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Object-level Impedance Control for Dexterous Manipulation with Contact Uncertainties using an LMI-based Approach

A. Caldas¹, A. Micaelli¹, M. Grossard¹, M. Makarov², P. Rodriguez-Ayerbe², D. Dumur²

Abstract—This paper presents a new control scheme for dexterous manipulation of an object by a multifingered hand. The effects of the uncertainties on the contact orientation and location are investigated and taken into account in the control design, allowing to manipulate the object robustly. The control law has three main objectives: (i) ensuring the motion control of the object, (ii) satisfying the constraints of the manipulation system, and (iii) being robust to the uncertainties on the contact point. The proposed control is based on a state feedback architecture with robust pole placement by an LMI approach. The controller is designed offline and can be related to an object-level impedance controller. The constraints of the manipulation system, e.g. the friction constraints, are taken into account with an additional control action, based on an online LMI evaluation. Simulation results are presented and demonstrate that the proposed control law ensures the three main objectives.

I. INTRODUCTION

In the last few decades, robotics has evolved into ever more complex systems working on ever more complex manipulation tasks. From these emerging needs, roboticists have proposed new mechanical designs and multifingered hands have been developed. Various strategies have been proposed to control these mechanical systems and the field of dexterous manipulation is still an active field of research [1]–[3].

One difficulty in dexterous manipulation tasks is to deal with uncertainties. In the present state of technology, a perfect geometric representation of a scene is very difficult to achieve and needs various sensor feedbacks [4]. For instance, tactile and force sensors with a high 3D resolution are still very expensive and difficult to use in practice due to mechanical integration problems. Therefore, to better comply with practical experimental conditions, control laws for dexterous manipulation should include considerations about geometric uncertainties on the contact point. Two different approaches have been proposed in the literature to address this problem: identifying the contact point location or taking into account the uncertainties in the control scheme.

In the first approach, the contact point location can be deduced from the kinematic of the robotic hand by observing

the constrained motion of fingers [5]. With geometric considerations and using only joint angles and torque sensors, an algorithm was proposed to gather contact data while interacting with an unknown object [6]. Others methods use the self-posture changeability to determine the contact points [7]. Most of these methods are based on assumptions about the geometry of the system, which should be perfectly known.

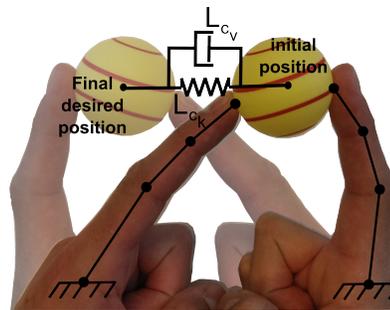


Fig. 1. Impedance behavior at the object-level.

In the second approach, the uncertainties are explicitly defined in the system modeling, and a robust controller can be designed. Just a few studies have considered this framework. In [8] and [9], force and gravity regressors are proposed to cope with Jacobian uncertainties, and stability is studied with a Lyapunov function. An adaptive force/position control for a robot finger under surface kinematic uncertainties is proposed in [10]. However, the proposed controller assumes that a force/tactile sensor is used to provide measurements of normal forces.

Many problems dealing with robust control theory can be reduced to standard convex optimization problems involving *Linear Matrix Inequalities* (LMIs) [11]. Ensuring force-closure grasping can be formulated as an optimization problem with LMIs defining the friction constraints [12] and the grasp quality can be evaluated with LMIs adding bounded contact forces [13]. However, to the best of our knowledge, LMIs have not yet been employed for controller design in the dexterous manipulation field, and more specifically when contact uncertainties are taken into account, even though it is an interesting tool to develop robust control laws for robotic hands.

The aim of the present paper is to propose a new control strategy for dexterous manipulation without force/tactile sensor and dealing with uncertainties on the contact point location when the geometry of the system is not supposed perfectly known. The controller can be decomposed into two

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parts: (i) a state-feedback with pole placement, and (ii) an adaptive control action ensuring the constraints, computed via an LMI optimization. The proposed strategy is based on a linearized model and provides a framework to easily calculate an impedance controller under uncertainties (Fig. 1), with three main objectives: motion control, constraint validation (friction cone, unilaterality and boundaries of the contact forces), and robustness to contact uncertainties.

The paper is organized as follows: in section II, a state-space representation of the system is presented. Section III describes the proposed control scheme. Numerical examples and simulations of the controller are presented in section IV. Section V gives the conclusions and perspectives.

