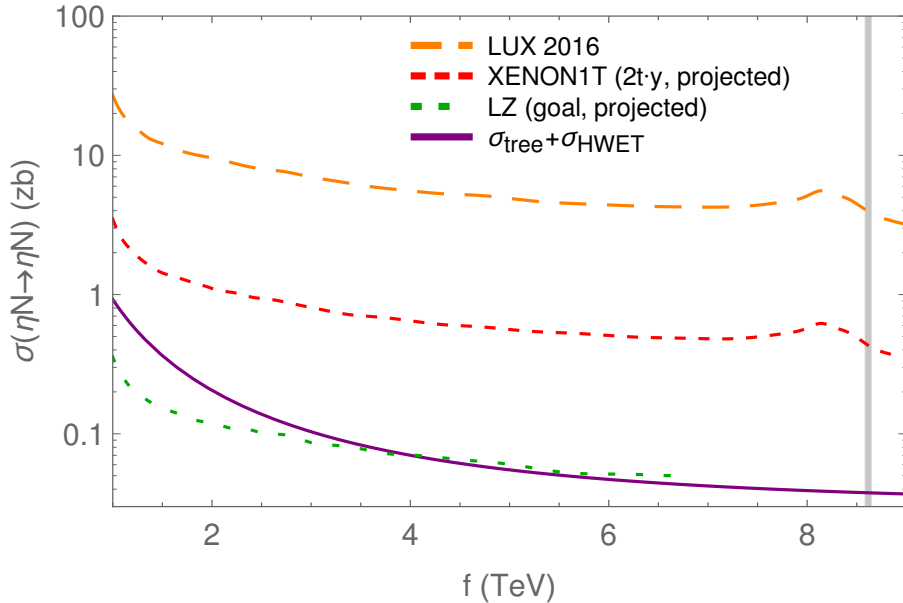


Figure 3. Estimate for the spin-independent direct detection cross section $\sigma(\eta N \rightarrow \eta N) = \sigma(\eta N \rightarrow \eta N)_{\text{tree}} + \sigma(\eta N \rightarrow \eta N)_{\text{HWET}}$ as a function of the compositeness scale f (purple) versus the current limits (linearly rescaled with the DM abundance) from LUX (dashed orange) [39] and the projected exclusion limits at 95% C.L. for LZ (dotted green) [40] and XENON1T of 2 years in 1 ton (dashed red) [41].

thus to be multiplied by a factor $([\Omega h^2]_{\text{DM}}/[\Omega h^2])^2 \simeq 0.012 [\Omega h^2]^{-2}$. Obviously, this takes into account the dependence of the abundance Ωh^2 of η on its mass (or, equivalently, on the scale f), as shown in Figure 1.

The weakest indirect detection bounds that we consider come from the observation by the Cherenkov radiation telescope H.E.S.S. of dwarf spheroidal galaxies, which are strongly DM dominated systems and supposed to be free from other gamma ray emission. These bounds correspond to the two upper lines of Figure 4, see [43]. The distance between them comes from their different assumptions for the radial distribution of DM in those galaxies. The upper curve assumes a Burkert profile [44], which features a constant inner density core, whereas the lower one is for an NFW profile [45, 46], which peaks at the center. A more stringent limit from dwarf spheroidals is reported by the collaborations of the FERMI satellite and the Cherenkov telescope MAGIC. The combination of their respective data leads to the red dashed curve [47], assuming an NFW profile. Although these data are more constraining, a direct comparison to the results of H.E.S.S. is not straightforward, since the details of the assumed profiles are different.

Notwithstanding the importance of dwarf spheroidal galaxies for indirect DM detection, the center of the Milky Way is thought to be the strongest gamma ray emitter and therefore an important candidate for a potential indirect DM detection. Clearly, the choice of DM profile is critical for the interpretation of these observations, but unfortunately the DM distribution in the center of our galaxy is uncertain. Moreover, there is a number of

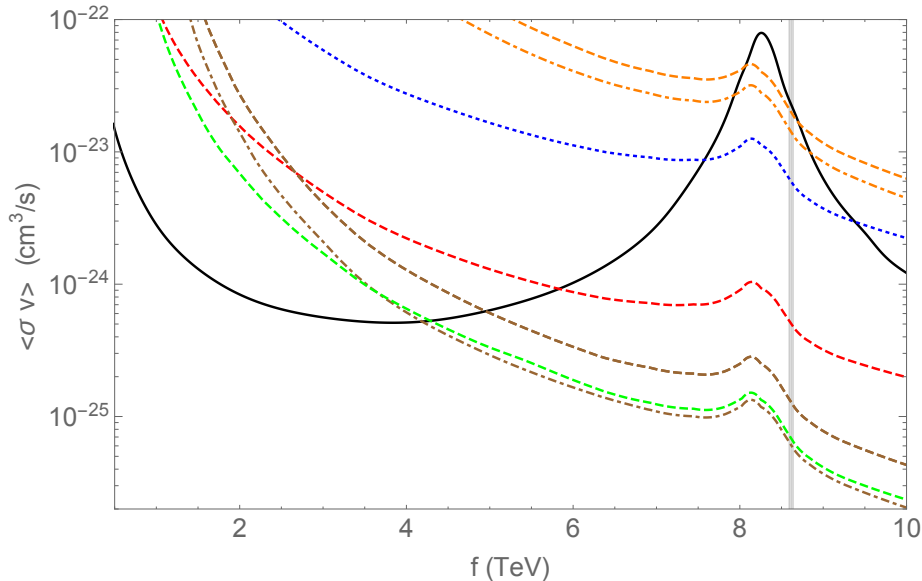


Figure 4. The thermally averaged annihilation rate of $\eta\eta$ into W^+W^- as a function of the compositeness scale, f . The black continuous line is the theoretical prediction of the model. From top to bottom we also show the upper bounds (rescaled with the square of the DM abundance) from the following observations: H.E.S.S. dwarf spheroidal galaxies [Burkert (dashed) and NFW (dot-dashed) profiles, in orange], CMB from Planck (blue, dotted), the combination of FERMI and MAGIC dwarf spheroidal galaxies (red, dashed), and the Milky Way center as seen by H.E.S.S. [NFW (dashed) and Einasto (dot-dashed) profiles, in brown]. See the main text for references. The green dashed line is the expected sensitivity of CTA for observations of the Milky Way center assuming an Einasto profile [42]. The vertical band at $f \simeq 8.5$ TeV locates the scale that gives the total DM abundance with a 95% C.L. from the prediction of the model; see also Figure 1.