II. MULTIFINGERED HAND REPRESENTATION

This part presents the multifingered hand model, based on the screw theory [14], and introduces useful notations.

A. State-Space Formulation

The multifingered hand model is obtained by combining the dynamics of the fingers and the object:

$$\begin{cases} M_h(q)\ddot{q} + C_h(q, \dot{q})\dot{q} + N_h(q, \dot{q}) - J_h(q, x_o)^T f_c = \tau \\ M_o(x_o)\ddot{x}_o + C_o(x_o, \dot{x}_o)\dot{x}_o + N_o(x_o, \dot{x}_o) + Gf_c = 0 \end{cases} \quad (1)$$

- For the first equation, $q = [q_{f_1} \ q_{f_2} \ \dots \ q_{f_k}]^T \in \mathbb{R}^{n_q}$ is the actuated joint position vector for the k fingers of the hand, $q_{f_i} \in \mathbb{R}^{n_{f_i}}$ being the actuated joint positions of the finger i , $\tau \in \mathbb{R}^{n_q}$ is the corresponding torque vector, and M_h , C_h and N_h are respectively the stacked inertia matrix, Coriolis, centrifugal and viscous friction matrix and gravity vector of the k fingers of the hand, $J_h \in \mathbb{R}^{n_c \times n_q}$ the hand Jacobian (with n_c the dimension of the contact frame), and $f_c \in \mathbb{R}^{n_c}$ the contact forces applied on the object.
- For the second equation, $x_o \in \mathbb{R}^{n_o}$ a local coordinate of the object, with $n_o = 6$ in 3D ($n_o = 3$ in 2D) the dimension of the object coordinate, $M_o \in \mathbb{R}^{n_o \times n_o}$ the inertia matrix, $C_o \in \mathbb{R}^{n_o \times n_o}$ the Coriolis and centrifugal matrix, $N_o \in \mathbb{R}^{n_o}$ the gravity vector, $G \in \mathbb{R}^{n_o \times n_c}$ the grasp map relating the contact frames to the object frame.

The grasping of the object by the fingers is defined by the following constraint:

$$J_h(q, x_o)\dot{q} = G^T \dot{x}_o \quad (2)$$

According to (1)-(2), the system motion can be formulated at the object level as follows (see [14] for more details):

$$M(q, x_o)\ddot{x}_o + C(q, x_o, \dot{q}, \dot{x}_o)\dot{x}_o + N(q, x_o, \dot{q}, \dot{x}_o) = GJ_h^{-T} \tau \quad (3)$$

with:

$$M = M_o + GJ_h^{-T} M_h J_h^{-1} G^T \quad (4)$$

$$C = C_o + GJ_h^{-T} C_h J_h^{-1} G^T + GJ_h^{-T} M_h \frac{d}{dt} (J_h^{-1} G^T) \quad (5)$$

$$N = N_o + GJ_h^{-T} N_h \quad (6)$$

In the following, the dependency on q , \dot{q} , x_o , \dot{x}_o is dropped in the notations.

(2)-(6) are valid under the following assumptions:

- A1 The system is not redundant, i.e. there is no internal movement of the fingers for a fixed position of the object. In this case, the hand Jacobian J_h is square and invertible. This assumption could be relaxed with a model taking into account the joint redundancy [14]-[15].
- A2 The contact points are fixed, which imply that G is constant. This assumption is naturally made with (2), and will be relaxed later by taking into consideration the uncertainties on the contact point location.
- A3 The contact forces remain in the friction cone. This constraint, which depends on the friction coefficient μ , can be linearized [16] and expressed by the inequality:

$$\Lambda f_c < \beta \quad (7)$$

with $\Lambda \in \mathbb{R}^{n_{constraints} \times n_c}$ and $\beta \in \mathbb{R}^{n_{constraints}}$, and $n_{constraints}$ the number of constraints. This requirement must be satisfied by the control law.

- A4 The grasp is manipulable, i.e. the desired motion can be generated by the fingers. In this case, the hand Jacobian is full row rank [14].
- A5 The influence of gravity N is negligible or compensated.

The linearization of (3) around an equilibrium point $[x_{o_{eq}} \ \mathbb{0}_{n_o}]^T$ leads to an LTI state-space representation:

$$\frac{d}{dt} \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} = \begin{bmatrix} \mathbb{0}_{n_o \times n_o} & \mathbb{I}_{n_o \times n_o} \\ \mathbb{0}_{n_o \times n_o} & -M_{eq}^{-1} C_{eq} \end{bmatrix} \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} + \begin{bmatrix} \mathbb{0}_{n_o \times n_q} \\ M_{eq}^{-1} G J_{heq}^{-T} \end{bmatrix} \tau \quad (8)$$

where constant matrices M_{eq} , C_{eq} and J_{heq} define respectively the inertia matrix, Coriolis and centrifugal matrix, and the hand Jacobian calculated at the equilibrium point. In the remaining of the article, the model-based control design will be related to (8).

Furthermore, the contact forces can be expressed as a function of state $[x_o \ \dot{x}_o]^T$, by reformulating the object dynamics according to the previous assumptions:

$$M_o \ddot{x}_o + C_o \dot{x}_o + Gf_c = 0 \Leftrightarrow Gf_c = \begin{bmatrix} -C_o & -M_o \end{bmatrix} \begin{bmatrix} \dot{x}_o \\ \ddot{x}_o \end{bmatrix} \quad (9)$$

Using (8) and applying the pseudo-inverse of G , f_c can be isolated in (9):

$$f_c = G^+ \begin{bmatrix} \mathbb{0}_{n_o \times n_o} & -C_o + M_o M_{eq}^{-1} C_{eq} \end{bmatrix} \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} - G^+ M_o M_{eq}^{-1} G J_{heq}^{-T} \tau + N_G \lambda \quad (10)$$

with $(\cdot)^+$ defining the pseudo-inverse, which is not unique for the grasp map G . The term $N_G \lambda \in Ker(G)$, with N_G a base of the null space of G , is introduced, defining the non-uniqueness of the pseudo-inverse, and introducing a new degree of freedom λ , that will be used in the control law, and corresponding to the magnitude of the internal forces.

B. Model of the Contact Uncertainties

Uncertainties on the contact point are due to modeling errors that can be of three types:

- Error on the contact surface (Fig. 2.a). This error occurs when the geometry of the object is not well known or is simplified (for calculation purposes). The contact frame is affected by an orientation uncertainty that would affect the grasp map G .
- Error on the object location (Fig. 2.b). This error occurs when the object position is uncertainly known, possibly due to a non valid initialization or a badly calibrated camera when visual servoing is used. The object frame considered in the control algorithm is affected by an offset compared to the real object frame. The grasp map G is affected by this error.
- Fixed contact point assumption error, e.g. when rolling or soft finger contact occurs. In the previous section, the model assumes a fixed contact point. If in practice the contact is ensured by a surface or is subject to rolling, the equivalent contact point is unknown. This error also affects the grasp map G .

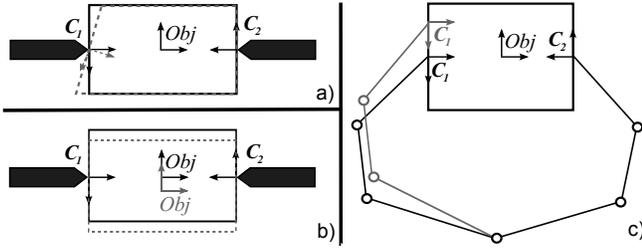


Fig. 2. Origins of uncertainties.

Let us note that other modeling errors can occur, e.g. error on the surface type, implying an uncertainty on the friction coefficient μ , or error on the hand Jacobian J_h (Fig. 2.c), that can affect the grasp map G if the considered contact point is deduced from the inaccurate hand models. These errors are not taken into consideration in this paper, but the robustness of the controller to hand Jacobian uncertainties will be investigated in the examples.

The effects of the geometric uncertainties on the contact point are summarized by the following notation of the grasp map G , which can be defined as a function of uncertainties:

$$G = G(\delta) \quad (11)$$

with $\delta \in P_\delta$ the vector of uncertainties. δ can be structured as a translation and/or a rotation error, linear or nonlinear, with P_δ being the set of all the uncertainties considered in the system (linear dependence of G on δ is investigated in [17]).

III. CONTROL SCHEME

A. General Form

The control inputs of the proposed state-space representation (8) are the joint torques. These signals can be expressed at the object level, allowing a direct connection between the

object position error and the joint torques expressed at the object level. The transform between the object and the joint spaces depends on the hand Jacobian J_h and the grasp map G , and can be expressed by:

$$\tau = \underbrace{\hat{J}_{heq}^T G^+}_{\tau_{motion}} u + \underbrace{\hat{J}_{heq}^T N_G}_{\tau_{internal}} \lambda \quad (12)$$

where \hat{J}_{heq} is the estimate of the hand Jacobian at the equilibrium point, and u the control input at the object level.