baryonic astrophysical sources of gamma rays which need to be accounted for when considering the possible emission from the Galactic center. These backgrounds are not well known either and this implies a large source of uncertainty in addition to the choice of DM profile. The pair of brown lines at the bottom of Figure 4 represent the current constraints from the Milky Way galactic center obtained by H.E.S.S. [48] for two profile choices: NFW (dashed) and Einasto [49] (dot-dashed). Although these observations appear to be the most stringent, it has to be emphasized that they are also the ones whose interpretation carries a larger uncertainty. It is interesting to point out that modifying the parameters of the NFW profile these limits can be weakened slightly above the Einasto curve, see [48].

As we mentioned earlier, the most robust bounds come from the CMB, and in particular from the Planck satellite. The blue dashed line of Figure 4 represents the bound obtained in the analysis of [50]. According to the CMB upper bound on the annihilation rate, our exceptional DM model can account for as much as 80% of the DM abundance of the Universe at 95% C.L., as can be read from Figures 4 and 1. This requires a value of the composite scale $f \simeq 7.5$ TeV, which corresponds to a triplet mass of ~ 2.2 TeV. If instead we take the strongest limits from the Galactic center from H.E.S.S. the maximum

percentage of the DM abundance that can be explained by η is at most 36%, corresponding to $f \simeq 4.25$ TeV and a mass of ~ 1.25 TeV. Given that indirect detection sets the strongest upper bounds in our model, we can conclude that a significant amount of the DM of the Universe might be in the form of the neutral component of our triplet.

Future indirect detection data could in principle test the model with improved sensitivity in the range of f that is relevant for DM. The Cherenkov Telescope Array CTA [51], which should start taking data by 2021, may currently be the best proposal that could contribute to that goal. Several CTA sensitivity estimates exist in the literature, in particular, for DM annihilation in the Galactic center into a pair of W bosons [42, 52, 53]. These estimates vary depending on the assumptions made about the final configuration design of the telescope array, the observational strategy (including its timespan) and several other factors. In Figure 4 we report the forecast of reference [42] for DM annihilation into W bosons, appropriately rescaled with the DM abundance. According to [42], it appears that once systematics effects are accounted for, the upper bound that will be reachable with CTA for this specific channel might not be too dissimilar from the most stringent current limits obtained by H.E.S.S. [48]. However, the value of the cross section that will be attainable with CTA for the range of masses that interests us is estimated to be a factor ~ 4.5 lower in [53]; but this number accounts only for statistical errors. In any case, it is clear that a proper comparison between current bounds and different forecasts would require, at the very least, the use of the same DM profile.

In principle, the model could also be constrained from searches of monochromatic gamma lines due to the annihilation of DM into two photons in the central regions of the Milky Way. To the best of our knowledge, the latest and most stringent upper bounds on the cross section for this process in the relevant range of mass have been obtained by the H.E.S.S. collaboration [54, 55]. A DM mass of ~ 1.2 TeV approximately corresponds to $f \sim 4$ TeV, which is the scale at which the H.E.S.S. limits on DM annihilation into W^+W^- intersect the theoretical prediction; see Figure 4. The current strongest bound for $\eta\eta \rightarrow \gamma\gamma$ and DM masses around that value is $\langle\sigma v\rangle \sim 10^{-27}$ cm³/s at 95% C.L., assuming an Einasto profile. For a scalar triplet with zero hypercharge, this cross section has been computed (including the Sommerfeld effect) in [33]. After the adequate rescaling with the DM abundance, the theoretical prediction is $\langle\sigma v\rangle \sim 5 \times 10^{-28}$ cm³/s, which is an order of magnitude lower than the aforementioned upper bound. Although, once more, the DM profile dependence is an important source of uncertainty,⁸ this channel is not more constraining in our case than $\eta\eta \rightarrow W^+W^-$.

A CTA sensitivity estimate applicable for $\eta\eta \rightarrow \gamma\gamma$ was produced in [57] under the assumption of an NFW profile. Translating this estimate to the relevant range of f and after rescaling by the DM abundance, it gives $\langle\sigma v\rangle \sim 3 \times 10^{-29}$ cm³/s, which is an order of magnitude lower than the theoretical estimate. This means that CTA observations of monochromatic gamma lines should allow to probe the model beyond the current H.E.S.S. bound from $\eta\eta \rightarrow W^+W^-$. This type of search may in fact be able to test all the range of f for which the limits on the annihilation cross section into W bosons still allows to

⁸See *e.g.* Reference [56].

account for a significant fraction of the DM relic abundance.

5 Singlet case

The model we have explored so far provides a hyperchargeless scalar triplet as DM candidate. This is a consequence of weakly gauging one particular $SU(2)$ of the two global ones respected by the strong sector, which makes the fundamental representation of $SO(7)$ decompose as $\mathbf{7} = \mathbf{2}_{1/2} \oplus \mathbf{3}_0$ under the EW subgroup $SU(2)_L$. However, as it was done in [9], one can also weakly gauge the other $SU(2)$ within $SO(4) \cong SU(2)_L \times SU(2)_R$, under which $\mathbf{7} = \mathbf{2}_{1/2} \oplus \mathbf{1}_0 \oplus \mathbf{1}_{\pm 1}$, obtaining an isospin singlet as potential DM candidate. We follow this path in this section, highlighting the specific differences between the two cases.