The transform J_{heq} links the joint level to the contact level and the transform G links the contact level to the object level. The first contribution τ_{motion} generates the object motion, expressed at the object level, and the second contribution $\tau_{internal}$ generates internal forces, which do not generate movement in the nominal case, but introduce an additional degree of freedom to fulfill the constraints. This decomposition of the torque vector is well known and was proposed since the 1980s [16]. While the proposed controller relies on this classical decomposition with a straightforward physical interpretation, the novelty of our contribution consists in the calculation of the signals u and λ , which takes into account uncertainties with an LMI approach.

Injecting (12) in (8) leads to:

$$\begin{aligned} \frac{d}{dt} \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} &= \begin{bmatrix} \mathbb{O}_{n_o \times n_o} & \mathbb{I}_{n_o \times n_o} \\ \mathbb{O}_{n_o \times n_o} & -M_{eq}^{-1} C_{eq} \end{bmatrix} \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} \\ &+ \begin{bmatrix} \mathbb{O}_{n_o \times n_q} \\ M_{eq}^{-1} G J_{heq}^{-T} \end{bmatrix} \hat{J}_{heq}^T G^+ u + \begin{bmatrix} \mathbb{O}_{n_o \times n_q} \\ M_{eq}^{-1} G J_{heq}^{-T} \end{bmatrix} \hat{J}_{heq}^T N_G \lambda \end{aligned} \quad (13)$$

If the estimation of the hand Jacobian is perfect, i.e. $\hat{J}_{heq} = J_{heq}$, the model becomes:

$$\frac{d}{dt} \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} = \underbrace{\begin{bmatrix} \mathbb{O}_{n_o \times n_o} & \mathbb{I}_{n_o \times n_o} \\ \mathbb{O}_{n_o \times n_o} & -M_{eq}^{-1} C_{eq} \end{bmatrix}}_A \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} + \underbrace{\begin{bmatrix} \mathbb{O}_{n_o \times n_o} \\ M_{eq}^{-1} \end{bmatrix}}_B u \quad (14)$$

In this specific case, the object motion is only affected by the control input u .

Furthermore, combining (10) and (12) with a perfect estimation of the hand Jacobian yields:

$$\begin{aligned} f_c &= G^+ [\mathbb{O}_{n_o \times n_o} \quad -C_o + M_o M_{eq}^{-1} C_{eq}] \begin{bmatrix} x_o \\ \dot{x}_o \end{bmatrix} \\ &- G^+ M_o M_{eq}^{-1} u + N_G \lambda \end{aligned} \quad (15)$$

Thus, the contact forces can be written as:

$$f_c = C_f x + B_f u + N_G \lambda \quad (16)$$

with $x = [x_o \quad \dot{x}_o]^T$ the state vector in (14).

Equations (14) and (16) will be used for the design of the robust control law.

B. Objectives of the Control Law

With respect to the proposed control input (12), the control objectives are:

- Motion tracking of the object. This objective is related to the control input u which is defined explicitly in the

D. Internal Force Control

The previous section provides a solution to the problem of motion control of the object, but the control law is relevant only if the constraints on the contact points are satisfied, particularly:

- C1 The contact points are fixed and no rolling neither sliding are allowed. This condition will be relaxed in the next section, by taking into account the uncertainties in the contact points.
- C2 The contact forces must remain in the friction cone.
- C3 The contact forces are limited according to joint torque minimal τ_{min} and maximal τ_{max} limits.

These constraints can be satisfied by resolving an LMI problem on the contact forces.

The joint torque limits can be expressed at the contact level:

$$\tau_{min} < \tau < \tau_{max} \quad (26)$$

Introducing (1) and applying the assumptions specified in II-A:

$$\tau_{min} < M_h \ddot{q} + C_h \dot{q} - J_h^T f_c < \tau_{max} \quad (27)$$

The following inequalities are deduced:

$$\begin{cases} J_h^T f_c + (-M_h \ddot{q} - C_h \dot{q} + \tau_{min}) < 0 \\ -J_h^T f_c + (M_h \ddot{q} + C_h \dot{q} - \tau_{max}) < 0 \end{cases} \quad (28)$$

The expression of the contact forces (16) is introduced in the constraints (28) and (7):

$$\begin{cases} \Lambda N_G \lambda + \Lambda(C_f x + B_f u) - \beta < 0 \\ J_h^T N_G \lambda + J_h^T(C_f x + B_f u) + \beta_2(q) < 0 \\ -J_h^T N_G \lambda - J_h^T(C_f x + B_f u) + \beta_2'(q) < 0 \end{cases} \quad (29)$$

with $\beta_2(q) = -M_h \ddot{q} - C_h \dot{q} + \tau_{min}$ and $\beta_2'(q) = M_h \ddot{q} + C_h \dot{q} - \tau_{max}$. The degree of freedom λ allows one to fulfill these three constraints depending on the current state x , joint angles q and control signals u . This problem can be solved by an online optimization with LMI constraints. The three constraints (29) can be formulated under an LMI form, by transforming the column of the matrix ΛN_G , $J_h^T N_G$ and $-J_h^T N_G$ and diagonalizing the vectors $\Lambda(C_f x + B_f u) - \beta$, $J_h^T(C_f x + B_f u) + \beta_2(q)$ and $-J_h^T(C_f x + B_f u) + \beta_2'(q)$ (see [13] for more details).

Furthermore, robustness to external wrench disturbances applied on the object can be ensured by introducing an offset on λ .

E. Algorithm Coping with Uncertainties

If uncertainties affected the system linearly, the classical method could have been to write it in an Linear Parametric Varying (LPV) form. Here, the uncertainties on the contact points affect the grasp map, and the system representation (14) is not linear according to the matrix G , thus it is not straightforward to formulate the model as a LPV system. Instead, the following approach is used.

A set P_Σ of all the possible state-space representations $\Sigma = (A, B, C, D)$ depending on the uncertainties is defined:

$$\Sigma \in P_\Sigma \Leftrightarrow \{\forall \delta \in P_\delta, \Sigma := \{\dot{x} = A(\delta)x + B(\delta)u\}\} \quad (30)$$

Knowing that the uncertainties do not affect linearly this set, no assumption can be made about the convexity of P_Σ . The uncertainties can be taken into account by discretizing the polytope P_δ , implying a discretization of P_Σ , and then test the LMI problems from III-C and III-D for each system resulting from the discretization of P_Σ (this set of systems will be called thereafter *discretized- P_Σ systems*).

For the motion control problem, and according to the motion control objectives defined in III-B, the proposed algorithm consists in minimizing the trace of P , which will maximize the eigenvalues real part of the closed-loop, and result in the fastest response. The problem is formulated as follows:

$$\begin{cases} \min_{Y, P} Tr(P) \\ \text{s.t. for all } \delta_i \in P_\delta \\ (19) - (21) \text{ are satisfied} \\ \text{end for} \end{cases} \quad (31)$$

Others criteria can be found in the literature [19], e.g. improving the robustness according to unstructured uncertainties.

The resulting static gain L_c ensures the stability of every *discretized- P_Σ systems*. If the sampling step of P_Σ is small enough, the motion tracking is guaranteed even in case of uncertain contact point location, rolling contact or soft finger contact.

The internal forces are also deduced by solving the LMI problems deduced from the constraints (29) for every *discretized- P_Σ systems*. The overall strategy is depicted in Fig. 3.

IV. NUMERICAL EXAMPLES AND SIMULATIONS

This section presents the simulation results of the proposed control scheme for different examples.

A. 2D uncertain manipulation system

The following 2D example relates to a grasp with two contact points. The contact forces $f_c = [f_{c_{1x}} f_{c_{1y}} f_{c_{2x}} f_{c_{2y}}]^T \in \mathbb{R}^4$ have to satisfy the following Coulomb friction constraints (Fig. 5):

$$\begin{pmatrix} -1 & -\mu & 0 & 0 \\ 1 & -\mu & 0 & 0 \\ 0 & 0 & -1 & -\mu \\ 0 & 0 & 1 & -\mu \end{pmatrix} \begin{pmatrix} f_{c_{1x}} \\ f_{c_{1y}} \\ f_{c_{2x}} \\ f_{c_{2y}} \end{pmatrix} < \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \quad (32)$$

with the friction coefficient $\mu = 1$. The grasp map is:

$$G_0 = \begin{pmatrix} 0 & -1 & 0 & 1 \\ 1 & 0 & -1 & 0 \\ r_o & 0 & r_o & 0 \end{pmatrix} \quad (33)$$

with the length of the rectangular object fixed to $r_o = 20mm$. Two types of uncertainties are considered:

E1 Translation error (Fig. 5a). The direction of the contact force is considered as known, but the location of the contact point is uncertain. The grasp map becomes:

$$G_r = \begin{pmatrix} 0 & -1 & 0 & 1 \\ 1 & 0 & -1 & 0 \\ r_o & 0 & r_o & \delta \end{pmatrix} \quad (34)$$

where $\delta = \pm 5mm$ represents the translation uncertainty of the second contact point.