Gauge contribution to the scalar potential Contrary to the triplet case, the potential of the new charged (and hypercharged) scalars receives contributions proportional to g' . Equation 2.16 has to be modified by:

$$V_{\text{gauge}}(\Pi) = \frac{3}{4} \frac{m_\rho^4}{(4\pi)^2} \left(\frac{g}{g_\rho}\right)^2 \frac{1}{\hat{\Pi}^2} \left[\left(6\tilde{c}_1 + 2\tilde{c}_2 \frac{g'^2}{g^2}\right) |H|^2 + 8\tilde{c}_2 \frac{g'^2}{g^2} \kappa^+ \kappa^- \right] \sin^2 \left(\frac{\hat{\Pi}}{f}\right). \quad (5.1)$$

This term modifies the mass splitting between κ^\pm and η , with respect to the case of the triplet. It gives a contribution $(m_{\kappa^\pm} - m_\eta)/m_\eta \sim g'^2/(N_c y_t^2) \sim 0.05$.

Fermion contribution to the scalar potential In the singlet case, the charged and neutral scalars do not exchange gauge bosons, and hence the first cannot decay into the second. In order to avoid an over-abundance of stable charged particles, for which stringent constraints exist [58–60] new sources of sizable explicit symmetry breaking have to be considered. Being the second heaviest fermion, we assume that this effect is driven by the bottom quark. There are many different possible embeddings of the right-handed bottom quark, b_R . However, not all of them respect the \mathbb{Z}_2 symmetry $\eta \leftrightarrow -\eta$ that makes the singlet scalar stable or generate a bottom Yukawa coupling at leading order in $\lambda_q \lambda_{b_R}$, with $\lambda_{b_R} = \lambda_d^{33}$. We consider the case where b_R mixes with the $\mathbf{7}_{2/3}$ within the $\mathbf{21}_{2/3}$, since it fulfills both conditions. Then, Equation 2.21 still holds, but it has to be supplemented by the (sub-leading) bottom contribution to the scalar potential:

$$V_{\text{bottom}}(\Pi) = \frac{N_c}{(4\pi)^2} m_*^4 \hat{c}_1 \left(\frac{|\lambda_{b_R}|}{g_*}\right)^2 \frac{1}{\hat{\Pi}^2} [2|H|^2 + \eta^2 + \kappa^+ \kappa^-] \sin^2 \left(\frac{\hat{\Pi}}{f}\right). \quad (5.2)$$

This term of the potential also contributes to breaking the mass degeneracy between κ^\pm and η , giving $(m_{\kappa^\pm} - m_\eta)/m_\eta \sim (g_* y_b)^2/y_t^4 \sim 6 \times 10^{-4} g_* \lesssim 10^{-2}$. In addition, the following Yukawa couplings are generated

$$\begin{aligned} \sum_\alpha \sum_{i=1}^7 \bar{q}_L^\alpha (\Delta_{qD}^\alpha)^\dagger_{i8} (\Delta_b)_{i8} b_R + \text{h.c.} &\sim \mathcal{L}_{\text{yuk,b}} = \frac{c_b}{2\sqrt{6}} \frac{\lambda_q^* \lambda_{b_R}}{g_*} \frac{f}{\hat{\Pi}} \sin \left(\frac{\hat{\Pi}}{f}\right) \bar{q}_L \left[H \cos \left(\frac{\hat{\Pi}}{f}\right) \right. \\ &\left. - i\tilde{H} \frac{3}{\sqrt{2}} \frac{\kappa^+}{\hat{\Pi}} \sin \left(\frac{\hat{\Pi}}{f}\right) \right] b_R + \text{h.c.} = -y_b \bar{q}_L \left[H - i\tilde{H} \frac{3}{\sqrt{2}} \frac{\kappa^+}{f} \dots \right] b_R + \text{h.c.}, \end{aligned} \quad (5.3)$$

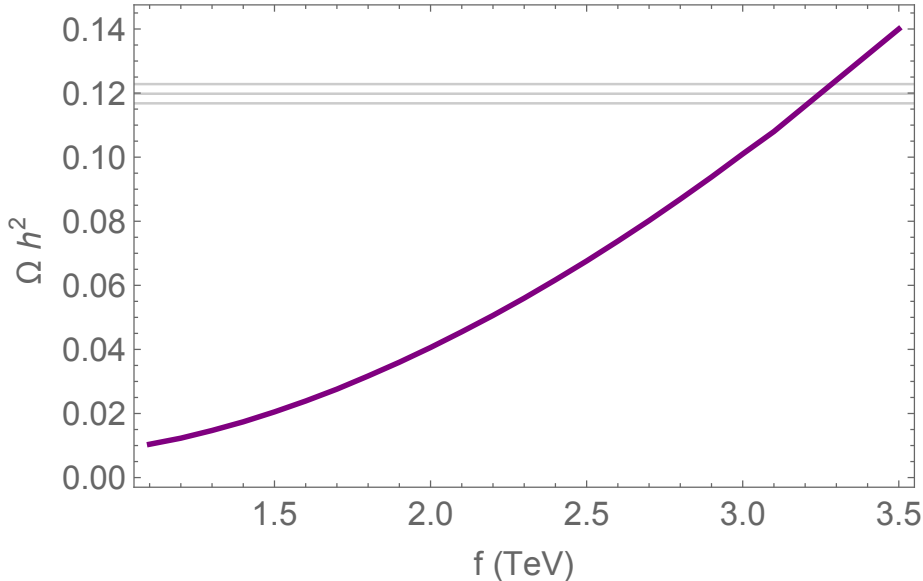


Figure 5. The dependence of the relic abundance Ωh^2 in the singlet case as a function of the compositeness scale f . The horizontal lines show the measured central value and a 95% C.L. interval around it as determined by Planck [32].

where c_b is a dimensionless order one parameter and we have traded $\frac{c_b}{2\sqrt{6}} \frac{\lambda_q^* \lambda_{bR}}{g_*}$ by $-y_b$ in the second expression. This provides a vertex $i \frac{3}{\sqrt{2}} \frac{m_b}{f} \bar{t}_L b_R \kappa^+$ that makes κ^\pm decay into tb .

Collider implications Searches for disappearing tracks do not constrain the singlet case. So, measurements of the Higgs couplings dominate the reach of current and future facilities. On another hand, analyses of invisible Higgs decays [61, 62] forbid only $f \lesssim 300$ GeV. Monojet searches are further suppressed by the small coupling of the Higgs boson to η . This can be also produced in gluon fusion via loops of top quarks, but its coupling to the latter is suppressed with respect to the top Yukawa by order ξ . The charged scalar can be instead produced via gauge interactions. However, the small rate together with the unclear final state containing tops and bottoms, make its discovery challenging at the LHC. Future facilities could probe this channel, though.

Relic density Given the small splitting between the masses of the charged and the neutral components (which is driven by the small gauge induced potential), the DM particles are not expected to annihilate into $\kappa^+ \kappa^-$ final states. As a consequence, the main annihilation channels are $t\bar{t}$ as well as $W^+ W^-$, ZZ and hh . The first channel dominates for small $f \lesssim 1.7$ TeV; see Figure 7, right panel. The main reason is that the annihilation into tops proceeds also via contact interactions (analogous to the ones coming from Equation 2.26), suppressed by $1/f^2$. Other DM interactions, instead, are driven by the Higgs portal. This receives contributions from both the scalar quartic coupling in the potential $\lambda_{H\Phi}$ and from derivative operators like $|H|^2 (\partial^\mu \eta)^2$, appearing in the sigma-model Lagrangian. The ratio

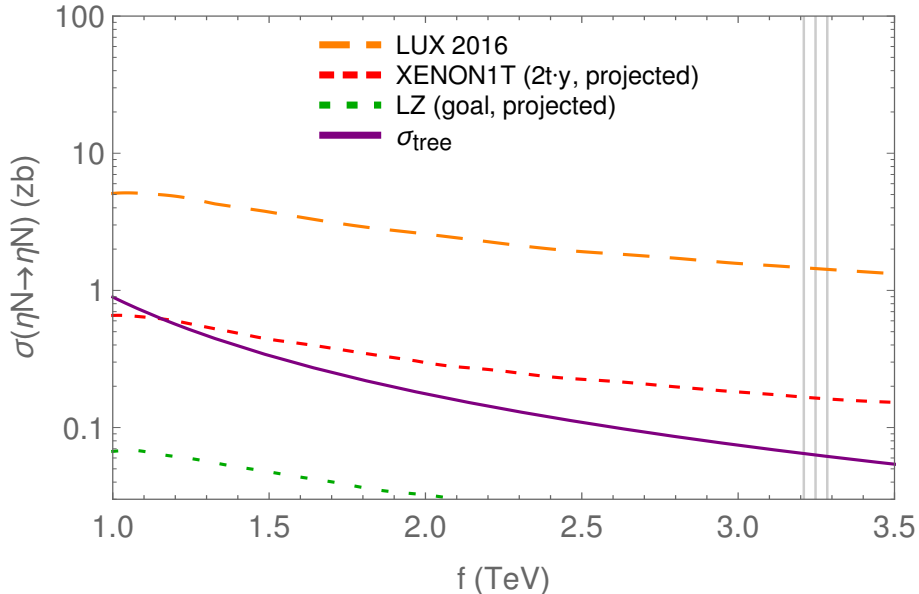


Figure 6. Spin-independent direct detection cross section as a function of the compositeness scale, f , in the singlet DM case. We show the theoretical estimate as a purple continuous line. We also show the current limits (linearly rescaled with the DM abundance) from LUX (dashed orange) [39] and the projected exclusion limits at 95% C.L. for LZ (dashed green) [40] and XENON1T of 2 years in 1 ton (dashed red) [41].

between these two is given by (see Table 1)

$$\frac{1}{2}\lambda_{H\Phi}\frac{f^2}{m_\eta^2} \sim \frac{1}{2}\frac{5}{18}\lambda_H\frac{3f^2}{2\lambda_H f^2} \sim 0.2, \quad (5.4)$$

and therefore the derivative interactions dominate. The main annihilation channel for large values of f is $\eta\eta \rightarrow W^+W^-$, as shown in Figure 7.⁹

Non-perturbative effects, like the Sommerfeld enhancement of the formation of bound states are not relevant. For each value of f we have computed the relic density by just using `micrOMEGAs v3` [65]. The result is shown in Figure 5, alongside the current observational band (as in Figure 1). It turns out that the whole relic abundance can be explained by this model with $f \sim 3$ TeV, for which $m_\eta \sim 900$ GeV. As we will see, current direct and indirect searches do not exclude this possibility. However, future experiments will have the required sensitivity to test this prediction.

Direct searches Contrary to the triplet case, the DM-nucleon interaction proceeds only via the Higgs exchange. As it can be seen in Figure 6, current searches are not constraining enough for this model, but future experiments will definitely probe the whole parameter space.

⁹For an exhaustive discussion of the effects of higher-dimensional operators in related models see for example References [63, 64].