E2 Orientation error (Fig. 5b). The location of the contact point is considered as known but the orientation of the contact force is uncertain. The grasp map becomes:

$$G_r = \begin{pmatrix} 0 & -1 & \sin(\theta_\delta) & \cos(\theta_\delta) \\ 1 & 0 & \cos(\theta_\delta) & \sin(\theta_\delta) \\ r_o & 0 & r_o \cos(\theta_\delta) & -r_o \sin(\theta_\delta) \end{pmatrix} \quad (35)$$

with $\theta_\delta = \pm 10^\circ$ being the orientation error of the second contact point.

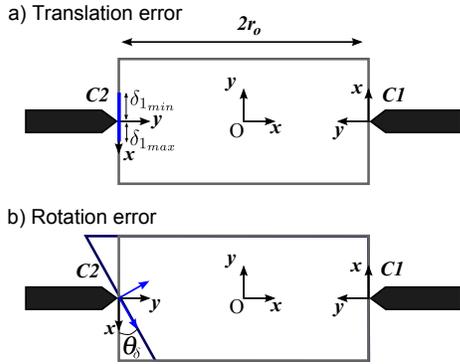


Fig. 5. Proposed example: a) translation error and b) rotation error

B. Results

The motion control was designed with the following LMI parameters:

- $\alpha = 0.5$, which ensures $Re(pole) < -0.5$, providing a stability constraints and minimal dynamics.
- $\theta = 25$, which guarantees a damping ratio of $\xi \simeq 0.6$.
- $r = 7$, which sets the maximal dynamics.

The algorithm (31) (called thereafter *Fast Controller*) was tested for the motion control and compared with another feasible controller designed without trace minimization (called thereafter *Feasible Controller*), i.e. in the previously defined LMI region. The LMI-based optimization algorithm was applied for the two examples (E1-E2). The motion consists in placing the object on the right with a different orientation (Fig. 7.a-c and 8).

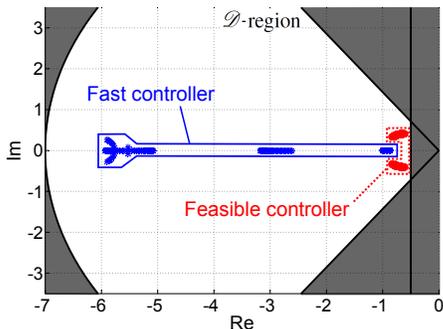


Fig. 6. Closed-loop poles for all the *discretized-P₂* systems with 0.5 mm step on δ

The following observations can be made:

- The poles of all the *discretized-P₂* systems are in the \mathcal{D} -region (Results are presented for example E1 in Fig. 6) for the *Fast* and *Feasible Controllers*. The fast behavior is obtained by placing the poles on the left side of the LMI region.
- The static error is negligible in the two examples (Fig.7.a-c and 8), whatever the chosen behavior (fast or feasible) is, and when no external disturbance is applied. The control law is therefore robust to model uncertainties: recall that an estimation of the nominal hand Jacobian \hat{J}_{heq} is used in the controller, while the true hand Jacobian $J_h(q, x_o)$ varies in the model during the simulation.
- Fast behavior is achieved. In Fig. 7.a-c, a faster response of the system is found with the *Fast Controller* than with the *Feasible Controller*.
- The magnitude of the control input is admissible (Fig. 7.d). This result is found by setting the circle LMI region, defining the maximal dynamics.