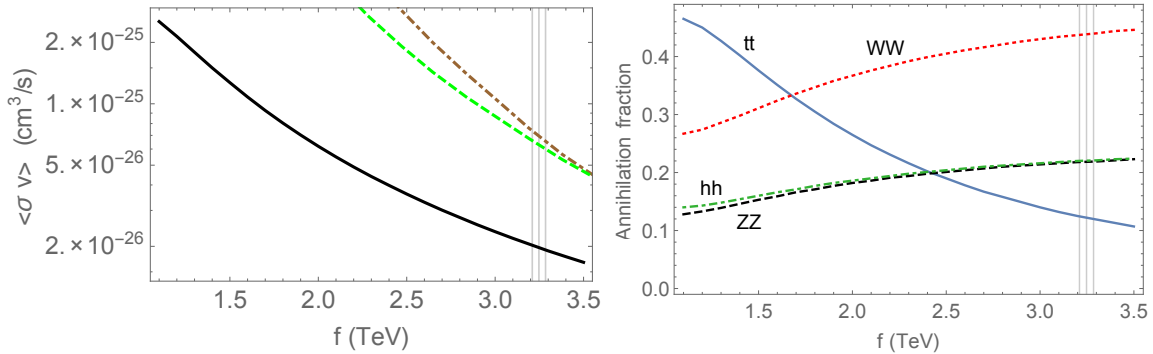


Figure 7. Left panel: The theoretical prediction for the total thermally averaged annihilation rate of DM particles as a function of the compositeness scale, f , for the singlet DM case (black continuous line). We also show the current upper bound (rescaled with the square of the DM abundance) from observations by H.E.S.S. of the Galactic center (assuming an Einasto profile, brown dot-dashed line) [48] and the expected sensitivity of CTA (also with an Einasto profile, green dashed) [42], for $\eta\eta \rightarrow W^+W^-$. Right panel: Annihilation fraction of the main channels for two-body final states; $t\bar{t}$ (blue continuous line), W^+W^- (red dotted), hh (green dot-dashed) and ZZ (black dashed). Other (subdominant) channels are not shown. As in previous plots, the vertical grey lines indicate the range of values of f corresponding to the observed DM abundance at 95% C.L.

Indirect searches The total thermally averaged cross section for DM annihilation as a function of f is shown as a black continuous line in the left panel of Figure 7. As we already mentioned, DM particles annihilate mostly into W^+W^- for sufficiently large values of the compositeness scale, see Figure 7, right panel. For this reason, we also show in the left panel the current upper constraints on $\eta\eta \rightarrow W^+W^-$ from observations of the Galactic center by H.E.S.S. (brown dot-dashed line) [48]. This bound assumes that DM particles annihilate exclusively into W^+W^- (and, as we already discussed, it is the most stringent one for this kind of process). We show as well an estimate of the future sensitivity of CTA for the same process (green dashed line) [42]. The remarks we made in the triplet case concerning this estimate and its comparison to the results of [48] also apply now. Clearly, the prediction of the singlet model for the total cross section appears to be well below the current bound and the future sensitivity for the dominant channel. We conclude that the singlet variant of exceptional composite DM is viable for all the interesting values of f . In particular, for $f \sim 3.25$ TeV, all the DM abundance in the Universe can be accounted for. A substantial improvement in the sensitivity of the next generation of indirect probes will be needed to test this result.

6 Conclusions

The amount of evidence for the existence of DM, which comes from astrophysics and cosmology, is overwhelming. Today, the nature and origin of DM are regarded as one of the biggest problems of contemporary physics. At the same time, a large theoretical effort has been directed towards solving the gauge hierarchy problem. Therefore, the possibility

of establishing a link between the two is a tantalizing idea. This is further supported by the the so-called WIMP miracle. As it is well-known, a WIMP of roughly TeV mass scale can help to explain the inferred DM abundance through the simple freeze-out mechanism.

In spite of the current lack of definite new physics signals at energies of the order of a few TeV, the aforementioned ideas are still widely acknowledged to be excellent reasons to expect a discovery at the LHC in the coming years. Moreover, ongoing direct and indirect detection experiments are also promising windows for the detection of DM particles at the TeV scale, and the sensitivity of these techniques will keep increasing in the near future.

We have worked out a non-minimal CHM containing a Higgs doublet and three additional scalars: two electrically charged and a neutral one. Depending on how the SM gauge interactions break the global symmetry, they can either transform as a whole $SU(2)_L$ triplet or as three singlets. Contrary to the minimal CHM, this setup can explain a large fraction of the observed DM relic abundance. Besides, improvements with respect to elementary extensions of the scalar sector take place, too. Indeed, if the global symmetries are broken mainly in the fermion sector, our setup depends on a single parameter (f) and the external \mathbb{Z}_2 symmetry stabilizing the DM candidate is *predicted* to be exact also after EW symmetry breaking. Were this not the case, the potential would receive sizable contributions from the gauge sector. These would affect this phenomenological study in several ways: The relevant observables would not only depend on f , but also on $\tilde{c}_1 g_\rho$. In order for the neutral scalar not to break the \mathbb{Z}_2 symmetry by taking a VEV, the condition $\tilde{c}_1 g_\rho^2 \gtrsim -2\pi^2 \lambda_H / g^2 \sim -7$ should hold. In any case, for $\tilde{c}_1 \sim g_\rho \sim 1$, the bounds on f would be modified only by a small amount.

Assuming that the breaking of $SO(7)$ is driven mainly by the fermion sector, the fraction of the DM abundance that can be accounted for in this framework depends on how the three additional scalars are arranged. In the case in which they form a triplet, the scale f is constrained to be below ~ 4.25 TeV by H.E.S.S. observations of gamma rays from the Galactic center. These would imply that at most ~ 36 – 46% of the DM abundance can be explained with this model, depending on the shape of the DM radial distribution in the Galactic center. This bound is relatively uncertain, precisely due to our lack of detailed knowledge about the DM profile in the innermost regions of the Galaxy and the modelling of the gamma ray background in that region. Conversely, CMB limits on the DM annihilation cross section are less stringent (though more robust) and allow to account for $\sim 80\%$ of the DM abundance with the triplet model. We stress that these results assume a standard thermal history of the Universe. A different thermal history, which in principle is compatible with the model, could allow to account for a higher percentage of the DM relic abundance in the triplet case, and would change the upper bound on f .

In the case in which the three additional scalars are arranged as three singlets, the neutral one can explain the totality of the DM relic abundance. This is simply because in this case the theoretical prediction for the DM annihilation cross section is well below all the current indirect detection upper bounds.

Future observations of the Galactic center from the Cherenkov telescope CTA are expected to improve the sensitivity on the cross section for several DM annihilations channels. However, for DM annihilating into W^+W^- –which is the common channel of interest

for both of our scenarios– the analysis of [42] indicates that the sensitivity that will be achieved with CTA is not expected to increase significantly beyond the current H.E.S.S. upper bounds in the range of possible DM masses that are relevant for us.

However, a forecast of the CTA sensitivity to monochromatic gamma ray lines (produced by DM annihilation into two photons) [57] indicates that testing most of the relevant range of f for DM in the triplet case will be possible with this channel. Instead, this kind of search is not that useful in the singlet case, since the cross section is much smaller than any current or expected future bound.

Searches for disappearing tracks performed at the LHC require f to be larger than 650 GeV in the triplet case, while Higgs measurements rise this bound up to $f \sim 800$ GeV in either scenario. Future facilities could improve this bound by almost a factor of 2. Likewise, current direct searches are not constraining, while future experiments would be able to probe all allowed values of f .

Clearly, the different searches are rather complementary. Besides, we have set a robust upper limit on the compositeness scale. In generic CHMs, the latter can be obtained only if (less definite) fine tuning arguments are advocated. Note also that this bound translates into an upper limit on the mass, M , of the fermionic resonances (roughly speaking, $M \lesssim f$). Consequently, a comment on the implications of our findings for the phenomenology of heavy vector-like fermions is necessary. In particular, let us focus on top-like resonances, for these are the ones whose interaction with the SM sector is stronger. These states can be produced in pairs in proton-proton collisions. The production cross section is mainly driven by QCD interactions, and hence model independent. Experimental limits on the mass of these resonances rely only on their branching ratio into the different lighter particles. Searches performed in the LHC Run I constrain their masses to be smaller than ~ 900 GeV (see for example Reference [66]). More recent analyses [67] have pushed this limit just above the TeV. In any case, the reach of current analyses is still far from the largest mass allowed by DM experiments. In this respect, our model –and also generic non-minimal CHMs with EW-charged DM candidates–, favours a hadronic high-energy collider as physics case for a future facility. On top of that, all current studies consider that the new fermions decay *only* into SM particles, not into other light scalars expected in non-minimal CHMs. So, if these setups are to be considered seriously, and they should, new dedicated searches need to be developed straight away (see References [68–73] for works in this direction).

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A Representation theory of $SO(7)$ and G_2

Let us define the following 8×8 matrices [9, 74]:

$$\begin{aligned} \gamma_1 &= i\sigma_2 \otimes i\sigma_2 \otimes i\sigma_2, & \gamma_2 &= \sigma_1 \otimes i\sigma_2 \otimes 1, & \gamma_3 &= i\sigma_2 \otimes 1 \otimes \sigma_1, & \gamma_4 &= -i\sigma_2 \otimes 1 \otimes \sigma_3, \\ \gamma_5 &= 1 \otimes \sigma_1 \otimes i\sigma_2, & \gamma_6 &= -\sigma_3 \otimes i\sigma_2 \otimes 1, & \gamma_7 &= -1 \otimes \sigma_3 \otimes i\sigma_2 \end{aligned} \quad (\text{A.1})$$

An 8-dimensional representation of $SO(7)$ is then given by the operators

$$J_{mn} = -J_{nm} = -[\gamma_m, \gamma_n]/4, \quad m, n = 1, \dots, 7. \quad (\text{A.2})$$

In this paper we consider instead an equivalent representation obtained by rotating J_{mn} (*i.e.* $J_{mn} \rightarrow S^\dagger J_{mn} S$) with the following S matrix:

$$S = \frac{1}{2} \begin{pmatrix} 0 & 1 & 1 & -1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & 1 & -1 & -1 & 0 & 0 & -1 & 0 \\ -1 & 0 & 0 & 0 & -1 & 1 & 0 & 1 \\ 0 & 1 & -1 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 & -1 & 1 & 0 & -1 \\ 0 & 1 & 1 & 1 & 0 & 0 & -1 & 0 \\ -1 & 0 & 0 & 0 & 1 & 1 & 0 & -1 \end{pmatrix}. \quad (\text{A.3})$$

The Lie algebra of $G_2 \subset SO(7)$ and the coset space are expanded, respectively, by the following 14 generators, F_i, M_i , and the 7 generators, N_i [9, 75]:

$$\begin{aligned} F_1 &= -\frac{i}{2}(J_{24} - J_{51}), & M_1 &= +\frac{i}{\sqrt{12}}(J_{24} + J_{51} - 2J_{73}), & N_1 &= \frac{i}{\sqrt{6}}(J_{24} + J_{51} + J_{73}), \\ F_2 &= +\frac{i}{2}(J_{54} - J_{12}), & M_2 &= -\frac{i}{\sqrt{12}}(J_{54} + J_{12} - 2J_{67}), & N_2 &= \frac{i}{\sqrt{6}}(J_{54} + J_{12} + J_{67}), \\ F_3 &= -\frac{i}{2}(J_{14} - J_{25}), & M_3 &= +\frac{i}{\sqrt{12}}(J_{14} + J_{25} - 2J_{36}), & N_3 &= \frac{i}{\sqrt{6}}(J_{14} + J_{25} + J_{36}), \\ F_4 &= -\frac{i}{2}(J_{16} - J_{43}), & M_4 &= +\frac{i}{\sqrt{12}}(J_{16} + J_{43} - 2J_{72}), & N_4 &= \frac{i}{\sqrt{6}}(J_{16} + J_{43} + J_{72}), \\ F_5 &= -\frac{i}{2}(J_{46} - J_{31}), & M_5 &= +\frac{i}{\sqrt{12}}(J_{46} + J_{31} - 2J_{57}), & N_5 &= \frac{i}{\sqrt{6}}(J_{46} + J_{31} + J_{57}), \\ F_6 &= -\frac{i}{2}(J_{35} - J_{62}), & M_6 &= +\frac{i}{\sqrt{12}}(J_{35} + J_{62} - 2J_{71}), & N_6 &= \frac{i}{\sqrt{6}}(J_{35} + J_{62} + J_{71}), \\ F_7 &= +\frac{i}{2}(J_{65} - J_{23}), & M_7 &= -\frac{i}{\sqrt{12}}(J_{65} + J_{23} - 2J_{47}), & N_7 &= \frac{i}{\sqrt{6}}(J_{65} + J_{23} + J_{47}). \end{aligned} \quad (\text{A.4})$$