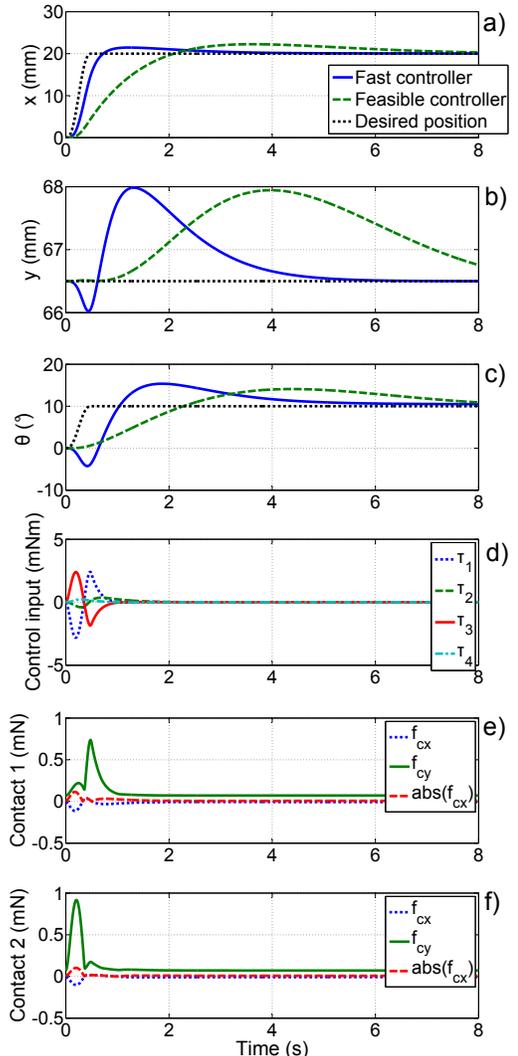


Fig. 7. Dynamic response (Example E1)

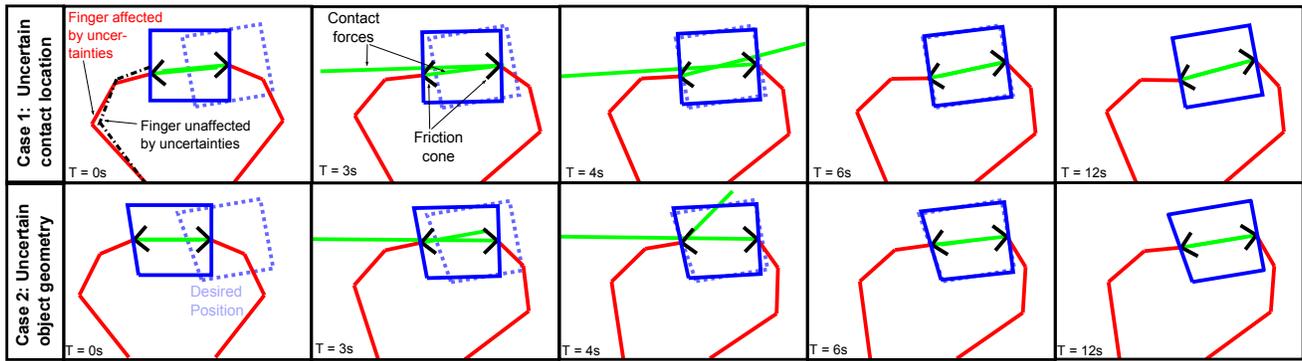


Fig. 8. Simulation.

- The contact forces remain in the friction cone during the movement (Fig. 8 and 7.e-f). The contact force on the y-axis is always positive, meaning that only unilateral forces can be applied, and f_{c_y} is always higher than $|f_{c_x}|$, validating the cone constraint. An offset on λ , i.e. f_{c_y} , of $100\mu N$ was introduced to achieve robustness to external disturbances, e.g. an external wrench applied at the object level.

V. CONCLUSIONS

The paper presents a new control law to cope with contact uncertainties for dexterous manipulation with a multifingered hand. Three objectives are achieved: (i) motion tracking of the object without any static error, (ii) satisfaction of the system constraints, i.e. unilaterality of the contact forces, friction constraints, and bounded joint torques, (iii) robustness to contact uncertainties. The controller was tested on two cases, translation and rotation errors, the objectives were fulfilled and a robust behavior was observed.

The problem of the robustness to contact uncertainties addressed in this paper could be related to dexterous manipulation by a human without tactile sensing [20] [21]. It would be interesting to compare the proposed control scheme with the human control.

Next works will consider the non redundant case and 3D examples. Knowing that the algorithm is based on a linearized model, it would be interesting to evaluate the region of the workspace where the desired properties of the closed loop are guaranteed. Next step will be to implement and test the proposed controller in a practical case.

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