$\{F_1, F_2, F_3\}$ and $\sqrt{3}\{M_1, M_2, M_3\}$ span two separate copies of $SU(2)$. In this particular basis, the vacuum (*i.e.* the vector that it is annihilated only by the generators of G_2)

adopts the form $\Sigma_0 = (0, 0, 0, 0, 0, 0, 0, f)^T$. The \mathbb{Z}_2 -even spurion Δ_q^α for the triplet case is given by

$$\Delta_q^1 = \frac{1}{2} \begin{pmatrix} 0 \\ 0 \\ 0 \\ \mathbf{0}_{7 \times 7} \\ 0 \\ -i \\ 1 \\ 0 \end{pmatrix}, \quad \Delta_q^2 = \frac{1}{2} \begin{pmatrix} 0 \\ 0 \\ 0 \\ \mathbf{0}_{7 \times 7} \\ i \\ 1 \\ 0 \\ 0 \end{pmatrix}. \quad (\text{A.5})$$

In the singlet case, Δ_q^1 is changed by Δ_q^{1*} whereas Δ_q^2 remains unchanged. In this case, the spurion for Δ_b reads

$$\Delta_b = \frac{1}{4\sqrt{3}} \begin{pmatrix} 0 & 0 & -i & 0 & 0 & 0 & 0 & 3 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 3i \\ i & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -i & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & -1 & i & 0 \\ 0 & 0 & 0 & i & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & -i & 0 & 0 & 0 \\ -3 & -3i & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}. \quad (\text{A.6})$$

B $SU(2)_L \times U(1)_Y$ quantum numbers of the pNGBs

To recognize which combination of pNGBs spans the $\mathbf{2}_{1/2}$ or the $\mathbf{3}_0$ of the EW group it is useful to remember that, if the broken generators X^a transform as

$$\exp(-\alpha^i Y_i) X^a \exp(\alpha^j Y_j) = R_{ab} X^a \quad (\text{B.1})$$

under an element $h = \exp(\alpha_i Y^i)$ of the unbroken group G_2 , the pNGBs accompanying them inside $U = \exp(i\Pi^a N^a/f)$ transform with the transposed matrix, *i.e.*,

$$\Pi^a \rightarrow R_{ab}^T \Pi^b. \quad (\text{B.2})$$

For simplicity, let us focus first on the triplet case. If we define

$$N^\pm \equiv \frac{N^1 \pm iN^2}{\sqrt{2}}, \quad N^0 \equiv -N^3, \quad \text{and} \quad N_\Phi = \begin{pmatrix} N^+ \\ N^0 \\ -N^- \end{pmatrix}, \quad (\text{B.3})$$

and use their commutations relations, we get

$$\sqrt{3}[M^i, N_\Phi] = -t^i N_\Phi, \quad [F^3, T_\Phi] = -0N_\Phi, \quad (\text{B.4})$$

where t^i , $i = 1, 2, 3$, are the three-dimensional $SU(2)$ representation given in (2.9). Therefore,

$$\begin{aligned} e^{-i\alpha_j\sqrt{3}M^j} N_\Phi e^{i\alpha_k\sqrt{3}M^k} &= N_\Phi - i\alpha_j\sqrt{3}[M^j, N_\Phi] + \dots \\ &= (1 + i\alpha_j t^j) N_\Phi + \dots = e^{i\alpha_j t^j} N_\Phi \end{aligned} \quad (\text{B.5})$$

and

$$\Phi^* \rightarrow \left(e^{i\alpha_j t^j} \right)^T \Phi^* \Rightarrow \Phi \rightarrow e^{-i\alpha_j t^j} \Phi, \quad (\text{B.6})$$

where we have defined

$$\Phi = \begin{pmatrix} \kappa^+ \\ -\eta \\ -\kappa^- \end{pmatrix}, \quad \text{and} \quad \kappa^\pm = \frac{\kappa^1 \pm \kappa^2}{\sqrt{2}}. \quad (\text{B.7})$$

This means that Φ transforms properly as a hyperchargeless $SU(2)$ triplet. Analogously, if we define

$$N_H = \frac{1}{\sqrt{2}} \begin{pmatrix} N^3 - iN^4 \\ N^6 + iN^7 \end{pmatrix} \quad (\text{B.8})$$

and use the commutation relations we get

$$\sqrt{3}[M^i, N_H] = -\frac{1}{2}\sigma^i N_H, \quad [F^3, N_H] = -\frac{1}{2}N_H, \quad (\text{B.9})$$

which implies that

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} h^1 - ih^2 \\ h^3 + ih^4 \end{pmatrix} \quad (\text{B.10})$$

transforms as an $SU(2)$ doublet with $Y = 1/2$ hypercharge. In the singlet case, this combination can be taken

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} -h^1 + ih^2 \\ h^3 - ih^4 \end{pmatrix}. \quad (\text{B.11})$$

C The case of composite leptons

An interesting possibility that has been explored recently is that leptons could play a role in EWSB when they transform in non minimal irreps of the global group, see *e.g.* References [76–78]. (By non-minimal irreps we mean that they can provide more than one independent invariant under the unbroken group at leading order in the spurion expansion, like *e.g.* the **14** in $SO(5)/SO(4)$ or the **35** in $SO(7)/G_2$.) The rationale is that, when the quark sector transforms in smaller representations of the Goldstone symmetry (like the spinorial, the fundamental, the adjoint, ...), even a moderate degree of compositeness in one of the lepton chiralities can have a sizable impact in the Higgs potential. This is

Parameter	μ_H^2	λ_Φ	$\lambda_{H\Phi}$
Value	$-v^2\lambda_H$	$\frac{16}{9}\lambda_H\left(1 - \frac{2}{3}\frac{v^2}{f^2}\right) - \frac{2}{3}\frac{\mu_\Phi^2}{f^2}$	$-\frac{4}{3}\lambda_H\left(1 - \frac{11}{9}\frac{v^2}{f^2}\right) - \frac{1}{3}\frac{\mu_\Phi^2}{f^2}$

Table 2. Values of the different parameters of the renormalizable scalar potential as a function of f , to order $\mathcal{O}(v^2/f^2)$. $v \sim 246$ GeV and $\lambda_H \sim 0.13$ stand for the SM EW VEV and the Higgs quartic coupling, respectively.

due to the fact that the leading lepton contribution to the Higgs quartic coupling scales in this case with $|\lambda_\ell|^2/g_*^2$, whereas the top one goes with $|\lambda_q|^4/g_*^4$, $|\lambda_q|^2|\lambda_\ell|^2/g_*^4$ or $|\lambda_t|^4/g_*^4$. Therefore, a relatively smaller value of λ_ℓ/g_* arising from the charged lepton sector can provide a comparable effect to the one coming from the top quark.

Moreover, the fact that all different lepton generations could be partially composite, could enhance the lepton contribution by a factor $N_{\text{gen}} \sim 3$, compensating the color factor $N_c = 3$ present in the top case. Indeed, the recent hints of violation of lepton flavor universality observed by LHCb and CMS in R_K and R_K^* [79, 80] seem to provide a further motivation to these scenarios, as discussed *e.g.* in [77].

In what follows, we will briefly discuss how a similar setup works in the case of $SO(7)/G_2$ and its impact on DM. We assume that \mathcal{O}_q^j and \mathcal{O}_u^j transform in the $\mathbf{8}_{2/3}$ and the $\mathbf{1}_{2/3}$ of $SO(7) \times U(1)_X$, respectively, whereas the composite operators mixing with the left-handed lepton doublets and the right-handed charged singlets, \mathcal{O}_L^j and \mathcal{O}_ℓ^j , transform respectively in the $\mathbf{1}_{-1}$ and $\mathbf{35}_{-1}$ of the same group. Then, the scalar potential can be written as

$$V(\Pi) \approx m_*^2 f^2 \frac{1}{16\pi^2} \left[N_c \left(\frac{|\lambda_q|}{g_*} \right)^2 c_1 V_1(\Pi) + \sum_{j=1}^3 \left(\frac{|\lambda_\ell|_{jj}}{g_*} \right)^2 [c_{2,j} V_2(\Pi) + c_{3,j} V_3(\Pi)] \right], \quad (\text{C.1})$$

with

$$\sum_\alpha |(\Delta_{qD}^\alpha)_8|^2 \sim V_1(\Pi) = \frac{|H|^2}{\hat{\Pi}^2} \sin^2 \left(\frac{\hat{\Pi}}{f} \right), \quad (\text{C.2})$$

$$|(\Delta_{\ell D})_{88}|^2 \sim V_2(\Pi) = \frac{8}{147} \frac{1}{\hat{\Pi}^4} \sin^4 \left(\frac{\hat{\Pi}}{f} \right) (3|H|^2 - 2|\Phi|^2)^2, \quad (\text{C.3})$$

$$\sum_{i=1}^7 |(\Delta_{\ell D})_{i8}|^2 \sim V_3(\Pi) = \frac{1}{21} \frac{1}{\hat{\Pi}^4} \sin^2 \left(\frac{\hat{\Pi}}{f} \right) \left[2(3|H|^2 - 2|\Phi|^2)^2 \cos^2 \left(\frac{\hat{\Pi}}{f} \right) + 49|H|^2|\Phi|^2 \right], \quad (\text{C.4})$$

where we have defined the dressed spurions $\Delta_{qD}^\alpha = U^{-1}\Delta_q^\alpha$, $\alpha = 1, 2$, and $\Delta_{\ell D} = U^{-1}\Delta_\ell U$

as usual, with¹⁰

$$\Delta_q^1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ -i \\ 1 \\ 0 \end{pmatrix}, \quad \Delta_q^2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ 0 \\ 0 \\ i \\ 1 \\ 0 \\ 0 \\ 0 \end{pmatrix}, \quad \Delta_\ell = \frac{1}{2} \sqrt{\frac{3}{7}} \text{diag} \begin{pmatrix} 4/3 \\ 4/3 \\ 4/3 \\ -1 \\ -1 \\ -1 \\ -1 \\ 0 \end{pmatrix}. \quad (\text{C.5})$$

The parameters $c_1, c_{2,j}$ and $c_{3,j}$, with $j = 1, 2, 3$, running over the three lepton generations, that appear in the scalar potential are order one dimensionless numbers. Note, however, that $c_{2,j}$ and $c_{3,j}$ always enter in the same linear combination. So, effectively, we are left with only three independent unknowns (the coefficients of $V_1(\Pi), V_2(\Pi)$ and $V_3(\Pi)$) which can be traded at the renormalizable level by the Higgs VEV v , the Higgs quartic λ_H and the mass parameter of the scalar triplet μ_Φ^2 , see Table 2 and Equation 2.24. The mass of the triplet in the EW phase is given by

$$m_\Phi^2 = \mu_\Phi^2 + \lambda_{H\Phi} v^2 = \mu_\Phi^2 \left[1 - \frac{v^2}{3f^2} + \mathcal{O}\left(\frac{v^4}{f^4}\right) \right] - \frac{4}{3} \lambda_H v^2 \left[1 - \frac{11}{9} \frac{v^2}{f^2} + \mathcal{O}\left(\frac{v^4}{f^4}\right) \right]. \quad (\text{C.6})$$

Since $\mu_\Phi^2 \sim f^2 \gg \lambda_H v^2$, the triplet does not take a VEV provided the underlying UV dynamics allows for a positive μ_Φ^2 (the same holds for the singlet if we weakly gauge the other $SU(2)$ as discussed in Section 5, since the main contribution to the potential is still given by Equation 2.24). The main difference with respect to the scenarios explored before is that the relationship between μ_Φ and f is in principle not known. However, the same phenomenological study could be done having as an extra variable the ratio μ_Φ/f , what we leave for a future work.

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¹⁰We are thinking of the triplet case. In the singlet case one has to change Δ_q^1 by Δ_q^{1*} , with the rest of the spurions remaining the same.

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